

Lecture #19

Digital To Analog, PWM, Stepper Motors

18-348 Embedded System Engineering

Philip Koopman

Monday, 28-March-2016

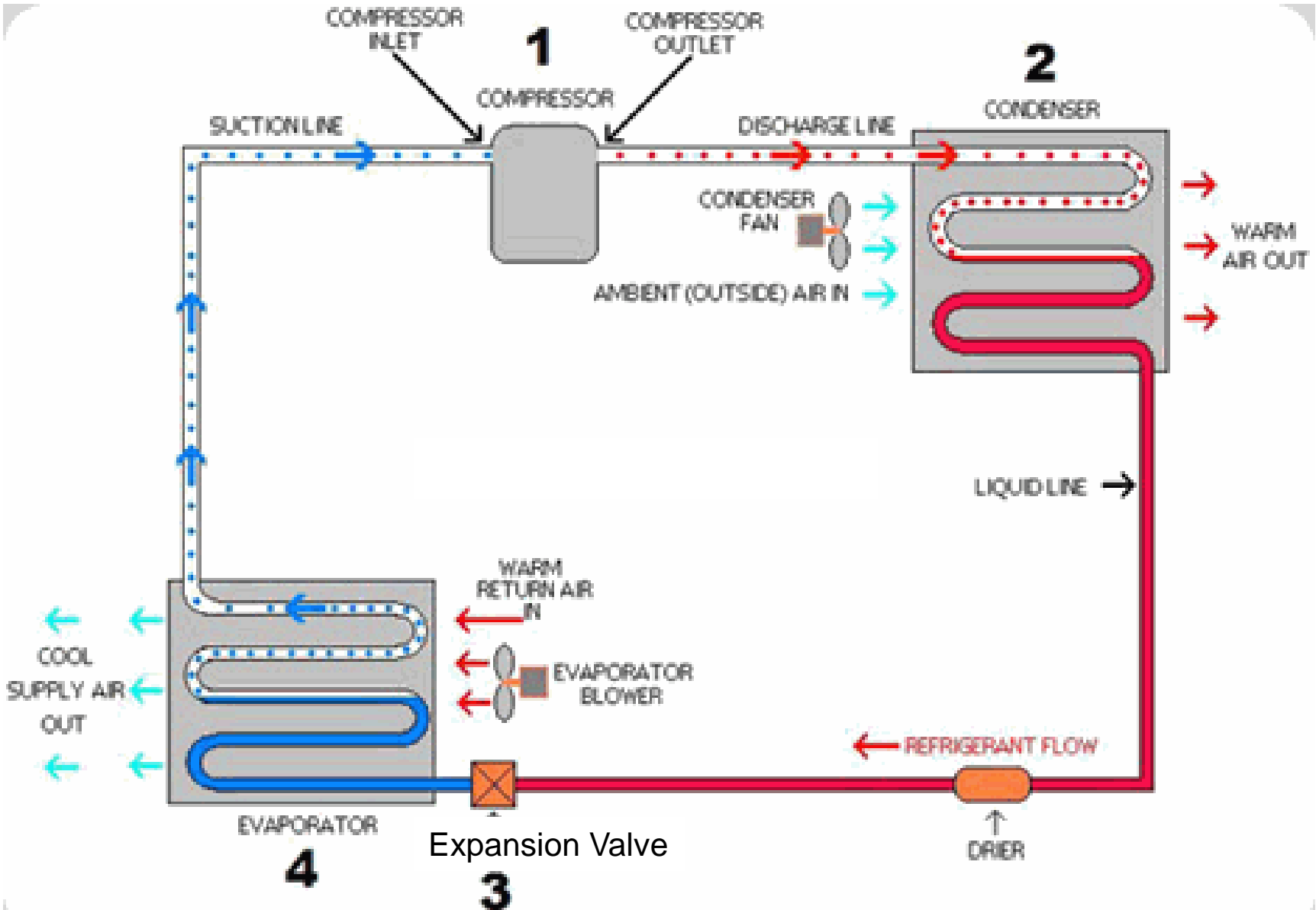


Electrical & Computer
ENGINEERING

© Copyright 2006-2016, Philip Koopman, All Rights Reserved

**Carnegie
Mellon**

Example System: HVAC Compressor



HVAC Embedded Control

◆ Compressors (reciprocating & scroll)

- Smart loading and unloading of compressor
 - Want to minimize motor turn on/turn off cycles
 - May involve bypassing liquid so compressor keeps running but doesn't compress
- Variable speed for better output temperature control
- Diagnostics and prognostics
 - Prevent equipment damage (e.g., liquid entering compressor, compressor stall)
 - Predict equipment failures (e.g., low refrigerant, motor bearings wearing out)

◆ Expansion Valve

- Smart control of amount of refrigerant evaporated
 - Often a stepper motor
- Diagnostics and prognostics
 - Low refrigerant, icing on cold coils, overheating of hot coils

◆ System coordination

- Coordinate expansion valve and compressor operation
- Coordinate multiple compressors
- Next lecture – talk about building-level system level diagnostics & coordination

Where Are We Now?

- ◆ **Where we've been:**
 - Interrupts, concurrency, scheduling, RTOS
- ◆ **Where we're going today:**
 - Analog Output
- ◆ **Where we're going next:**
 - Analog Input
 - Human I/O
 - Very gentle introduction to control
 - ...
 - Test #2 and last project demo

Preview

◆ Digital To Analog Conversion

- Example implementation
- Understanding performance
- Low pass filters

◆ Waveform encoding

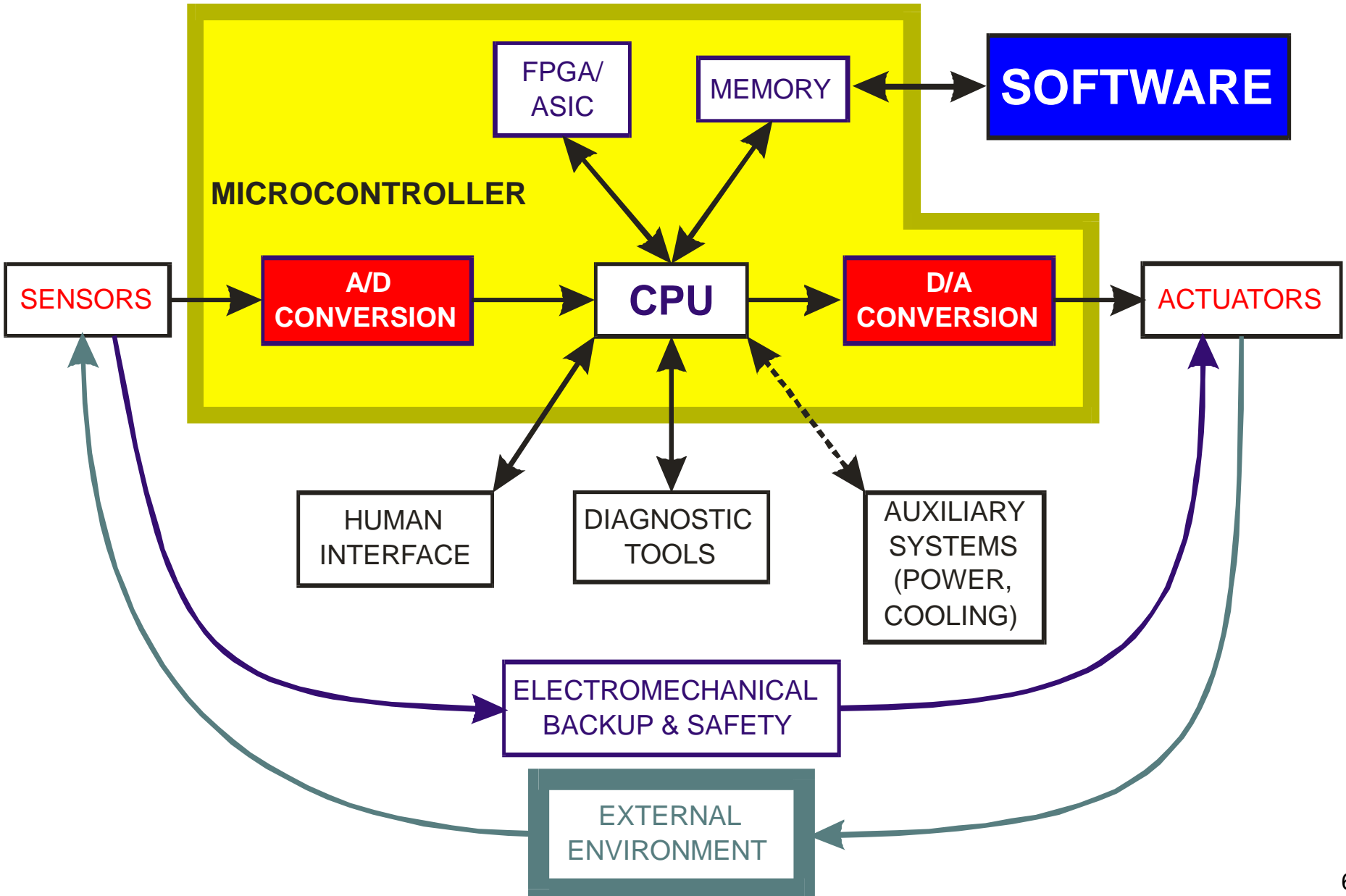
◆ PWM

- Digital way to “fake” analog
- How to use course processor PWM support hardware
- How a servo works

◆ How a stepper motor works

- Note: 3-D printers are mostly stepper motors + PWM

Big Picture – I/O Is Where The Work Gets Done!



Analog → Digital → Analog Conversion

◆ The real world is analog

- Voltage, current are continuous
- Time is continuous

◆ But the computing world is discrete

- Bits, bytes
- Some sensors/actuators use digital values...
... but many deal with analog values

◆ A/D conversion “analog to digital”

- Getting analog inputs to digital form

◆ D/A conversion “digital to analog”

- Getting digital inputs to analog form

◆ Digital I/O

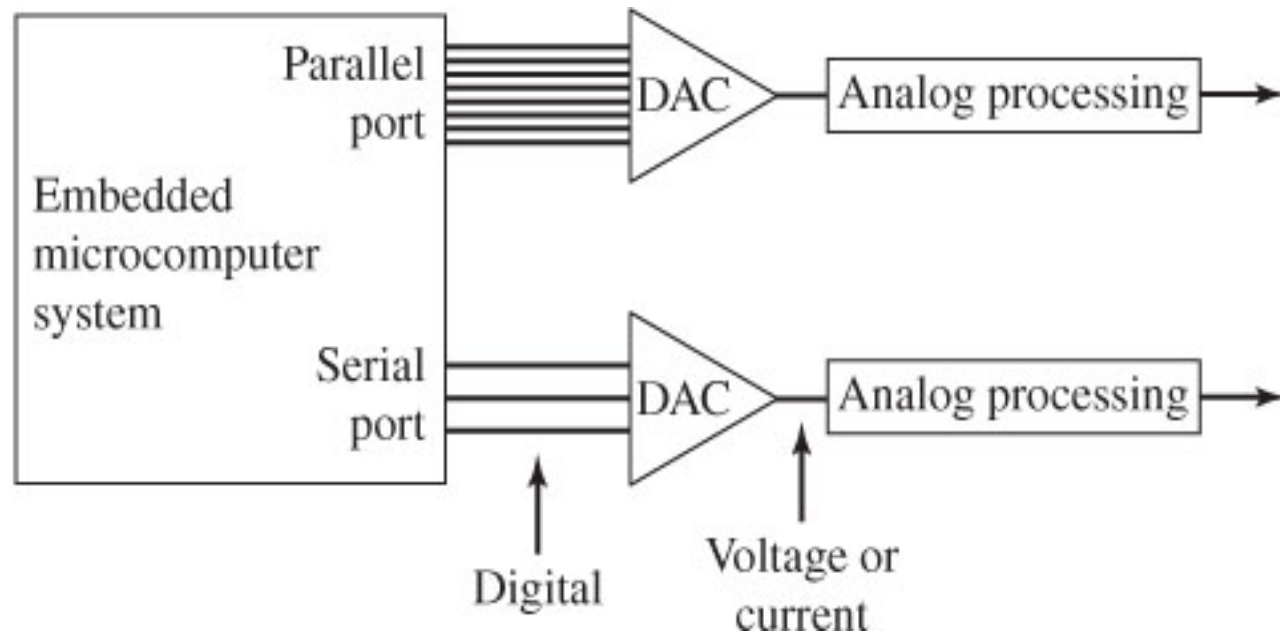
- Sometimes you can fake analog values with digital (e.g., digital pulsing)

D/A Conversion

- ◆ “DAC” = “D/A Converter” = “Digital To Analog Converter”
- ◆ Given several bits of a digital value, convert it to an analog value
 - Usually voltage or current
 - Many drives an actuator, further converting output into motion, heat, light, etc.
 - Might be directly connected to CPU or accessed via a serial bus

Figure 11.33
DACs provide analog output for our embedded microcomputer systems.

[Valvano]



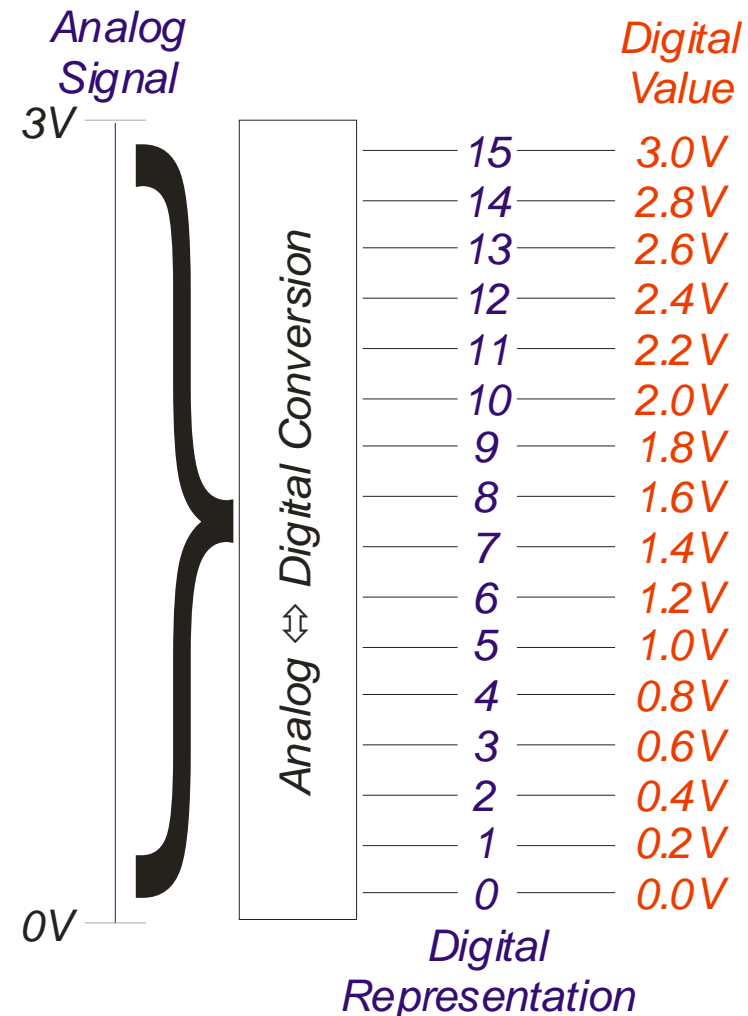
General Idea Of A DAC

◆ Input is bits

- k-bit value, often 8 bits but can be any integer number
- Signed or unsigned number (often unsigned)

◆ Output is an analog value (volts, amps)

- Digital value determines output
- Can be output many ways:
 - Absolute voltage
 - Offset added to reference voltage
 - Current (mAmps, Amps)



Analog Circuits Aren't "Ideal"

- ◆ Real DACs have offset error, gain error, slew, ringing, nonlinearities...

Figure 11.35

Static and dynamic performance measures of DACs.

[Valvano]

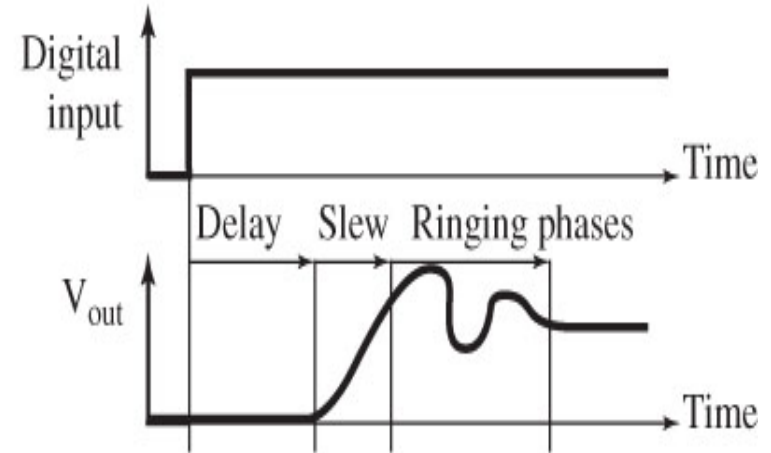
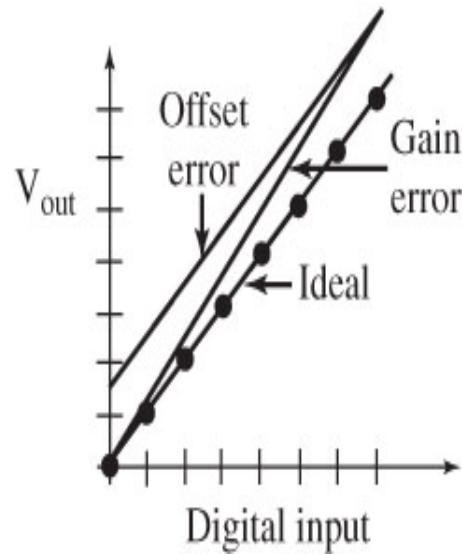
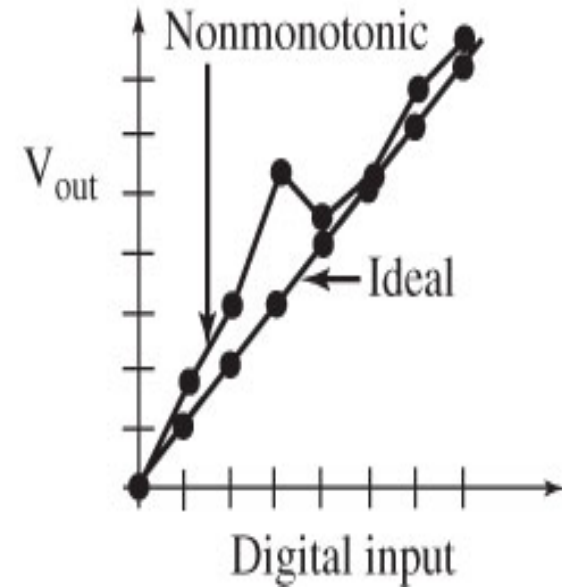
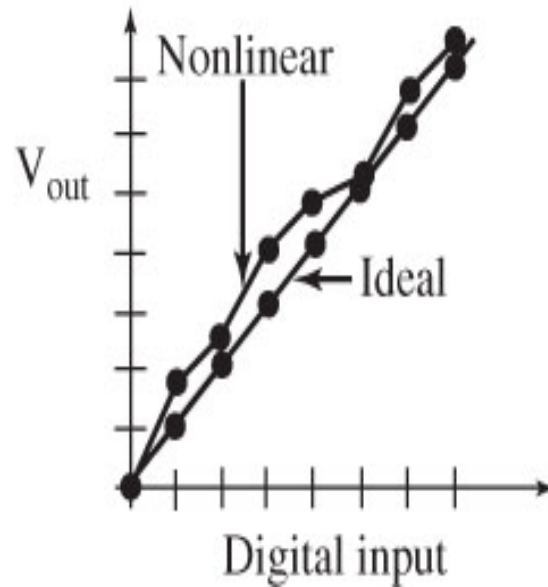


Figure 11.36

Nonlinear and nonmonotonic DACs.

[Valvano]

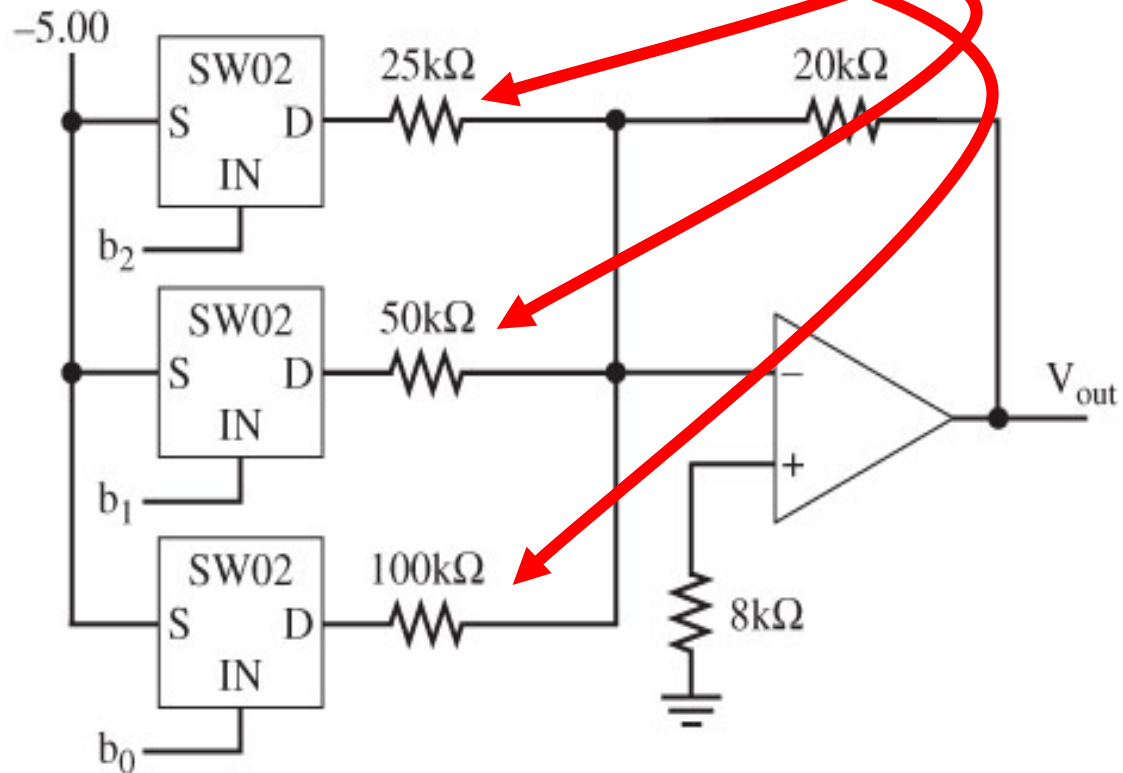


Example 3-Bit DAC

◆ Operating Principle for “Summing DAC”:

- One switch per bit; bit closes switch when “on”; opens switch when “off”
- Different resistor values put different voltages out
- Net resistance (hence input voltage) subject to parallel resistance value
- Note: each resistor 2x previous resistor
 - Each bit contributes half the voltage of the next higher bit

Figure 11.38
Three-bit unsigned summing DAC.



[Valvano]

DAC Performance

◆ Usually, DACs attempt to be linear:

$$V_{out} \approx V_{fullscale} \left(\frac{b_7}{2} + \frac{b_6}{4} + \frac{b_5}{8} + \frac{b_4}{16} + \frac{b_3}{32} + \frac{b_2}{64} + \frac{b_1}{128} + \frac{b_0}{256} \right) + V_{offset}$$

- Notes: $V_{fullscale}$ input in this equation has to be 1/256 above output “full scale”
 - If all these bits are on, result is 255/256 of $V_{fullscale}$
- V_{offset} is supposed to be zero in most applications
- Doesn't take into account non-ideal behaviors!

◆ Quantization effects – value

- Analog value isn't exact
- Analog value is approximated via a “bin” or voltage quantum
- Bin size is $\sim 1/2^K$ of full scale (not quite because of the “fencepost” numbering issue)

◆ Quantization effects – time

- Analog value produced periodically by CPU
- Not continuously as with real analog signal!

Generating An Analog Waveform – Computed

◆ Periodic output values

- Use timer-based interrupt
- (What is the problem with this particular example from Valvano?)

Program 11.2

Periodic interrupt used to create the analog output waveform.

```
unsigned short wave(unsigned short t){
    float result,time;
    time=2*pi*((float)t)/1000.0;
    // integer t in msec into floating point time in seconds
    result=2048.0+1000.0*cos(31.25*time)-500.0*sin(125.0*time);
    return (unsigned short) result;}
```

```
#define Rate 2000
#define OC5 0x20
unsigned short Time; // Inc every 1ms
#pragma interrupt_handler TOC5handler()
void TOC5handler(void){
    [Valvano] TFLG1=OC5; // ack C5F
    TC5=TC5+Rate; // Executed every 1 ms
    Time++;
    DACout(wave(Time));}
```

Generating An Analog Waveform – Table Based

```
// 6811
#define Rate 2000
#define OC5 0x08
#pragma interrupt_handler TOC5handler()
void TOC5handler(void){
    TFLG1=OC5;    // Ack interrupt
    TOC5=TOC5+Rate; // Executed every 1 ms
    if(++I==32) I=0;
    DACout(wave[I]);}
```

```
// 6812
#define Rate 2000
#define OC5 0x20
#pragma interrupt_handler TOC5handler()
void TOC5handler(void){
    TFLG1=OC5;    // ack C5F
    TC5=TC5+Rate; // Executed every 1 ms
    if(++I==32) I=0;
    DACout(wave[I]);}
```

Program 11.5

Periodic interrupt used to create the analog output waveform.

Program 11.4

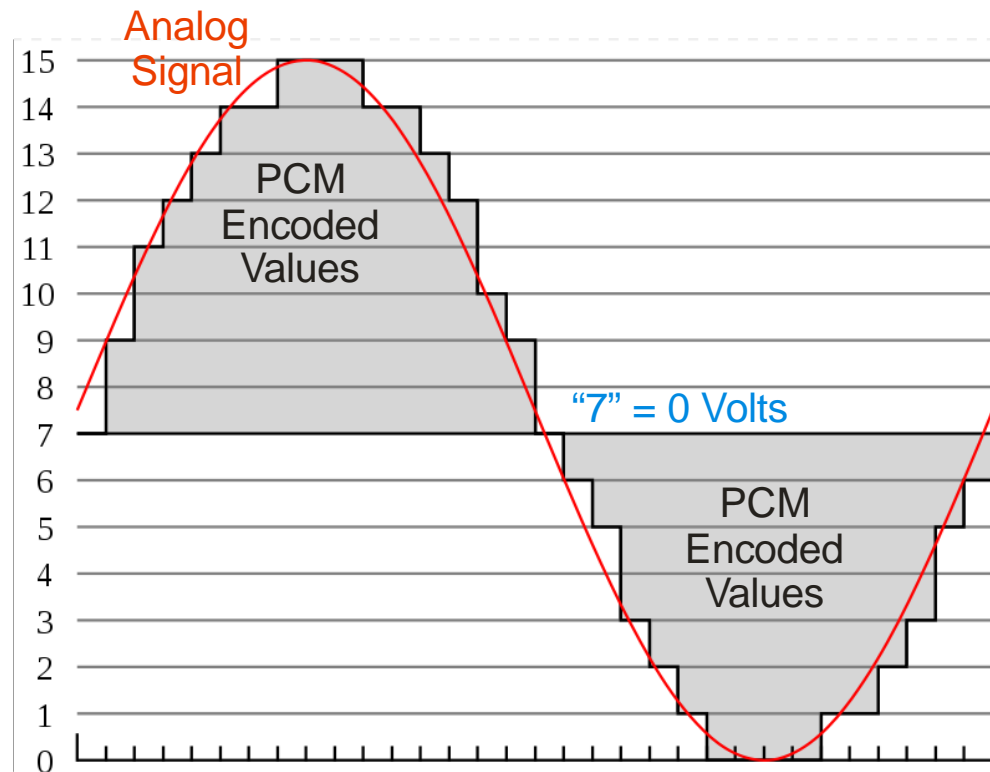
Simple data structure for the waveform.

[Valvano]

```
unsigned short I; // incremented every 1ms
const unsigned short wave[32]= {
    3048,2675,2472,2526,2755,2957,2931,2597,
    2048,1499,1165,1139,1341,1570,1624,1421,
    1048,714,624,863,1341,1846,2165,2206,2048,
    1890,1931,2250,2755,3233,3472,3382};
```

Encoding Waveforms – PCM

- ◆ **Sample rate – how often are the samples?**
 - Want samples at least twice as fast as highest frequency component (a.k.a. Nyquist Rate)
- ◆ **PCM – Pulse Code Modulation**
 - Use the binary value in each sample
 - Use as an unsigned value
 - Typically put zero point in middle
 - E.g. 0-15; 7 = 0 Volts
 0 = -5 Volts
 - Example:
CD-Audio is 16-bit PCM at 44 KHz (stereo – two channels)
 - Why 44 KHz?



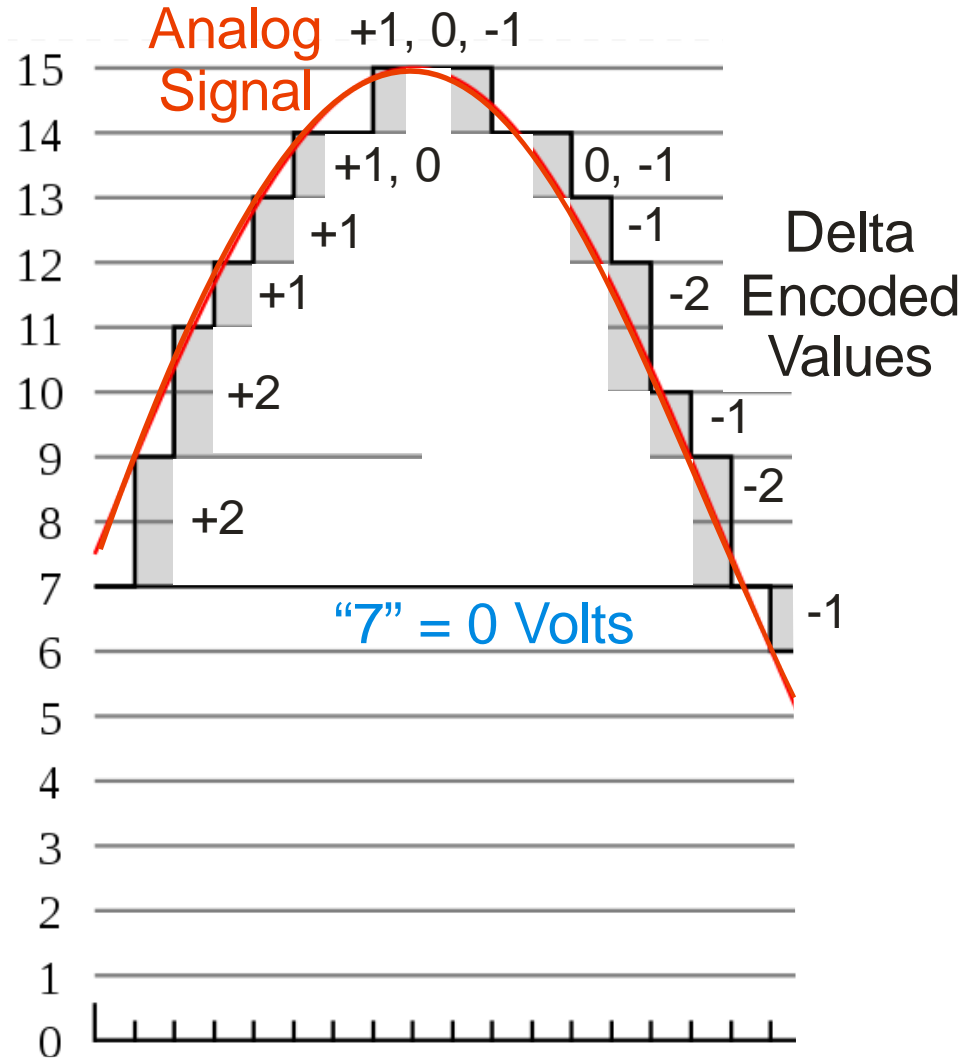
Delta Modulation

◆ Delta Modulation

- Use the difference from last sample
- Uses fewer bits per sample...
... but assumes signal changes gradually
- Bits per sample related to bandwidth of signal – higher bandwidth means bigger deltas (more bits per sample)
- Example on right is, perhaps, 3 bit encoding: $\{-4, -3, -2, -1, 0, 1, 2, 3\}$
- Values are twos complement rather than unsigned
- Values must be added to running total (i.e., integrated)

◆ Other more sophisticated encodings

- Linear predictive coding
- Application-specific coding (MP3, etc.)



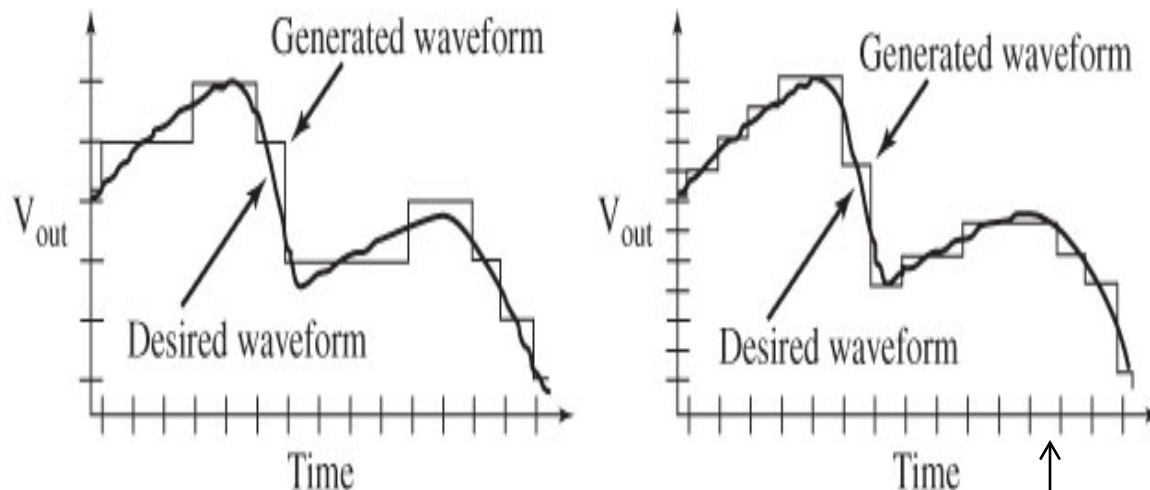
It's All About The Bandwidth – Bits Per Second

◆ Increasing # bits of resolution improves output waveform

- Reduces value quantization error

Figure 11.46

The waveform on the right was created by a DAC with one more bit than the left.



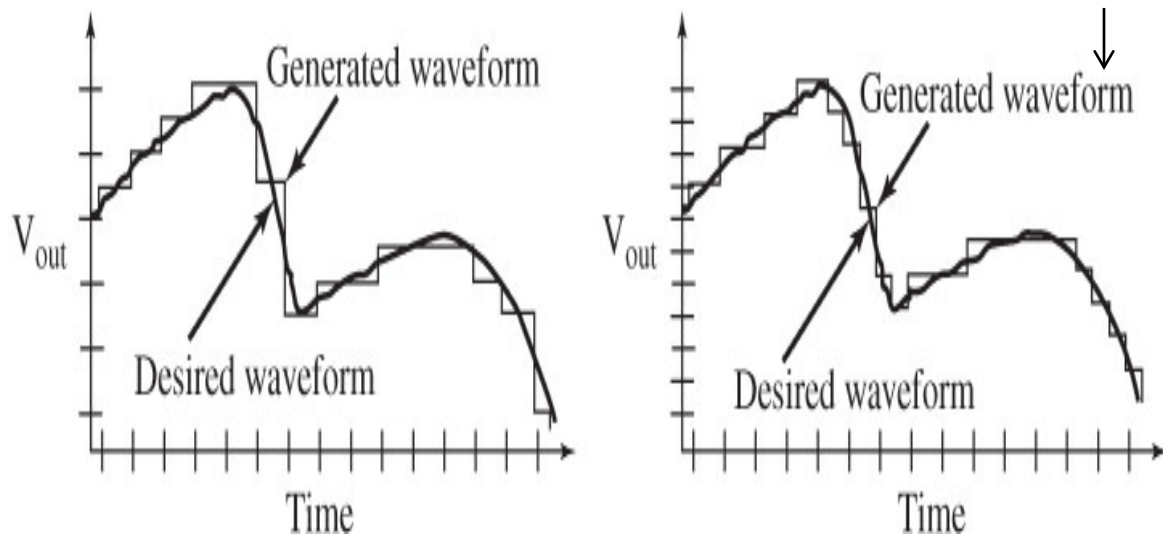
[Valvano]

◆ Increasing sample rate improves output waveform

- Reduces time quantization error

Figure 11.47

The waveform on the right was created by a system with twice the output rate than the left.



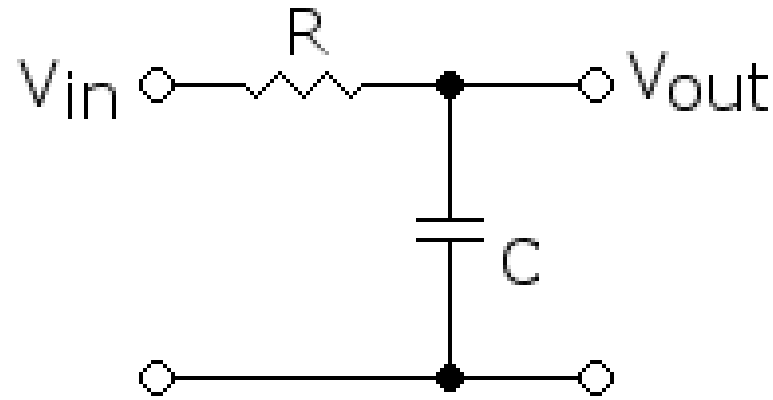
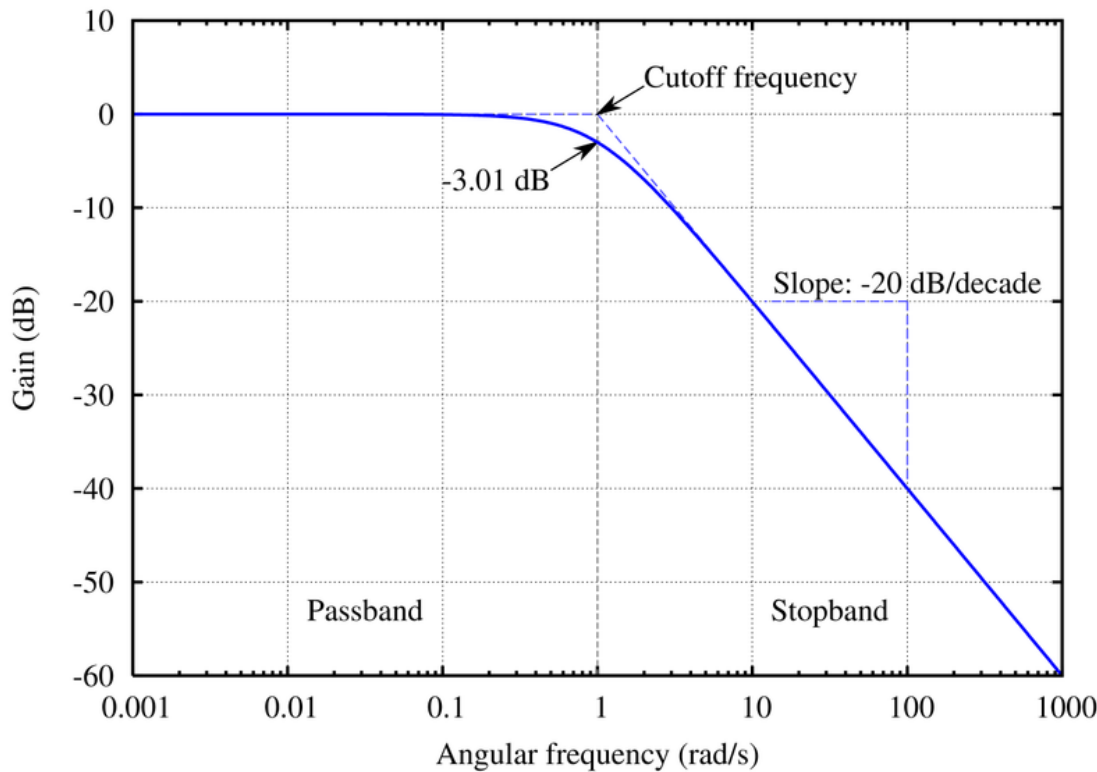
PICTURES REVERSED

[Valvano]

Low Pass Filters

◆ Can we get rid of the bumps in the output?

- Add more bits (expensive, doesn't necessarily work very well)
..OR..
- Use a Low Pass Filter!



[Wikipedia]

◆ Or, sometimes ... do nothing (implicit low pass filter)

- Physical time constants of controlled system or actuators might smooth bumps!

Pulse Modulation

◆ DACs are expensive – take a lot of area

- And even more if you want lots of analog output channels!
 - The course processor doesn't even have D/A outputs built into it
- So, how do you actually do D/A conversion without a DAC?
- Preferably using a *single output pin*?
- Preferably in a way that is lower noise than a DAC (e.g., purely digital)

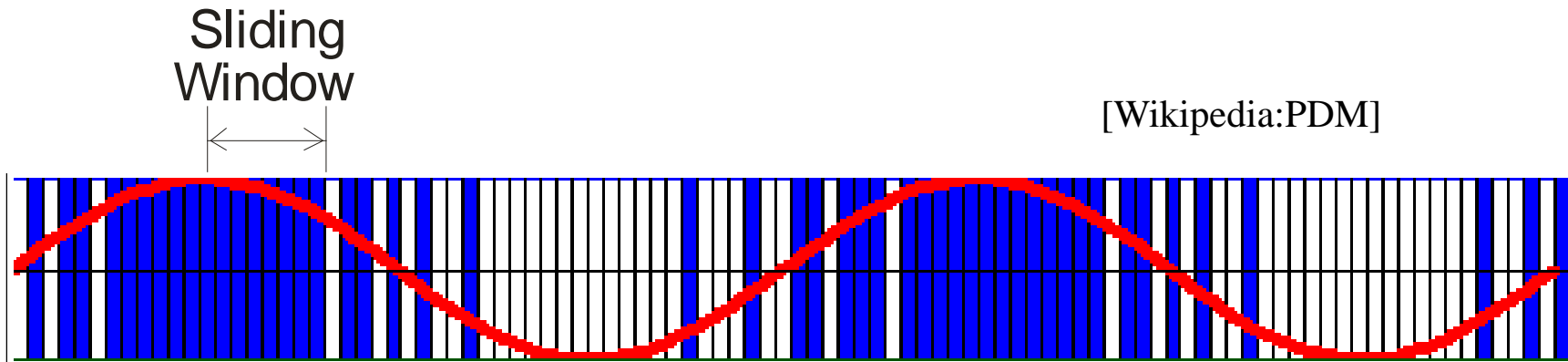
◆ Can use purely digital output to “fake” analog output

- Pulse Density Modulation
 - Use high speed bit stream to represent proportion of full scale value
- Pulse Width Modulation
 - Send varying width of pulses to change power/duty cycle of actuator
- Others:
 - Pulse Rate modulation (how often a pulse is sent)

Pulse Density Modulation

◆ Look at a sliding window of p pulses

- Bit value of 1 = “+1” Bit value of 0 = “-1”
- Signal value is the sum of the +1 and -1 values of the bits in the window
- Generally want very high bit rate for this to work (used in audio systems)
 - Works on AC signals; can have offset error on slow or DC signals
- Get analog output with LP Filter (capacitor does analog work)



◆ How do you know signal is going down just after the peak?

- When first -1 enters sliding window, output starts going down
- Output is phase-shifted to the right by the sliding window size

PDM Implementation Sketch

```
for(;;)
{ { if (<next sample time>) { <update desired_output> }
  if (desired_output > current_output)
  { output(1);    // Go up if we are currently too low
    current_output += delta_value;
  } else
  { output(0);    // Go down if we are currently too high
    current_output -= delta_value;
  }
  <wait for next output bit time; constant bit rate>
}
```

◆ Tradeoffs:

- With only two values, analog noise less of an issue (only “hi” and “lo”)
- Direct tradeoff of value quantization vs. time quantization
 - Big window gives more values, but takes longer to make big changes
 - Small window has less phase shift, but supports fewer total values
 - It’s all about the bandwidth – bits per second is the limiting factor

Pulse Width Modulation

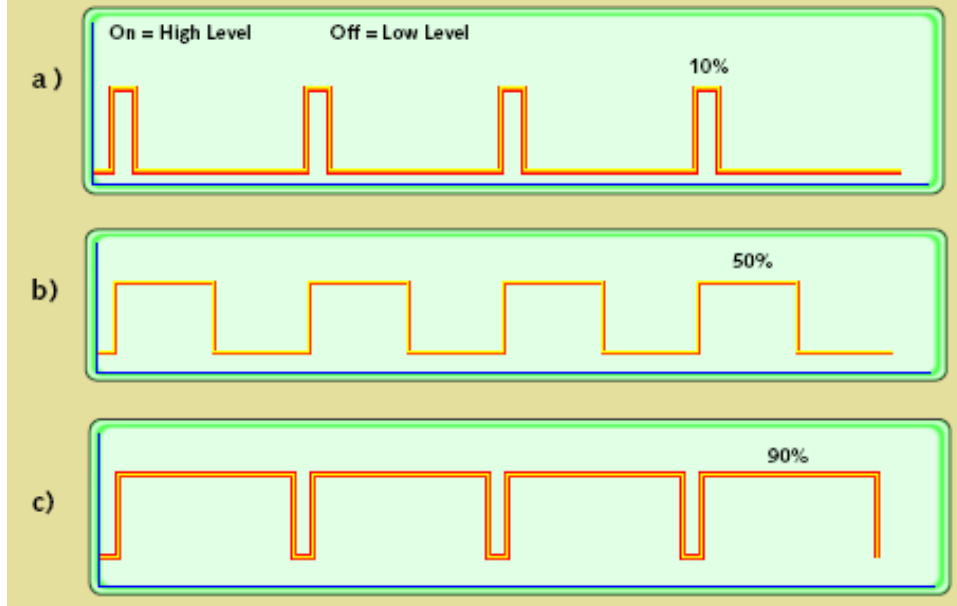
◆ Idea: represent value with high/low duty cycle

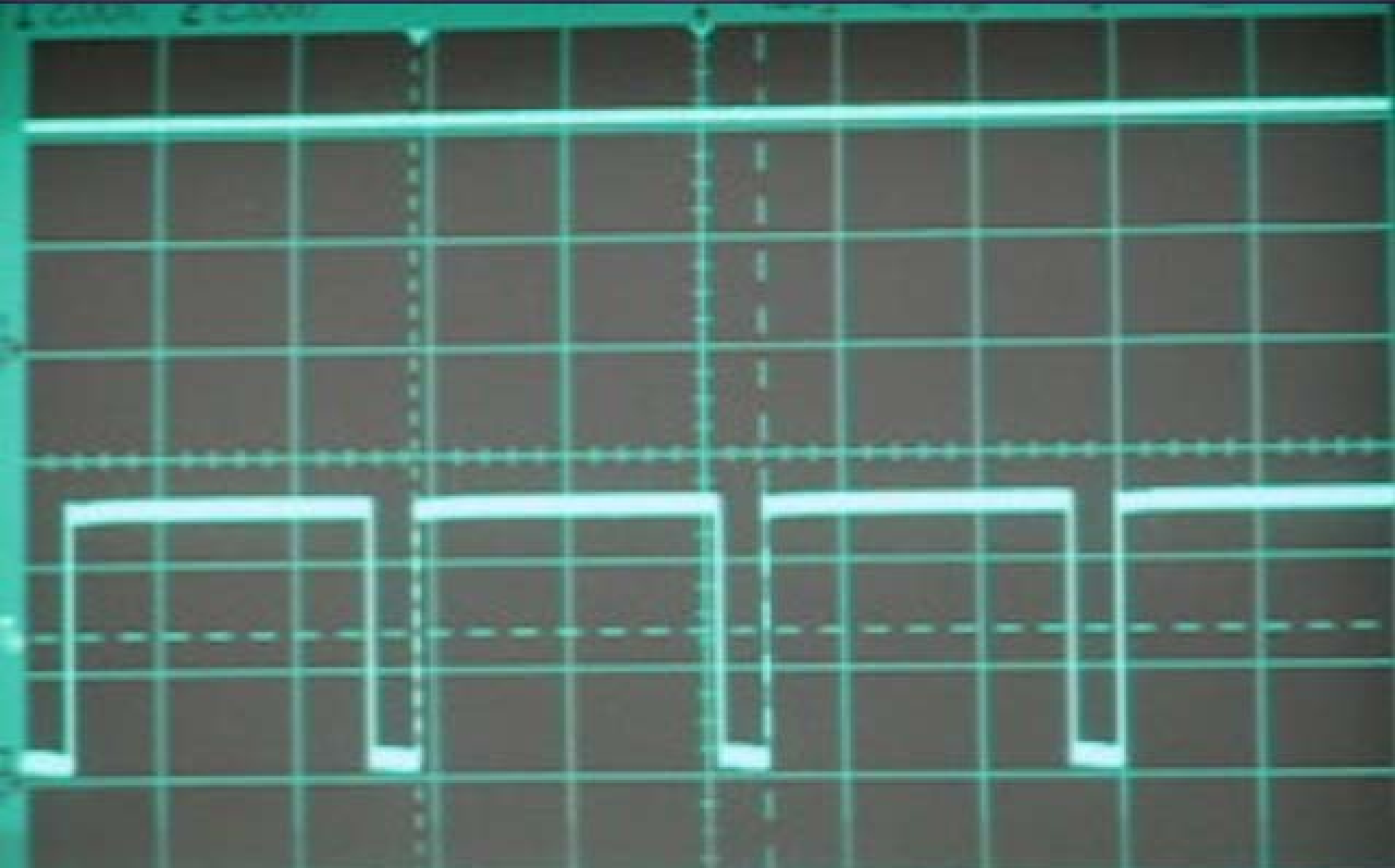
- Constant period, some high and some low within period
- e.g., 30% duty cycle: 3 msec high, 7 msec low (10 msec period)
- e.g., 90% duty cycle: 90 msec high, 10 msec low (100 msec period)

◆ Can be used to deliver varying levels of power

- This is how LED dimming works
- Often relies on time constant of actuator to do LP Filtering “for free”
- Can be used, for example, to control cooling fan speed
 - Physical inertia of the fan integrates pulses into an average fan speed

FIGURE 1 PWM signals of varying duty cycles





Avg(1): 3.952V Duty(2): 82.0% Period(2): 512ns

← →
✓

1

2
✓

▲ Ext

PWM Block Diagram

- ◆ See Chapter 12 of MC8S12 data sheet for details

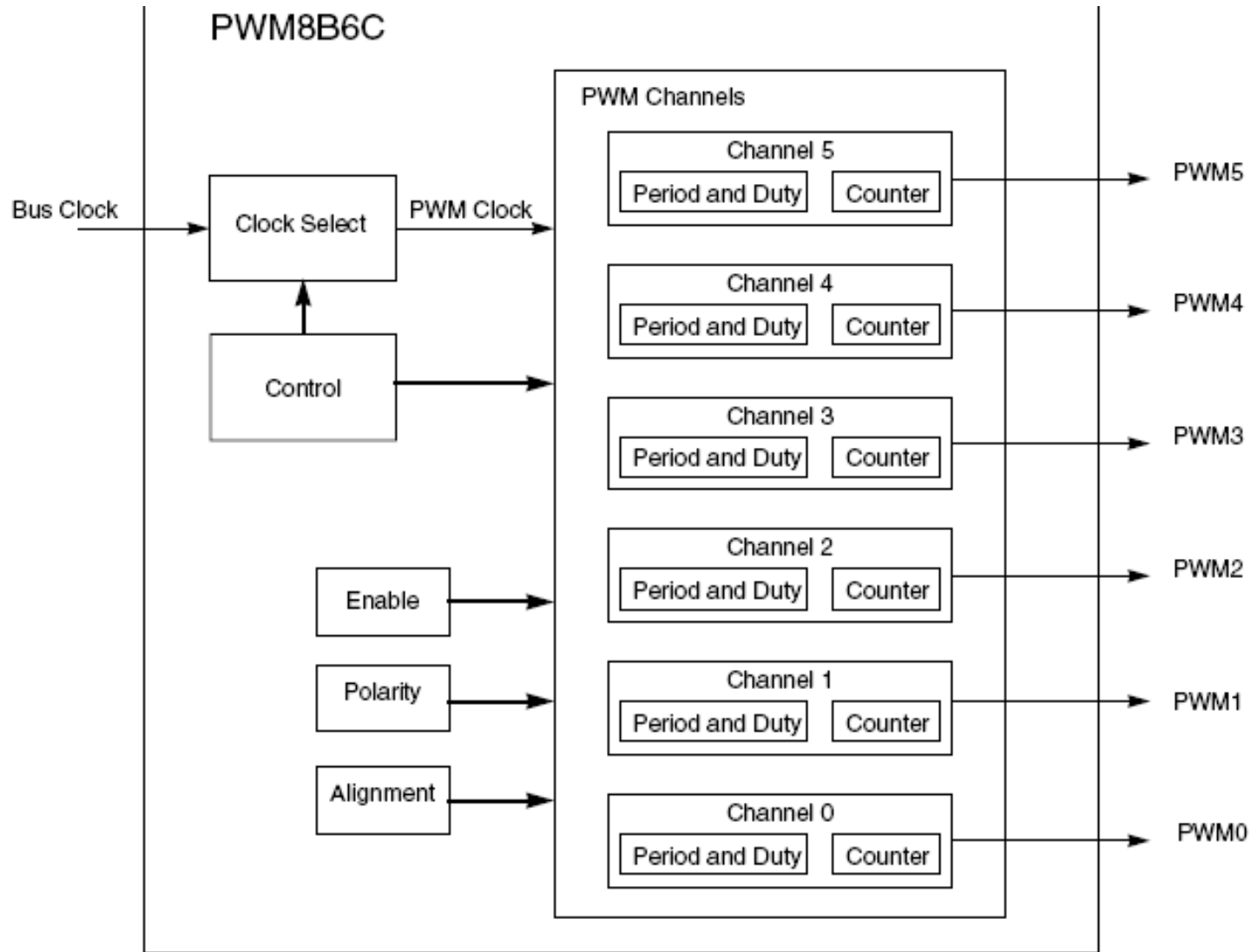


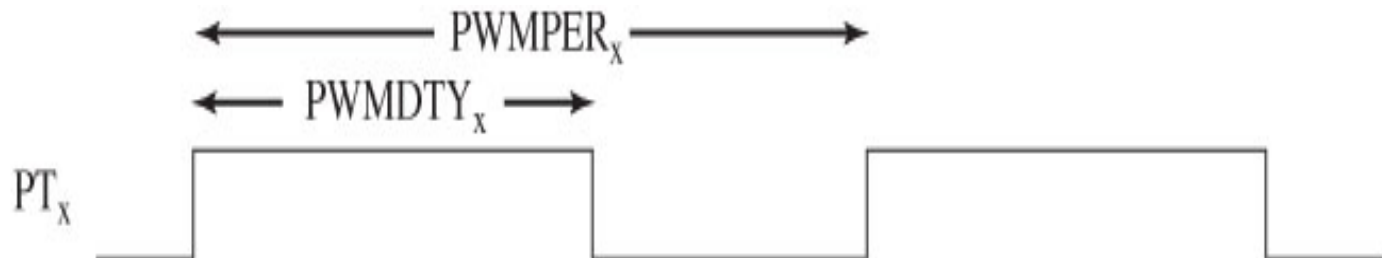
Figure 12-1. PWM8B6CV1 Block Diagram

PWM Registers

- ◆ **MODRRx – Timer vs. PWM channel x (1 = PWM)**
- ◆ **PWME_x – enable PWM channel x (1 PWM)**
- ◆ **PWMPOL_x – polarity**
 - 0 = low followed by high (first part of pulse is low)
 - 1 = high followed by low (first part of pulse is high)
- ◆ **PWMPRCLK – clock prescaler (similar to other clock prescalers)**
- ◆ **PWMCLK – clock select for PWM (Clock A/B or Clock SA/SB)**
 - Clocks SA/SB are scaled versions of Clock A, Clock B
 - E.g., PWMSCLA is scaling value for Clock A – lets it run up to 512x slower
- ◆ **PWMCTL – control register concatenation**
 - Concatenates pairs of 8-bit counters to give 16-bit counters
 - CON23: channel 2 register is high-order byte of a 16-bit channel
- ◆ **PWMPER_x – period for channel**
- ◆ **PWMDTY_x – duty cycle for channel**
- ◆ **PWMSDN – optional pin for emergency shutdown of pulses**
 - Interrupt vector \$FF8C
 - Why do you want emergency shutdown of pulses?

Figure 6.24

PWM output generated
when PPOL=1.



```
;MC9S12C32 assembly
```

```
PWM_Init3          ;1s PWM on PT3
```

```
    bset MODRR,#$08 ;PT0 with PWM
```

```
    bset PWME,#$08 ;enable chan 3
```

```
    bset PWMPOL,#$08 ;high then low
```

```
    bclr PWMCLK,#$08 ;Clock B
```

```
    bset PWMCTL,#$20 ;concat 2+3
```

```
    ldaa PWMPRCLK
```

```
    anda #$8F
```

```
    oraa #$60
```

```
    staa PWMPRCLK      ;B=E/64
```

```
    movw #62500,PWMPER23 ;1s period
```

```
    movw #0,PWMDTY23   ;off
```

```
    rts
```

```
PWM_Duty3          ;RegD is duty cycle
```

```
    std  PWMDTY0      ;0 to 62500
```

```
    rts
```

```
// MC9S12C32 C
```

```
// 1s PWM on PT3
```

```
void PWM_Init(void){
```

```
    MODRR |= 0x08; // PT3 with PWM
```

```
    PWME  |= 0x08; // enable channel 3
```

```
    PWMPOL |= 0x08; // PT3 high then low
```

```
    PWMCLK &=~0x08; // Clock B
```

```
    PWMCTL |= 0x20; // Concatenate 2+3
```

```
    PWMPRCLK = (PWMPRCLK&0x8F)|0x60; // B=E/64
```

```
    PWMPER23 = 62500; // 1s period
```

```
    PWMDTY23 = 0;      // initially off
```

```
}
```

```
// Set the duty cycle on PT3 output
```

```
void PWM_Duty(unsigned short duty){
```

```
    PWMDTY23 = duty; // 0 to 62500
```

```
}
```

Program 6.21

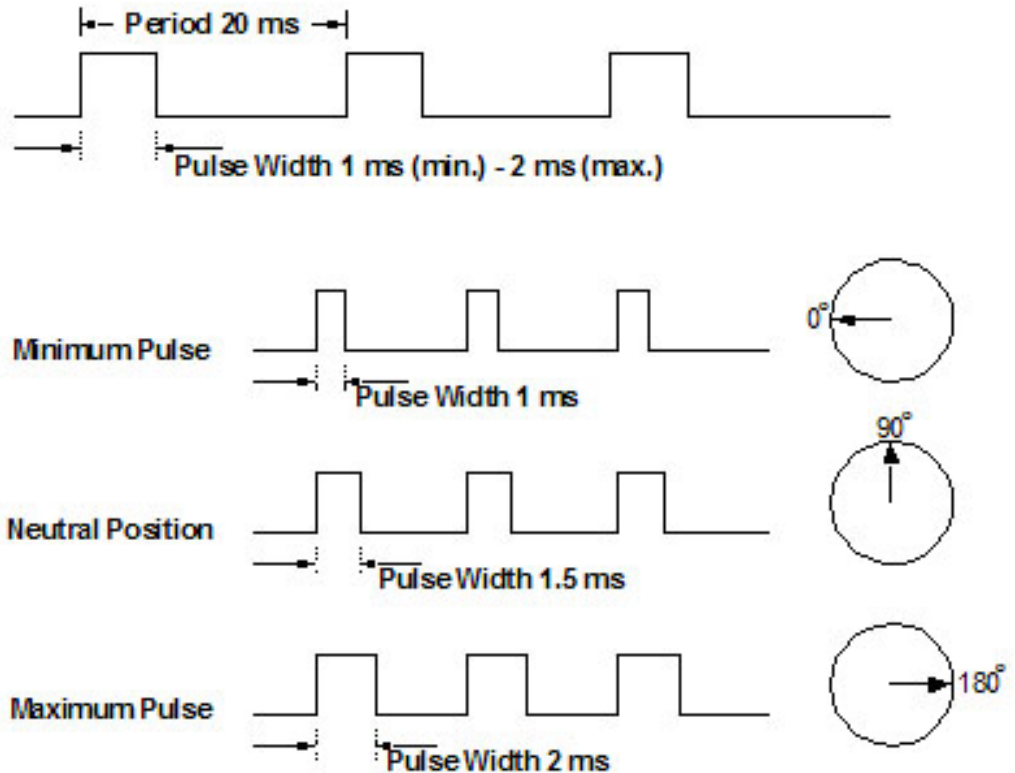
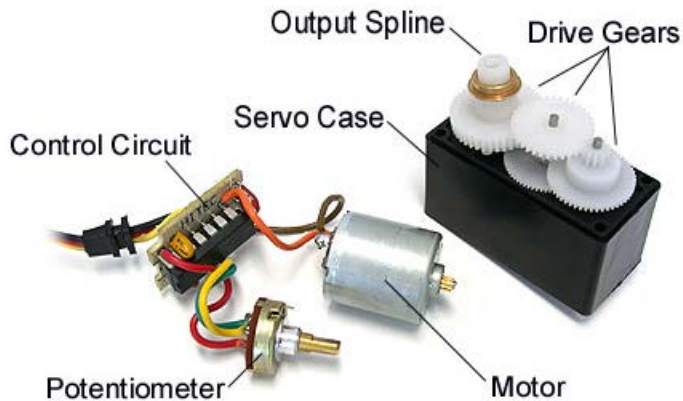
Implementation of an 8-bit PWM output.

[Valvano]

How Do Servos Work?

◆ Uses PWM to set position between “zero” and “full”

- PWM sets commanded position
- Potentiometer used to measure actual position
- Servo self-adjusts to keep actual position at/near commanded position
 - Closed loop control; maintains position even if external forces try to move servo



Is PWM A Free Ride?

- ◆ **Digital values have very low amplitude noise**
 - Analog values – noise shows up in any disturbance
 - Digital values – noise only if signal crosses threshold
- ◆ **Is it a free lunch?**
 - No– still have noise in *timing*
 - Clock edges can move around depending on value noise, ringing, etc.
 - Quantization noise in timing...
 - Based on PWM clocks putting edge in the right place
 - Based on PDM having consistent clock lengths
 - Need enough bits in the PWM counter to manage timing (8 bits or 16 bits)
- ◆ **If you are receiving PWM with a digital device need to do pulse capture**
 - Done using Pulse Accumulator hardware (or relevant software)
 - Can be used to measure frequency (time between edges)
 - Can be used to measure duty cycle (proportion of high to low times)
 - This is in Valvano, but not something we'll cover beyond this mention

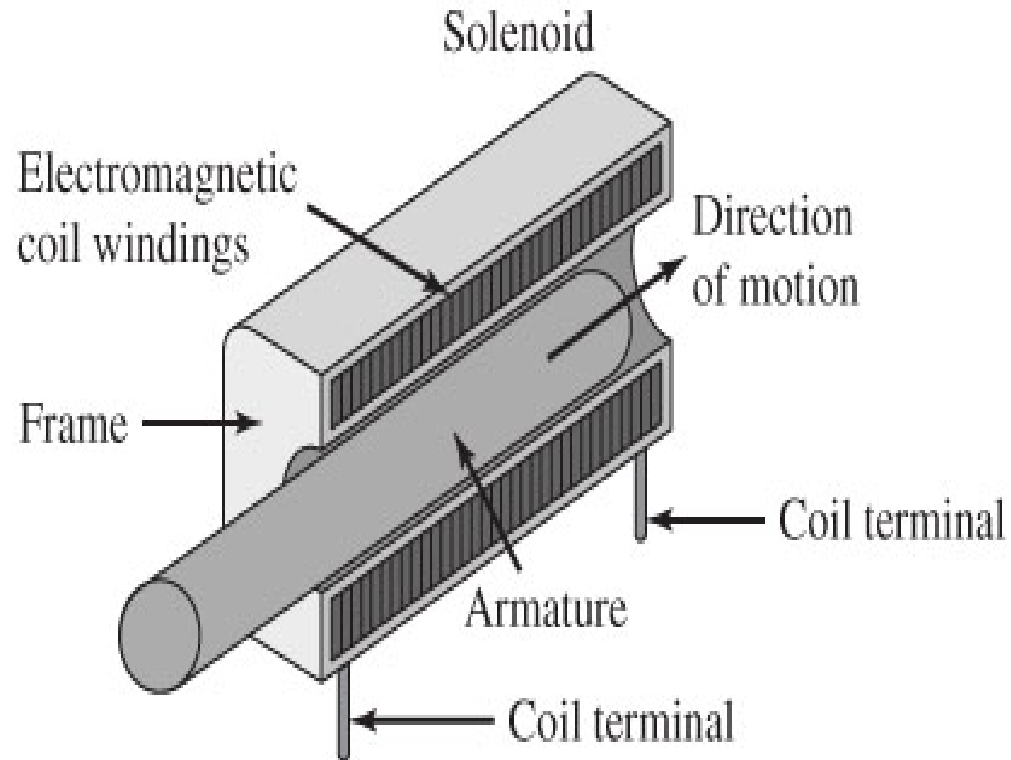
Solenoids

◆ Used to generate a short-stroke linear motion

- Release driven by spring, gravity, or second solenoid on same armature

Figure 8.64

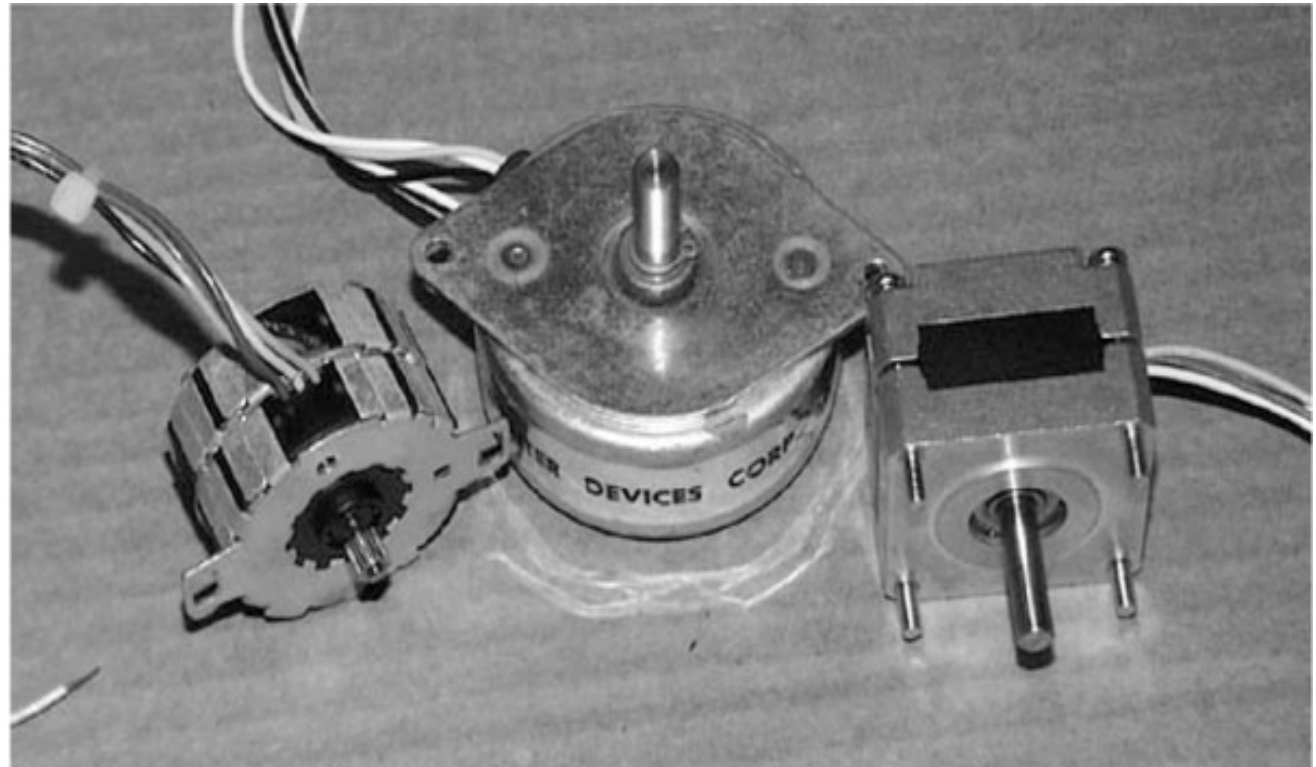
Mechanical drawing of a solenoid showing that the EM coil causes the armature to move.



Stepper Motors

- ◆ Many simple embedded systems use stepper motors
 - Uses a digital (on/off) interface
 - Permits rotating motor to one of a set of rotational positions
 - Gives good positional stability without use of shaft encoder/feedback
 - General motor control is a whole other lecture (or set of lectures)

Figure 8.79
Three stepper motors.



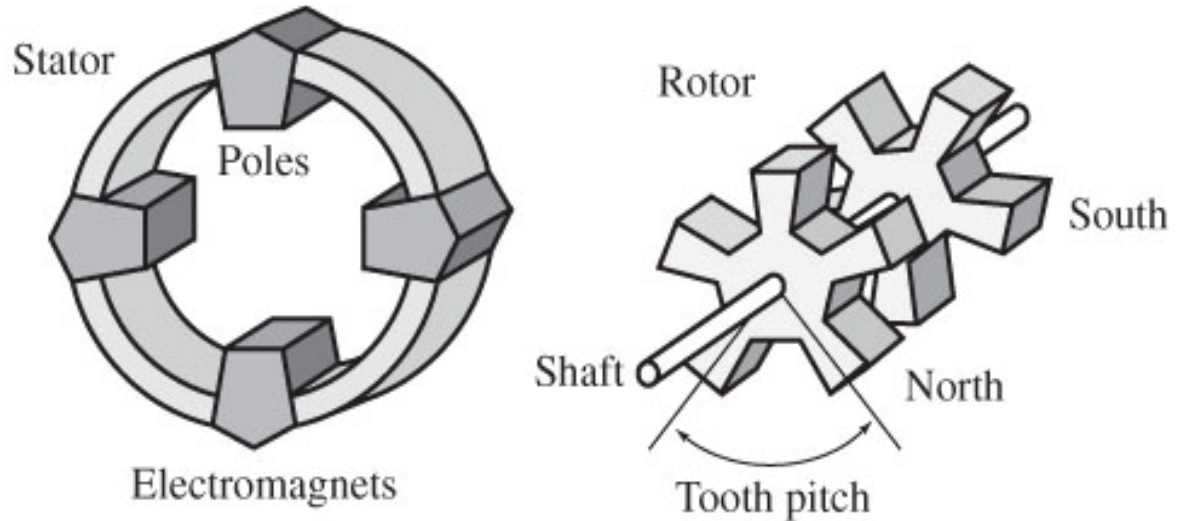
[Valvano]

Stepper Motor General Idea

- ◆ **Magnetic rotors spin, driven by electromagnetic stators**
 - Stator Poles alternate North and South to force motors to spin
 - (animation on following slides)

Figure 8.82

Simple stepper motor with 20 steps per revolution.



- 20 steps per revolution → 18 degrees per step
- 200 steps per revolution → 1.8 degrees per step
- # steps per revolution = # stator coils (phases) * # teeth

Photos Of Stepper Motors

- ◆ <http://www.doc.ic.ac.uk/~ih/doc/stepper/kp4m4/>

KP4M4-001 Stepper Motor



+12v dc, four-phase, unipolar, permanent magnet, 3.6° per step

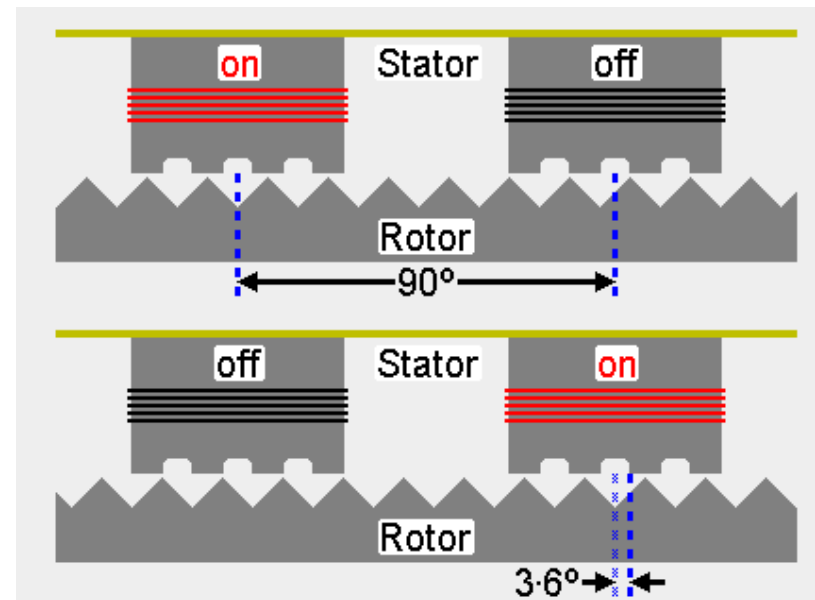
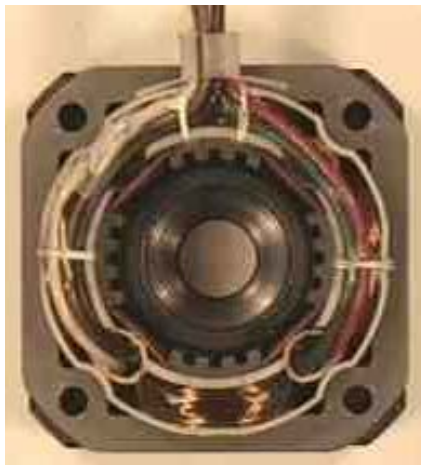
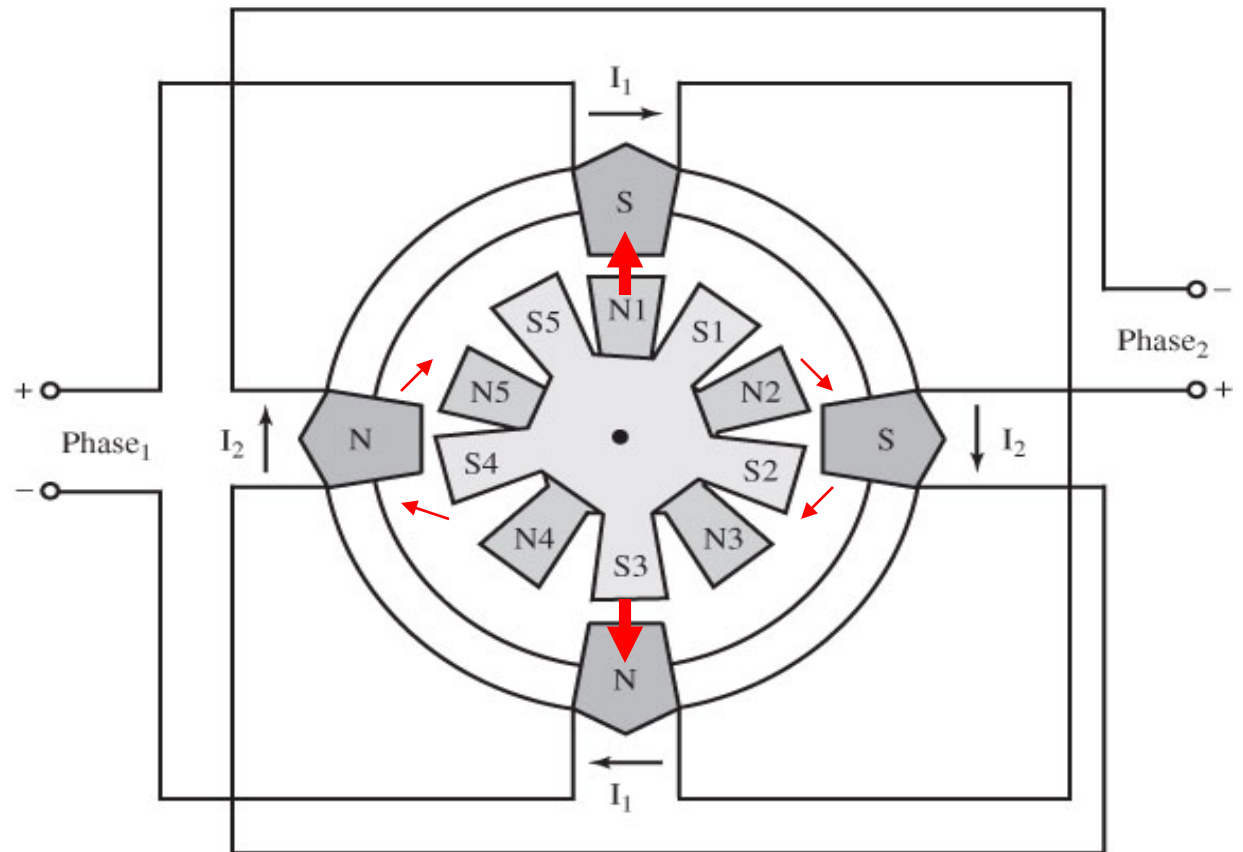


Figure 8.83
Stable state 1.



[Valvano]

Figure 8.84

Unstable state as rotor goes from state 1 to state 2.

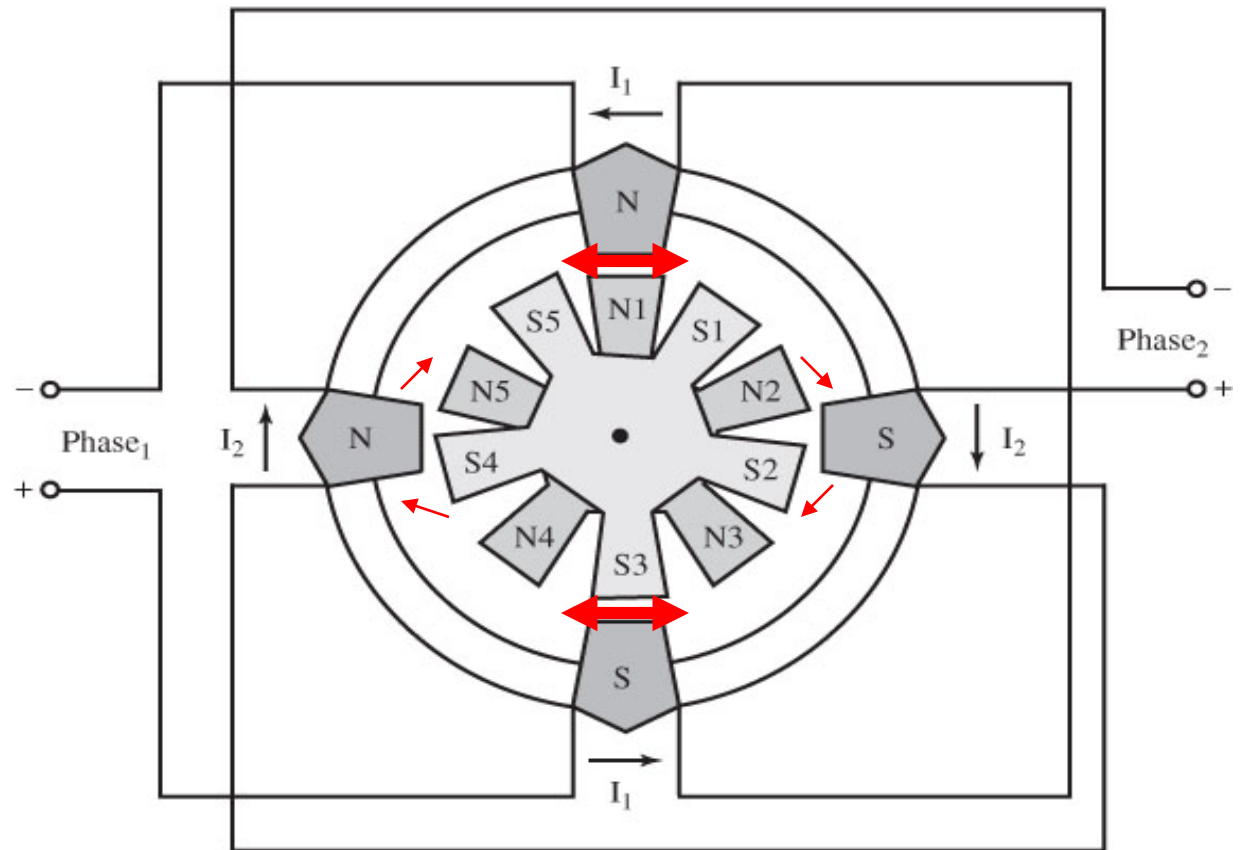
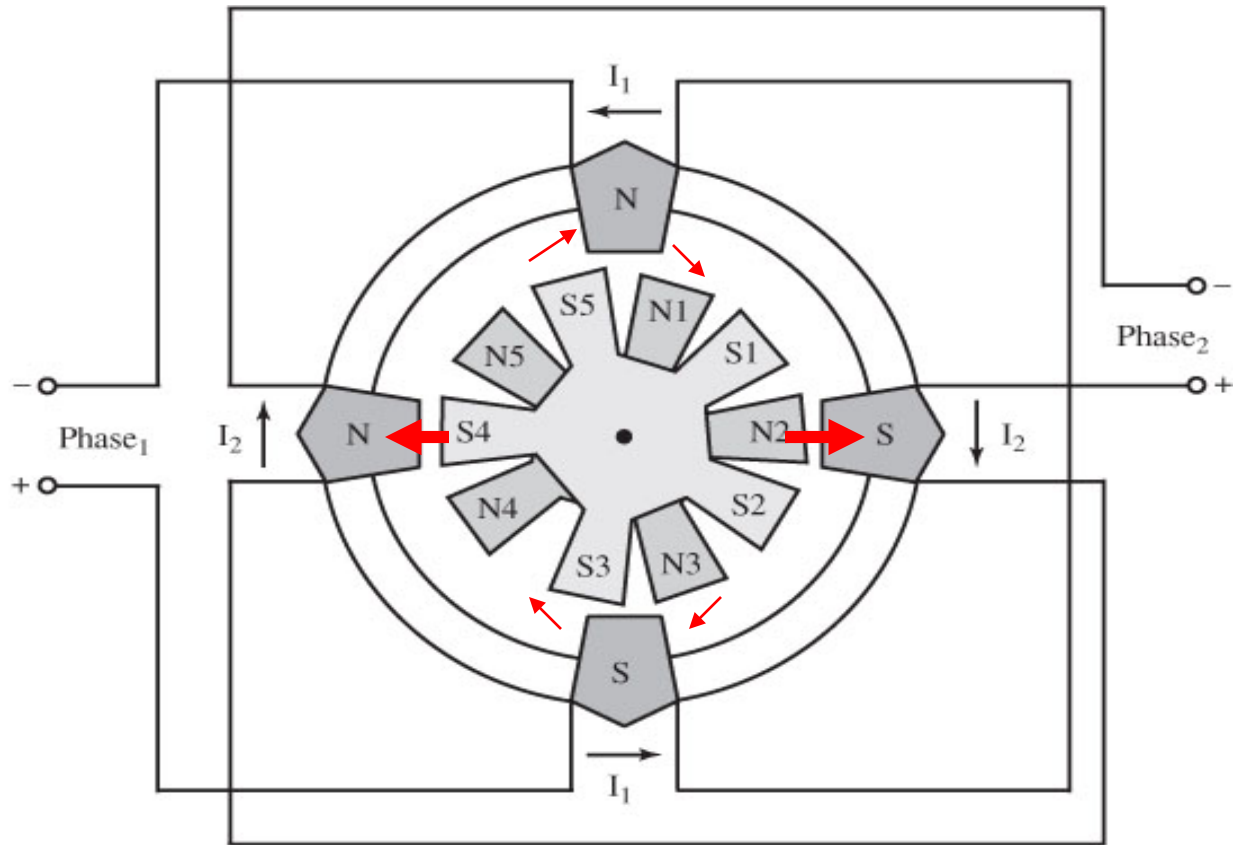
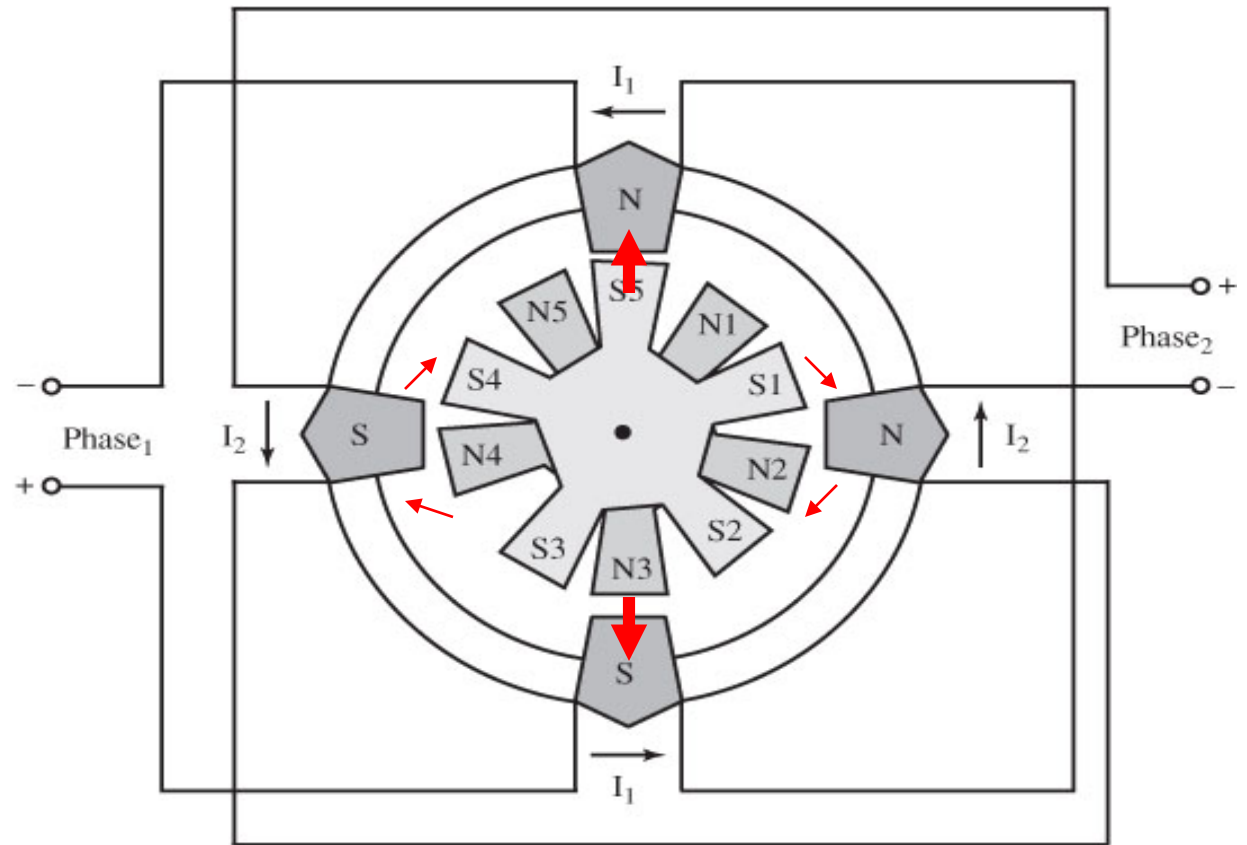


Figure 8.85
Stable state 2.



[Valvano]

Figure 8.86
Stable state 3.



[Valvano]

Stepper Motor Ramp Up & Ramp Down

◆ Stepper motor changes speed as it moves

- Magnetic pole changes have to coordinate with current speed
- Motor spec & math gives you a speed profile

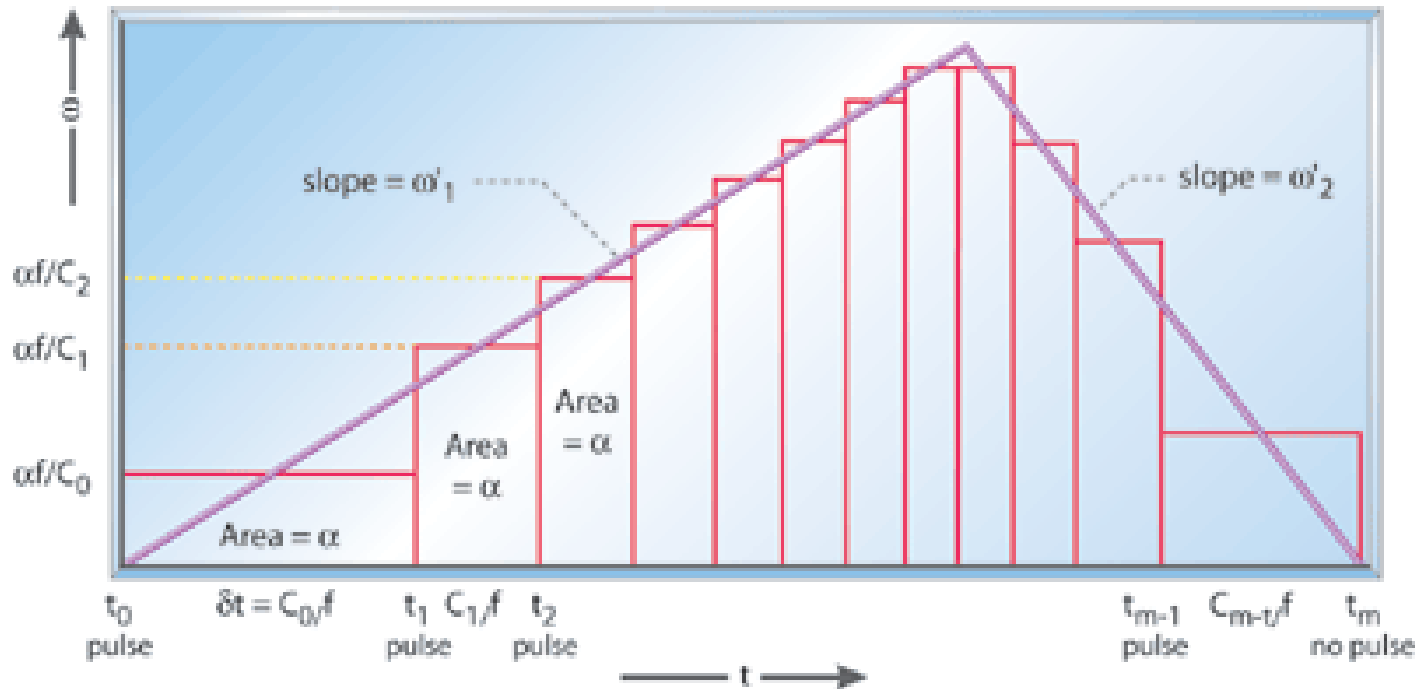


Figure 1: Ramp geometry: move of $m = 12$ steps

[Austin04]

◆ What happens if you don't know where you are?

- Lose power
- Controller resets
- Something jams and you lose steps?

Stepper Motor Drive Circuit

◆ Note: not the same motor type as other Valvano pictures

- A/A' and B/B' are always a high/low pair
- High turns coil on; Low turns coil off
- 1N914 diodes protect against back-EMF overvoltage when turning coil off

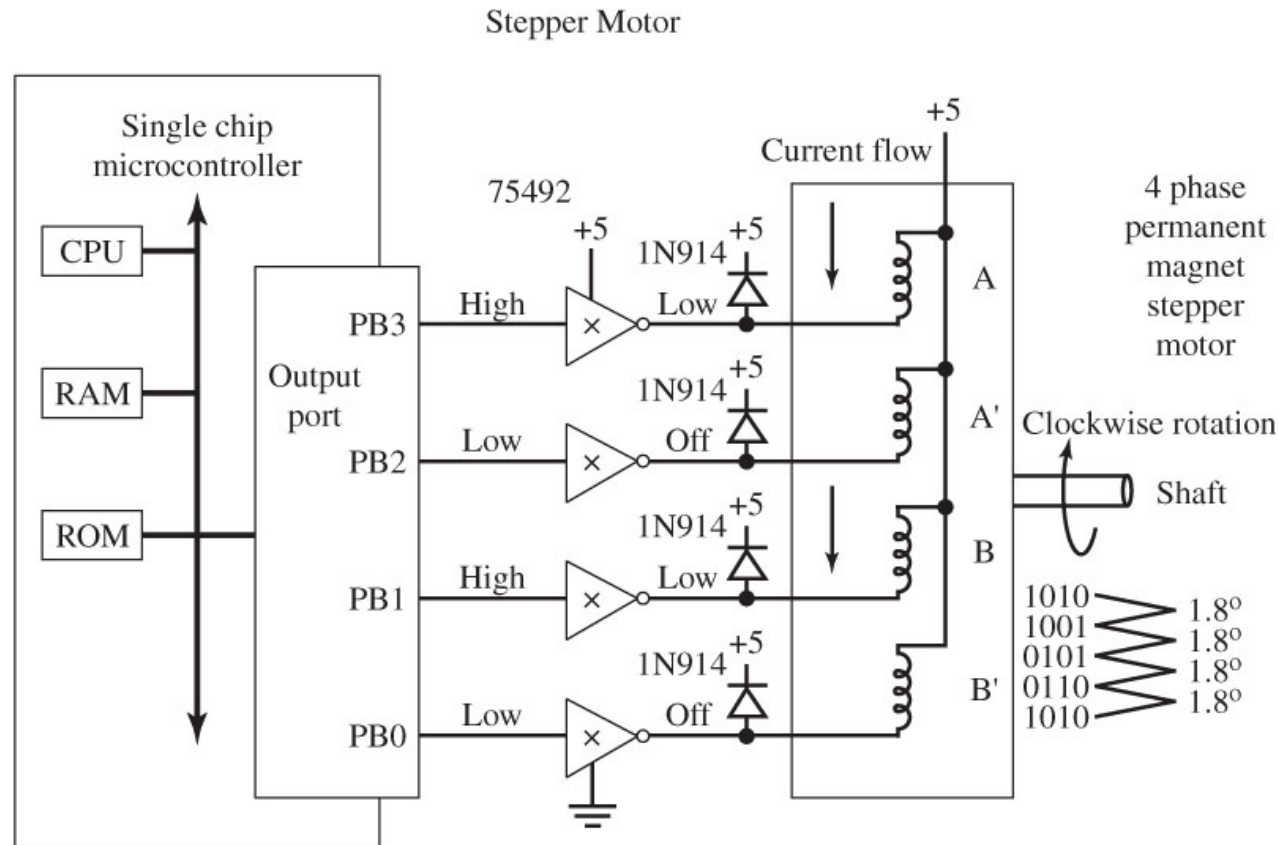


Figure 8.80
Simple stepper interface.

[Valvano]

Stepper Motors Are A Robot Gateway Device

◆ Makerbot – stepper motors to position things

- The vibration from making “steps” makes noise. Can you do something fun with that?



Review

◆ Digital To Analog Conversion

- Example implementation – how DAC actually works
- Performance aspects: especially quantization issues

◆ Encoding waveforms to feed to a DAC

- Low pass filter on outputs

◆ Pulse Modulation

- Pulse Density Modulation vs. Pulse Width Modulation
- How PWM works in general
- For lab, be able to program the PWM hardware
- How a servo works

◆ Stepper motor

- Simplest kind of motor to use; have an idea of what's going on with phases
- And how a solenoid works