

18734: Foundations of Privacy

# Database Privacy: k-anonymity and de-anonymization attacks

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# Publicly Released Large Datasets

- ▶ Useful for improving recommendation systems, collaborative research
- ▶ Contain personal information
- ▶ Mechanisms to protect privacy, e.g. anonymization by removing names

▶ Yet, private information leaked by attacks on anonymization mechanisms



**m o v i e l e n s**  
helping you find the *right* movies



**amazon.com.**



Article [Discussion](#)

**AOL search data leak**

From Wikipedia, the free encyclopedia

# Non-Interactive Linking

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**Background/  
Auxiliary  
Information**

**DB1**

**DB2**



**Algorithm to link information**



**De-identified record**

# Roadmap

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▶ ~~Motivation~~

▶ Privacy definitions



▶ Netflix-IMDb attack

▶ Theoretical analysis

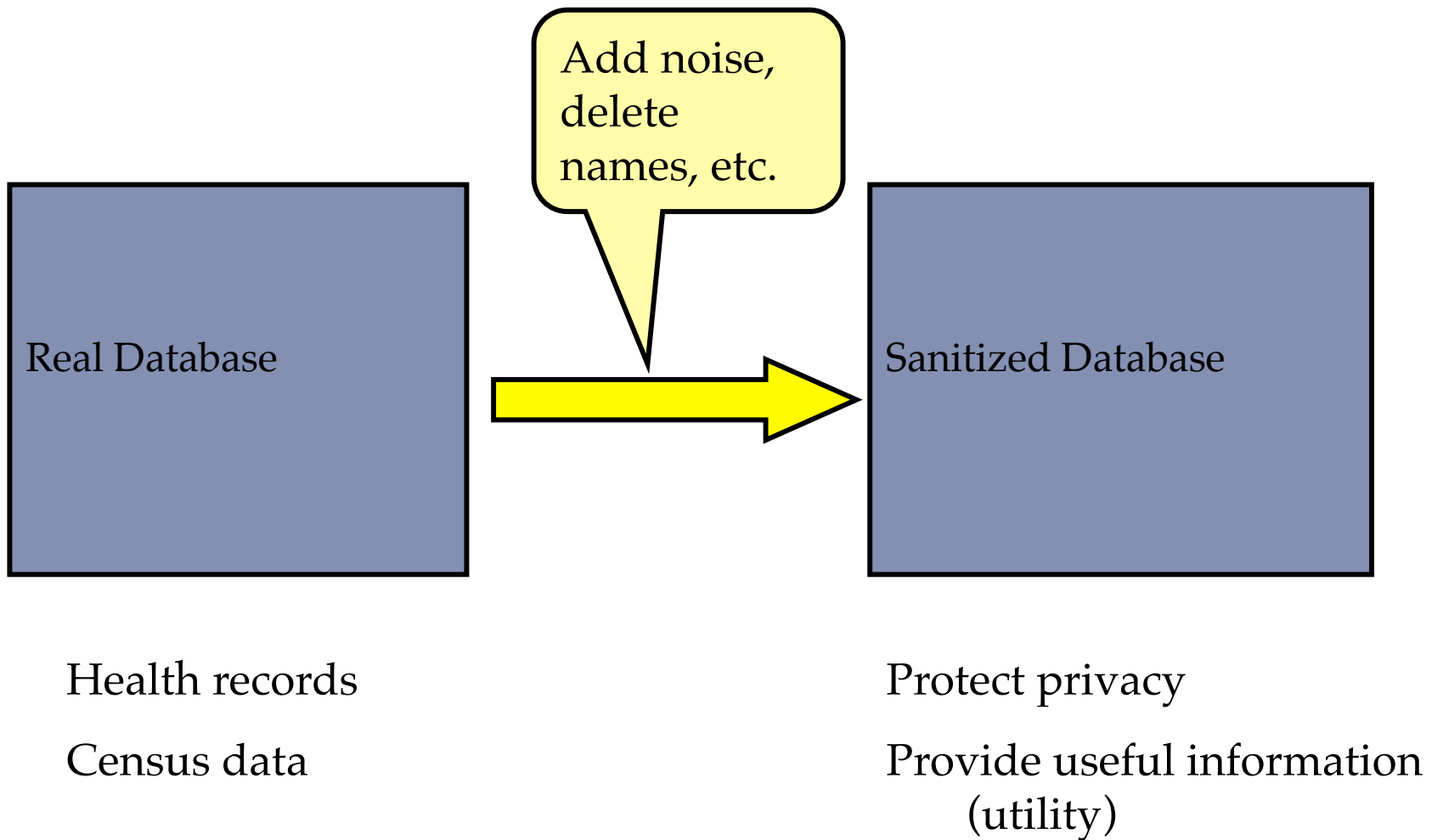
▶ Empirical verification of assumptions

▶ Conclusion

▶ 4

# Sanitization of Databases

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# Database Privacy

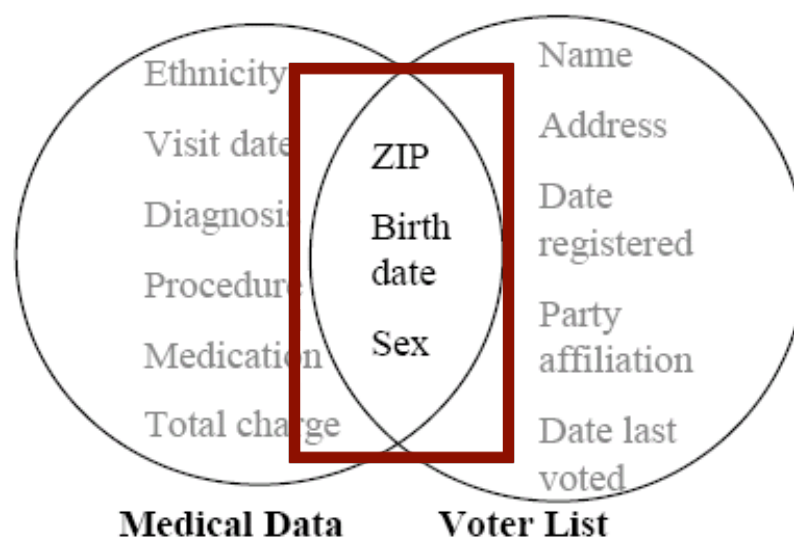
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- ▶ Releasing sanitized databases
  1. k-anonymity [Samarati 2001; Sweeney 2002]
  2. Differential privacy [Dwork et al. 2006] (*future lecture*)

# Re-identification by linking

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Linking two sets of data on shared attributes may uniquely identify some individuals:



*87 % of US population uniquely identifiable by 5-digit ZIP, gender, DOB*

# K-anonymity

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- ▶ Quasi-identifier: Set of attributes that can be linked with external data to uniquely identify individuals
- ▶ Make every record in the table indistinguishable from at least  $k-1$  other records with respect to quasi-identifiers
- ▶ Linking on quasi-identifiers yields at least  $k$  records for each possible value of the quasi-identifier



# K-anonymity and beyond

	Non-Sensitive			Sensitive
	Zip Code	Age	Nationality	Condition
1	13053	28	Russian	Heart Disease
2	13068	29	American	Heart Disease
3	13068	21	Japanese	Viral Infection
4	13053	23	American	Viral Infection
5	14853	50	Indian	Cancer
6	14853	55	Russian	Heart Disease
7	14850	47	American	Viral Infection
8	14850	49	American	Viral Infection
9	13053	31	American	Cancer
10	13053	37	Indian	Cancer
11	13068	36	Japanese	Cancer
12	13068	35	American	Cancer

Figure 1. Inpatient Microdata

	Non-Sensitive			Sensitive
	Zip Code	Age	Nationality	Condition
1	130**	< 30	*	Heart Disease
2	130**	< 30	*	Heart Disease
3	130**	< 30	*	Viral Infection
4	130**	< 30	*	Viral Infection
5	1485*	≥ 40	*	Cancer
6	1485*	≥ 40	*	Heart Disease
7	1485*	≥ 40	*	Viral Infection
8	1485*	≥ 40	*	Viral Infection
9	130**	3*	*	Cancer
10	130**	3*	*	Cancer
11	130**	3*	*	Cancer
12	130**	3*	*	Cancer

Figure 2. 4-anonymous Inpatient Microdata

Provides some protection: linking on ZIP, age, nationality yields 4 records

Limitations: lack of diversity in sensitive attributes, background knowledge, subsequent releases on the same data set

# Re-identification Attacks in Practice

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Examples:

- ▶ Netflix-IMDB
- ▶ Movielens attack
- ▶ Twitter-Flicker
- ▶ Recommendation systems – Amazon, Hunch,..


Goal of De-anonymization: To find information about a record in the released dataset

# Roadmap

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- ▶ ~~Motivation~~
- ▶ ~~Privacy definitions~~
- ▶ Netflix-IMDb attack 
- ▶ Theoretical analysis
- ▶ Empirical verification of assumptions
- ▶ Conclusion

# Anonymization Mechanism


	Gladiator	Titanic	Heidi
 Bob	5	2	1
Alice	3	2.5	2
Charlie	1.5	2	2

Each row corresponds to an individual

Each column corresponds to an attribute, e.g. movie

Delete name identifiers and add noise



	Gladiator	Titanic	Heidi
 r <sub>1</sub>	4	1	0
r <sub>2</sub>	2	1.5	1
r <sub>3</sub>	0.5	1	1

Anonymized Netflix DB

# De-anonymization Attacks Still Possible

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## ▶ Isolation Attacks

- ▶ Recover individual's record from anonymized database
- ▶ E.g., find user's record in anonymized Netflix movie database

## ▶ Information Amplification Attacks

- ▶ Find more information about individual in anonymized database
- ▶ E.g. find ratings for specific movie for user in Netflix database

# Netflix-IMDb Empirical Attack [Narayanan et al 2008]

Anonymized Netflix DB

	Gladiator	Titanic	Heidi
$r_1$	4	1	0
$r_2$	2	1.5	1
$r_3$	0.5	1	1

Publicly available IMDb ratings  
(noisy)

	Titanic	Heidi
 Bob	2	1

Used as auxiliary information



**Weighted Scoring Algorithm**



Isolation Attack!

	$r_1$	4	1	0
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# Problem Statement

Anonymized database

	Gladiator	Titanic	Heidi
$r_1$	4	1	0
$r_2$	2	1.5	1
$r_3$	0.5	1	1

Auxiliary information about a record (noisy)

	Titanic	Heidi
 Bob	2	1

Attacker uses algorithm to find record

**Attacker's goal:** Find  $r_1$  or record similar to Bob's record

Enhance theoretical understanding of why empirical de-anonymization attacks work

# Research Goal


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Characterize classes of auxiliary information and properties of database for which re-identification is possible



# Roadmap

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- ▶ ~~Motivation~~
- ▶ ~~Privacy definitions~~
- ▶ ~~Netflix-IMDb attack~~
- ▶ Theoretical analysis 
- ▶ Empirical verification of assumptions
- ▶ Conclusion

# Netflix-IMDb Empirical Attack [Narayanan et al 2008]

Anonymized Netflix DB

	Gladiator	Titanic	Heidi
$r_1$	4	1	0
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Publicly available IMDb ratings  
(noisy)

		Titanic	Heidi
	Bob	2	1

Used as auxiliary information



Weighted Scoring Algorithm

How do you measure similarity of this record with Bob's record?  
(Similarity Metric)

What does **auxiliary information** about a record mean?



	$r_1$	4	1	0
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# Definition: Asymmetric Similarity Metric

	Gladiator	Titanic	Heidi
	$v_1$	$v_2$	$v_3$
y	5	0	-
r	0	2	3

Individual Attribute Similarity

$$T(y(i), r(i)) = 1 - \frac{|y(i) - r(i)|}{p(i)}$$

$$T(y(v_1), r(v_1)) = 1 - \frac{|5 - 0|}{5} = 0$$

Intuition: Measures how closely two people's ratings match on one movie

Movie (i)	$T(y(i), r(i))$
Gladiator	0
Titanic	0.6
Heidi	0

$p(i)$ : range of attribute  $i$

Intuition: Measures how closely two people's ratings match overall

$S(y,r)$	$0.6 / 2 = 3$
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Similarity Metric

$$S(y,r) = \sum_{i \in \text{supp}(y)} \frac{T(y(i), r(i))}{|\text{supp}(y)|}$$

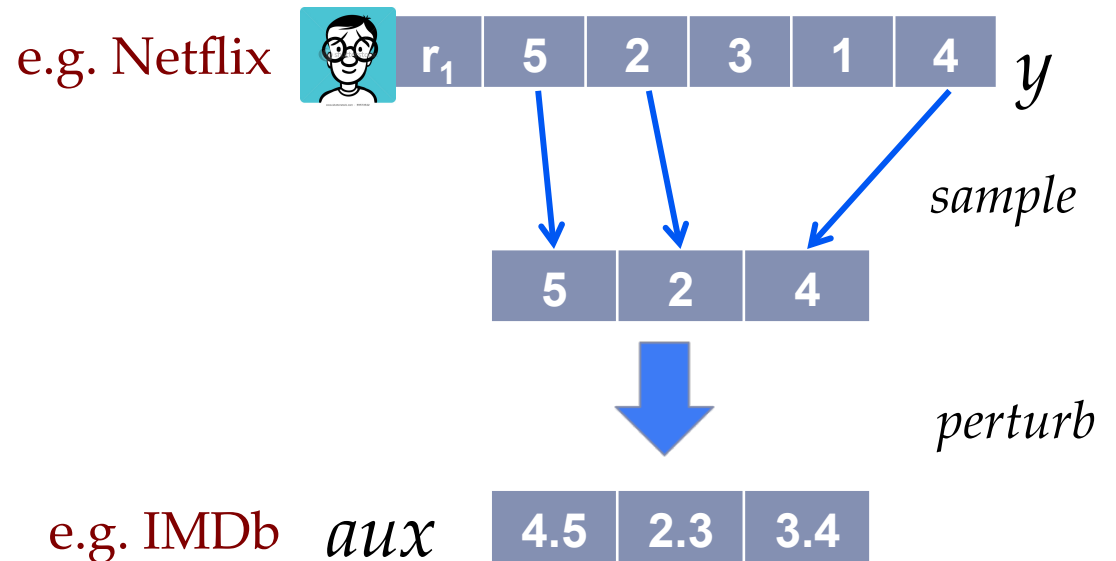
$\text{supp}(y)$ : non null attributes in  $y$

# Definition: Auxiliary Information

Intuition:

*aux* about *y* should be a subset of record *y*  
*aux* can be noisy

*aux* captures information available outside normal data release process



Bound level of perturbation in *aux*

$$\gamma \in [0,1]$$

( $m, \gamma$ )-perturbed auxiliary information

$$\forall i \in \text{supp}(aux). T(y(i), aux(i)) \geq 1 - \gamma$$

$|\text{supp}(aux)| = m = \text{no. of non null attributes in } aux$



# Weighted Scoring [Narayanan et al 2008, Frankowski et al 2006]

Intuition: The fewer the number of people who watched a movie, the rarer it is

## Weight of an attribute $i$

$$w(i) = \frac{1}{\log(|\text{supp}(i)|)}$$

$|\text{supp}(i)|$  = no. of non null entries in column  $i$

Use weight as an indicator of rarity

Score gives a weighted average of how closely two people match on every movie, giving higher weight to rare movies

## Scoring Methodology

$$\text{Score}(aux, r_j) = \sum_{i \in \text{supp}(aux)} \frac{w(i) * T(aux(i), r_j(i))}{|\text{supp}(aux)|}$$

$|\text{supp}(aux)|$  =  $m$  = no. of non null attributes in  $aux$

Compute *Score* for every record  $r$  in anonymized DB to find out which one is closest to target record  $y$

# Weighted Scoring Algorithm [Narayanan et al 2008]

Compute *Score* for every  $r$  in  $D$

$$Score(aux, r_j) = \sum_{i \in \text{supp}(aux)} \frac{w(i) * T(aux(i), r_j(i))}{|\text{supp}(aux)|}$$

$w_i$	0.63	0.5	0.63
	$v_1$	$v_2$	$v_3$
$r_1$	5	2	-
$r_2$	3	1	4
$r_3$	-	2	4

Score(aux, $r_j$ )
0.52
0.40
0.23

$v_1$	$v_2$
4.5	2.3

*aux*

One of the records  $r$  in anonymized database is  $y$ , which row is it?

*Eccentricity measure* > threshold

$$e(aux, D) = \max_{r \in D} (Score(aux, r)) - \max_{2, r \in D} (Score(aux, r))$$

Output record with max Score

$r_1$	5	2	-
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*Score(aux, r)* used to predict  $S(y, r)$

# Where do Theorems Fit?

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4.5	2.3
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**Computed:**  
Score of all records  $r$  in  $D$  with  $aux$



4.5	2.3
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**Desired:**  
Guarantee about *Similarity*

→  
Theorems help bridge the gap


$r_1$	5	2	-
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$r_1$	5	2	-
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# Theorems

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- ▶ Theorem 1: When Isolation Attacks work? 
- ▶ Theorem 2: Why Information Amplification Attacks work?



# Theorem 1: When Isolation Attacks work?

Intuition: If eccentricity is high, algorithm always finds the record corresponding to auxiliary information!

If

$aux$  is  $(m, \gamma)$ -perturbed

Eccentricity threshold  $> \gamma M$

Eccentricity: Highest score - Second highest score

$\gamma$ : Indicator of perturbation in  $aux$

$M$ : Average of weights in  $aux$

$\check{O}$ : Record output by algorithm

$y$ : Target record

then

$$Score(aux, \check{O}) = Score(aux, y)$$

If  $\check{O}$  is the only record with the highest score then  $\check{O} = y$

# Isolation Attack: Theorem

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**Theorem IV.1** *Let  $y$  denote the target record from a given database  $D$ . Let  $aux_y$  denote  $(m, \gamma)$ -perturbed auxiliary information about record  $y$ . If the eccentricity measure  $e(aux_y, D) > \gamma M$  where  $M = \frac{\sum_{i \in \text{supp}(aux_y)} w_i}{|\text{supp}(aux_y)|}$  is the scaled sum of weights of attributes in  $aux_y$ , then*

- 1)  $\max_{r \in D} (\text{Score}(aux_y, r)) = \text{Score}(aux_y, y)$ .
- 2) Additionally, if only one record has maximum score value  $= \text{Score}(aux_y, y)$ , then the record  $o$  returned by the algorithm is the same as target record  $y$ .

# Theorems

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- ▶ ~~Theorem 1: When Isolation Attacks work?~~
- ▶ Theorem 2: Why Information Amplification Attacks work?



# Intuition: Why Information Amplification Attacks work?

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- ▶ If two records agree on rare attributes, then with high probability they agree on other attributes too
- ▶ Use intuition to find record  $r$  similar to  $aux$  on many rare attributes (using  $aux$  as 'proxy' for  $y$ )

# Intuition: Why Information Amplification Attacks work?

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For > 90%  
of records

> 0.75

- ▶ If a high **fraction** of attributes in *aux* are **rare**, then any record *r* that is **similar to *aux***, is **similar to *y***

Similarity  
> 0.75

Similarity  
> 0.65

# Theorem 2: Why Information Amplification Attacks work?

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Define Function

$$f_D(\eta_1, \eta_2, \eta_3)$$

If a high **fraction** of attributes in *aux* are **rare**, then any record *r* **similar to *aux***, is **similar to *y***

- Measure overall similarity between target record *y* and *r* that depends on:

$\eta_1$  : Fraction of rare attributes in *aux*

$\eta_2$  : Lower bound on similarity between *r* and *aux*

$\eta_3$  : Fraction of target records for which guarantee holds

$$S(y, r) \geq f_D(\eta_1, \eta_2, \eta_3)$$

# Theorem 2: Why Information Amplification Attacks work?

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Using Function

$$f_D(\eta_1, \eta_2, \eta_3)$$

$$S(y, r) \geq f_D(\eta_1, \eta_2, \eta_3)$$

Theorem gives guarantee about similarity of record output by algorithm with target record

# Roadmap

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- ▶ ~~Motivation~~
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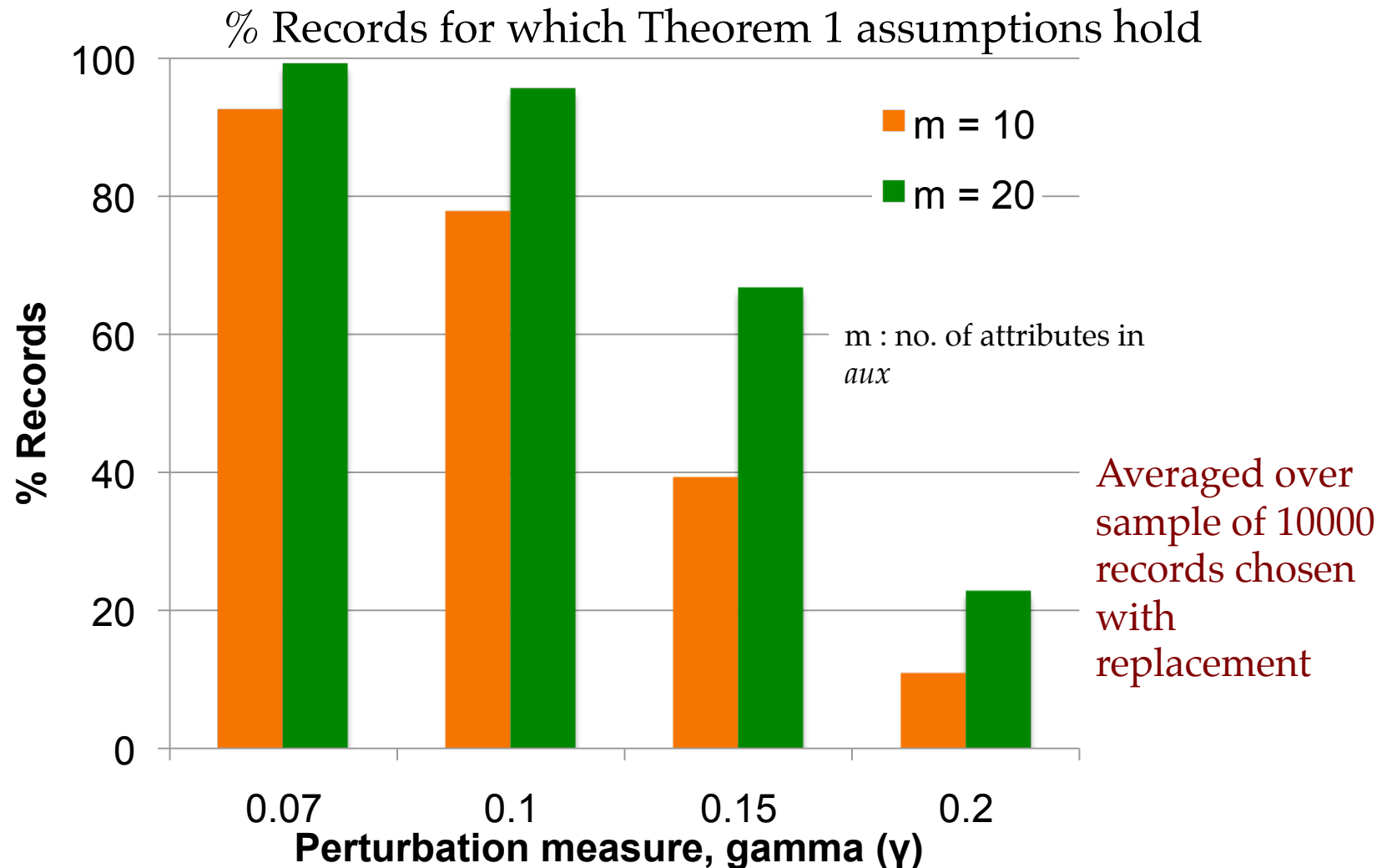


# Empirical verification

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- ▶ Use `anonymized' Netflix database with 480,189 users and 17,770 movies
- ▶ Percentage values claimed in our results = percentage of records not filtered out because of
  - ▶ insufficient attributes required to form aux OR
  - ▶ insufficient rare or non-rare attributes required to form aux

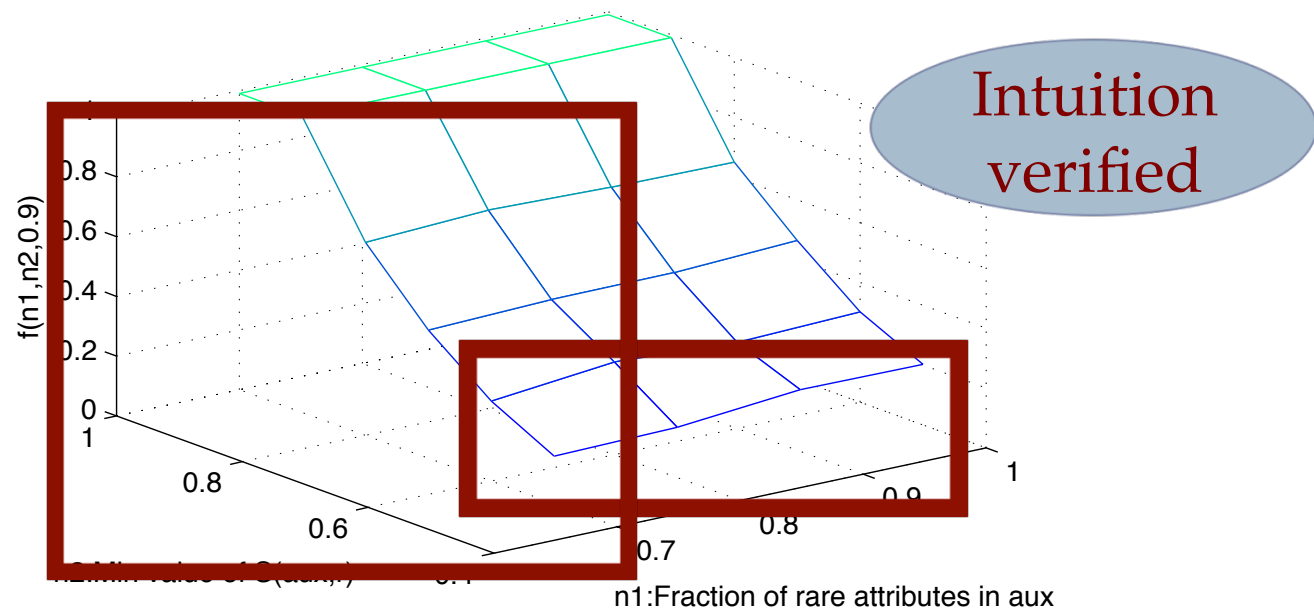
# Do Assumptions hold over Netflix Database?



# Does Intuition about $f_D$ hold for Netflix Database?

$f_D(\eta_1, \eta_2, \eta_3)$  can be evaluated given D

$$S(y, r) \geq f_D(\eta_1, \eta_2, \eta_3)$$



For Netflix DB,

$f_D(\eta_1, \eta_2, \eta_3)$  is monotonically increasing in  $\eta_1$  and  $\eta_2$  and tends to 1 as  $\eta_2$  increases

# Roadmap

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- ▶ Motivation
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# Conclusion

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- ▶ Naïve anonymization mechanisms do not work
- ▶ We obtain **provable** bounds about, and **verify empirically**, why some de-anonymization attacks work in practice
- ▶ Even perturbed auxiliary information can be used to launch de-anonymization attacks if:
  - ▶ *Database* has many **rare dimensions** and
  - ▶ *Auxiliary information* has information about these rare dimensions

# Acknowledgment

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- ▶ Slides 5-9 are from CMU 18-739 (Fall 2009) taught by Anupam Datta, with minor edits

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▶ Questions?