

# Chapters 5 & 7 Impact of different dispatch methods on Azores Islands

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# Key Purpose

- To study the impact of different sized wind parks and different dispatch methods in Flores and St Miguel power systems

# Key Findings

- Advanced Dispatch Methods, e.g., look-ahead model predictive control (MPC)-based dispatch, reduces overall generation cost by 1.5% as compared with static dispatch, in the Flores island.
- As variable resources get more and more, potential saving of advanced dispatch methods will be more significant.
- Distributed implementation of advanced look-ahead dispatch gets very close to solutions as compared with centralized look-ahead dispatch.

# Mathematical Formulation

- Notations

$G$  : set of all available generators;

$G_w$  : set of wind energy generators;

$\hat{L}(k)$  : expected demand at time step  $k$ ;

$C_i(P_{G_i})$  : cost function of generator  $i$ ;

$P_{G_i}^{\min}, P_{G_i}^{\max}$  : minimum and maximum generation output ;

- Centralized Static Economic Dispatch with Inelastic Demand

$$\min_{P_G} \sum_{i \in G \setminus G_w} (C_i(P_{G_i}(k))),$$

Minimize the total generation cost

$$s.t. \sum_{i \in G \setminus G_w} P_{G_i}(k) = \hat{L}(k) - \hat{P}_{G_w}(k);$$

Energy balancing equation

$$P_{G_i}^{\min} \leq P_{G_i}(k) \leq P_{G_i}^{\max}, i \in G \setminus G_w;$$

Capacity constraints for generators

Note: in static dispatch, wind resources are treated as *negative load*

# Mathematical Formulation (cont'd)

- Notations (complimentary)

$\hat{P}_{G_w}^{min}, \hat{P}_{G_w}^{max}$  : expected minimum and maximum wind generation output at time step  $k$ ;

$R_i$  : ramping rate of generator  $i, i \in G$ ;

$K$  : time steps in a look-ahead optimization period;

- Centralized Look-ahead Economic Dispatch with Inelastic Demand

$$\min_{P_G} \sum_{k=1}^K \sum_{i \in G} (C_i(P_{G_i}(k))), i \in G$$

$$s.t. \sum_i P_{G_i}(k) = \hat{L}(k), i \in G;$$

$$\hat{P}_{G_w}^{max}(k) = g_j(\hat{P}_{G_w}^{max}(k-1));$$

$$\hat{P}_{G_w}^{min}(k) \leq P_{G_w}(k) \leq \hat{P}_{G_w}^{max}(k);$$

$$P_{G_i}^{min}(k) \leq P_{G_i}(k) \leq P_{G_i}^{max}(k), i \in G \setminus G_w;$$

$$|P_{G_i}(k+1) - P_{G_i}(k)| \leq R_i, i \in G$$

Minimize the overall generation cost for the look-ahead period

Energy balancing equation

Wind generation forecast

Wind resources availability constraints

Capacity constraints for conventional units

Ramping constraints for generators

# Mathematical Formulation (cont'd)

- Notations (complimentary)

$S_i(P_{G_i}(k))$  : supply bid function of unit  $i$

$\lambda(k)$  : price of electricity at time step  $k$ ;

- Distributed Look-ahead Economic Dispatch with Inelastic Demand

$$\max_{P_{G_i}(k)} \sum_{k+1}^{k+K} \hat{\lambda}(k) (P_{G_i}(k)) - (C_i(P_{G_i}(k)))$$

Maximize profits of the market participant

s.t.  $\hat{P}_{G_i}^{max}(k) = g_i(\hat{P}_{G_i}^{max}(k-1));$  Estimate the upper bound of the output

$\hat{P}_{G_i}^{min}(k) = h_i(\hat{P}_{G_i}^{min}(k-1));$  Estimate the lower bound of the output

$|P_{G_i}(k+1) - P_{G_i}(k)| \leq R_i;$  and, Ramping constraint of the unit  $i$

$\hat{P}_{G_i}^{min} \leq P_{G_i}(k) \leq \hat{P}_{G_i}^{max}$  Capacity constraint of the unit  $i$

Expected prices  $\hat{\lambda}(k)$  are updated at every step, by perturbation the price signals, supply bid functions  $S_i(P_{G_i}(k))$  could be generated.

# Solution approach

- Dynamic Programming was utilized to accommodate inter-temporal dynamics
- Specificities
  - Flores has a small power system with significant contribution of hydro resources
  - The lack of water is compensated through an increase of diesel production

# Flores Island





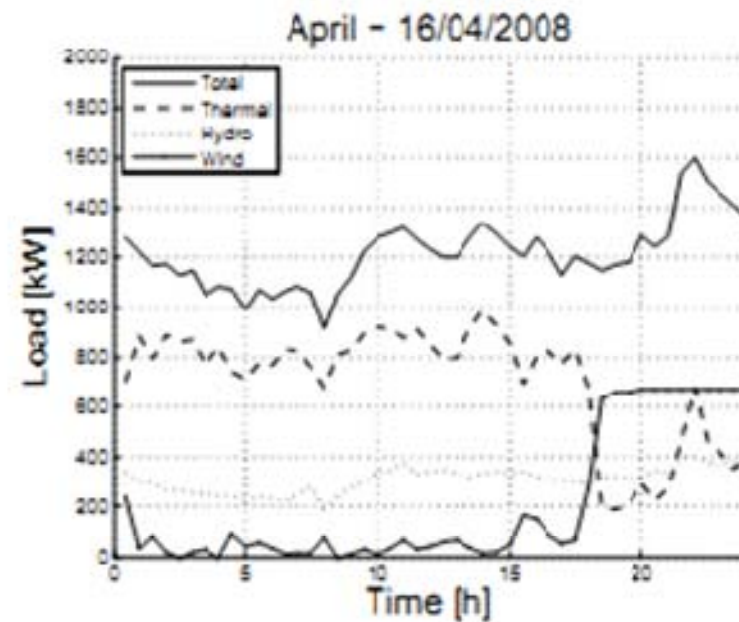
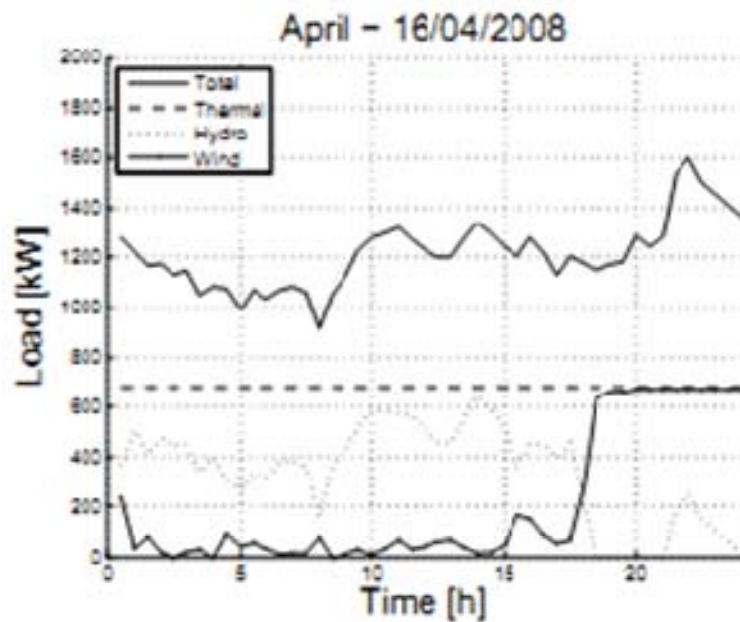
# System Circumstances

Gen	Type	Capacity (MW)	Lowest Output (MW)	Marginal Cost (\$/MWh)	Ramping Rate (%/min)
1	Diesel	2.5	0	261	100.0%
2	Hydro	1.5	0.15	87	5.1%
3	Wind	0.66	0	88	67.0%

- Diesel is the most expensive but is the fastest unit.
- Hydro in this island is a slow but inexpensive unit
  - Two scenarios studies: with and w/o reservoirs
- Wind is dispatchable and could be curtailed when it is required.

# Illustration of static ED

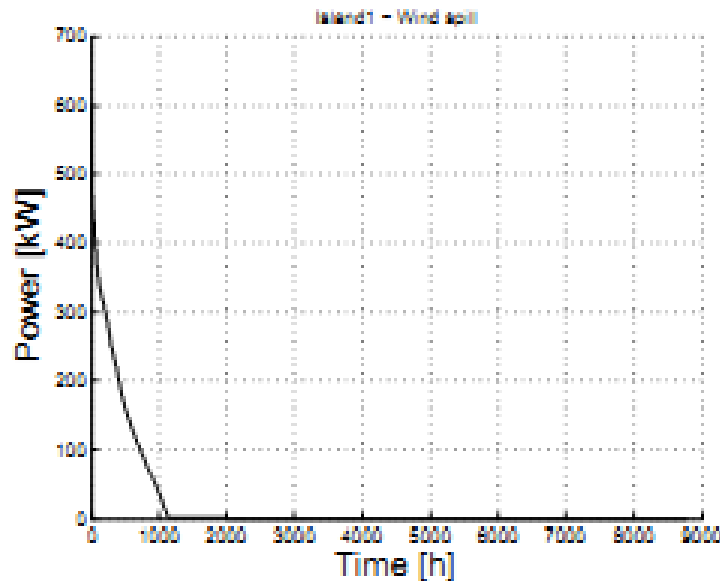
Impact of reservoir size



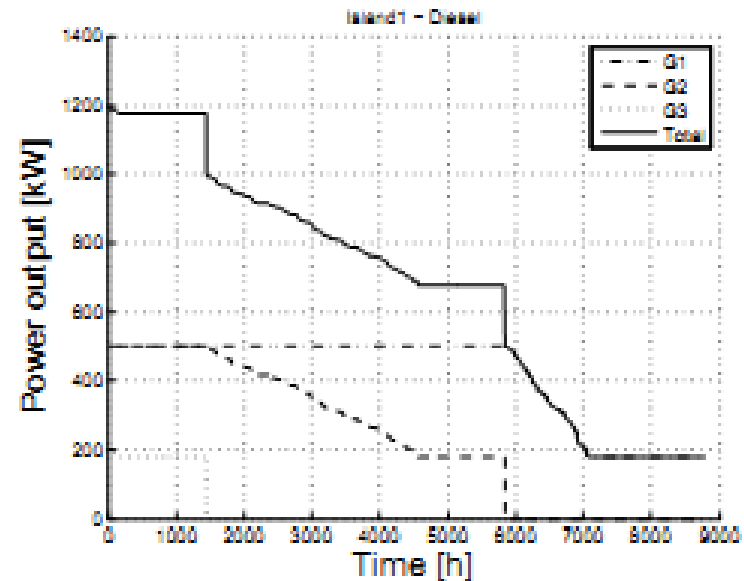
a) hydro generation with reservoir and b) hydro generation without reservoir. It is assumed that there are 2 wind turbines on the system.

# Illustration of static ED

## Impact of wind turbines size



(a)



(b)

a) Total wind spill for 4 turbines; energy spilled is about 6%.

b) Duration curve associated to diesel production. As expected, total diesel power never goes to zero.

# Summary of Impacts of Wind Turbines

No. Wind Turb.	Total Energy Produced [MWh]		Cost [USD]	
	Reservoir	No Reservoir	Reservoir	No Reservoir
1	8,063	9,884	2,104,300	2,579,600
2	7,238	8,991	1,889,200	2,346,500
3	6,458	8,235	1,685,400	2,149,300
4	5,955	7,708	1,554,300	2,011,900
5	5,585	7,331	1,457,600	1,913,400
6	5,293	7,025	1,381,600	1,833,600
7	5,039	6,769	1,315,400	1,766,600

For Flores, with and without reservoir

# Total Operating Cost

	Version 1 Static Scheduling	Version 2 Centralized Look-ahead	Version 3 Distributed look-ahead	Savings (%)
Jan.16th	\$ 4,017.11	\$ 3,953.94	\$ 3,970.28	1.598%
Apr.16th	\$ 4,676.08	\$ 4,604.45	\$ 4,633.94	1.556%
July.16th	\$ 8,287.53	\$ 8,257.15	\$ 8,290.98	0.368%
Oct.15th	\$ 8,890.01	\$ 8,890.01	\$ 8,890.01	0.000%

Note:

**Version 1**  
the static  
scheduling case

**Version 2**  
the centralized  
look-ahead  
scheduling case

**Version 3**  
the distributed  
look-ahead  
scheduling case  
(Version 1 price)

- Look-ahead economic dispatch could reduce the total operating cost compared with static dispatch by about 1.5%, given high wind penetration.
- The centralized look-ahead dispatch gives the best economic performance.
- Given the small duality gap between the distributed approach and the centralized approach (0.3% of total cost), the look-ahead dispatch could be implemented in *a distributed way without too much performance degradation*.

# Scheduling Results on Jan.16th

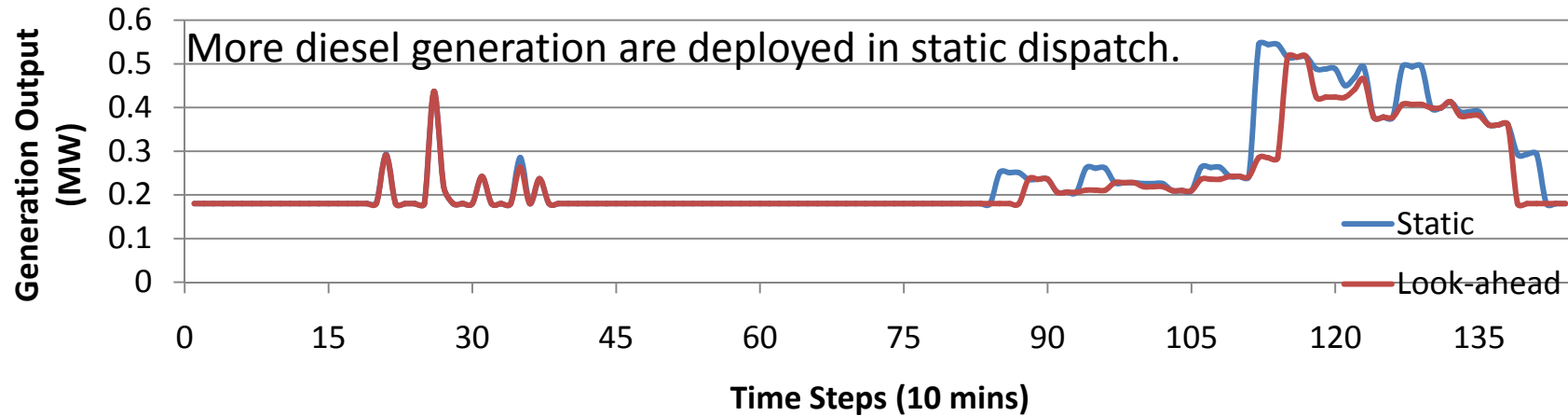


Fig. 1.a Generation outputs of Diesel Units on Jan.16<sup>th</sup>

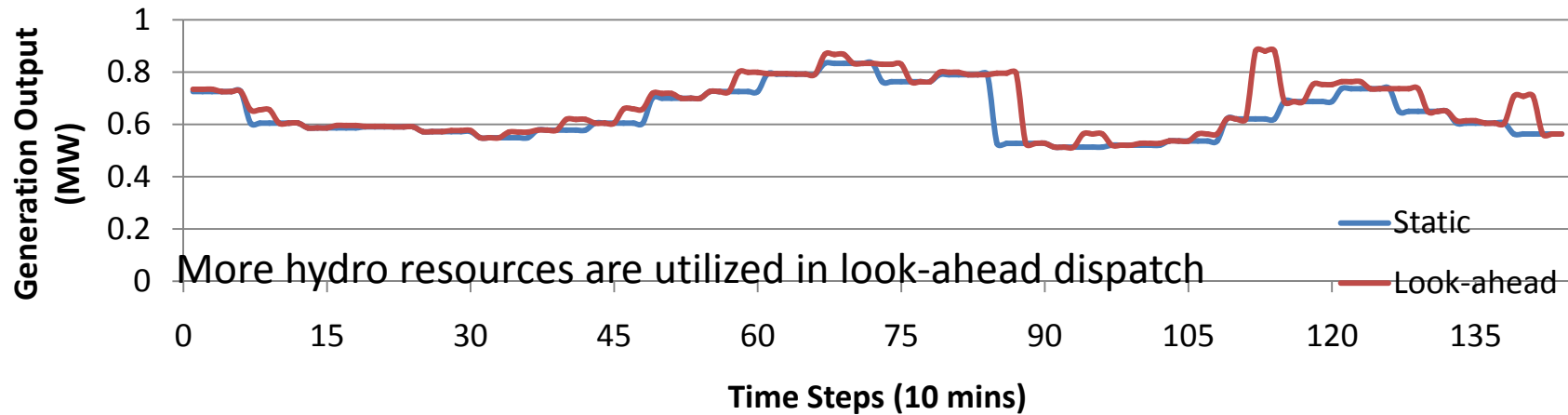


Fig. 1.b Generation outputs of Hydro Units on Jan.16<sup>th</sup>

# Scheduling Results on Apr. 16th

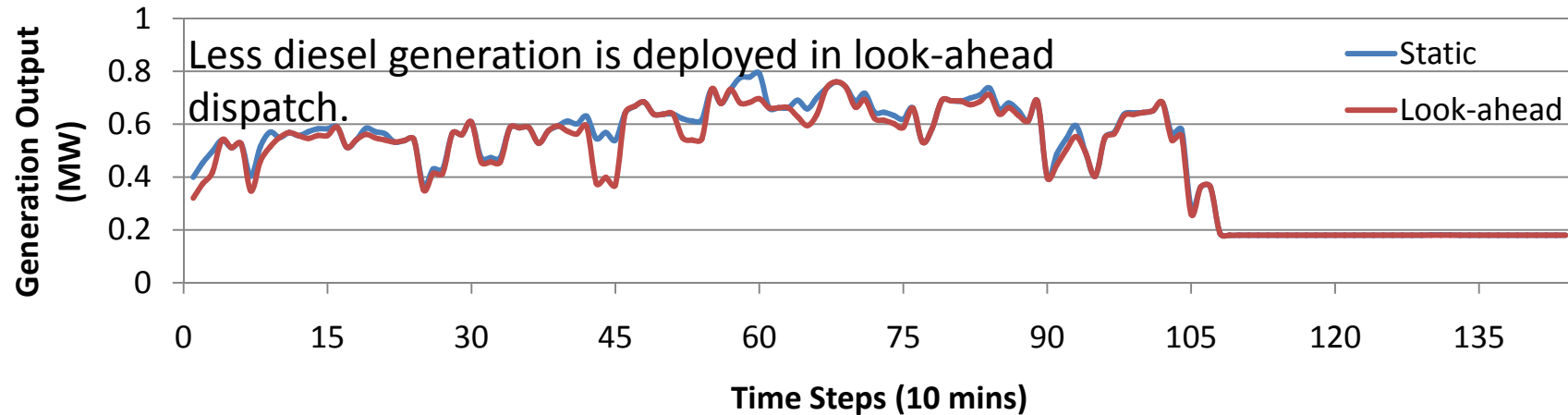


Fig. 2.a Generation outputs of Diesel Units on Apr.16<sup>th</sup>

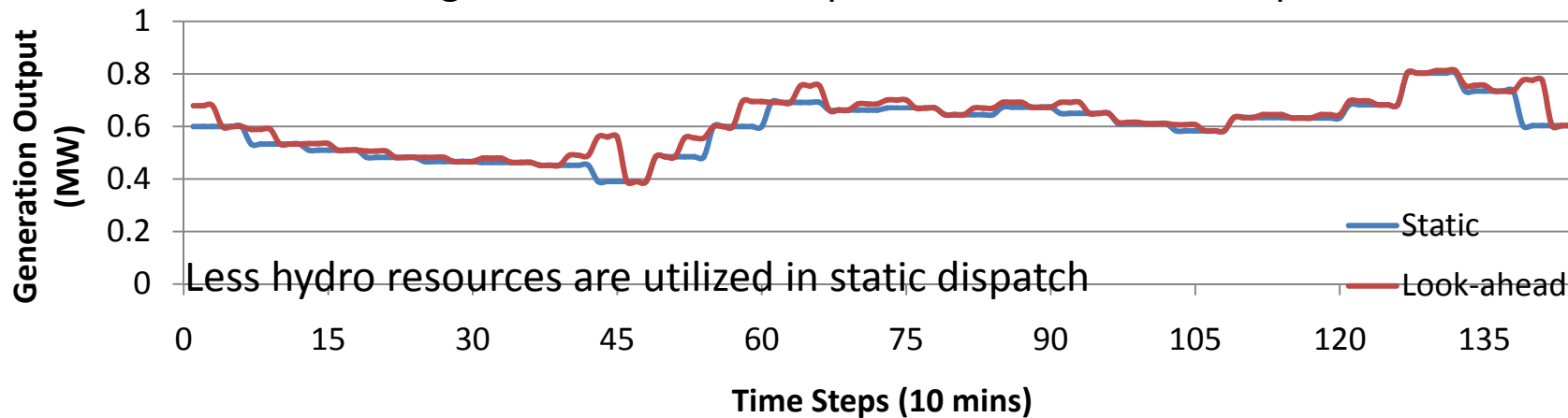
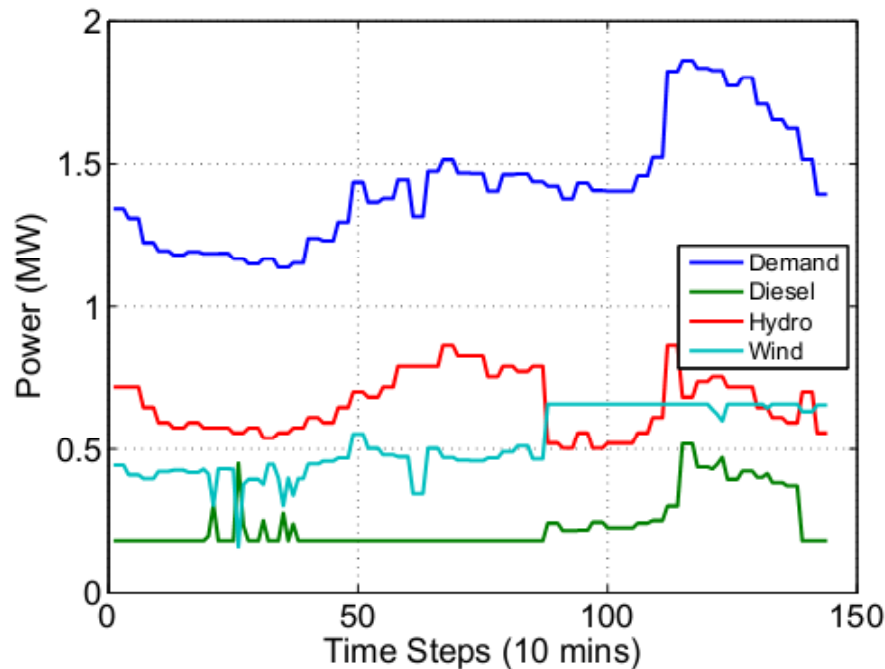
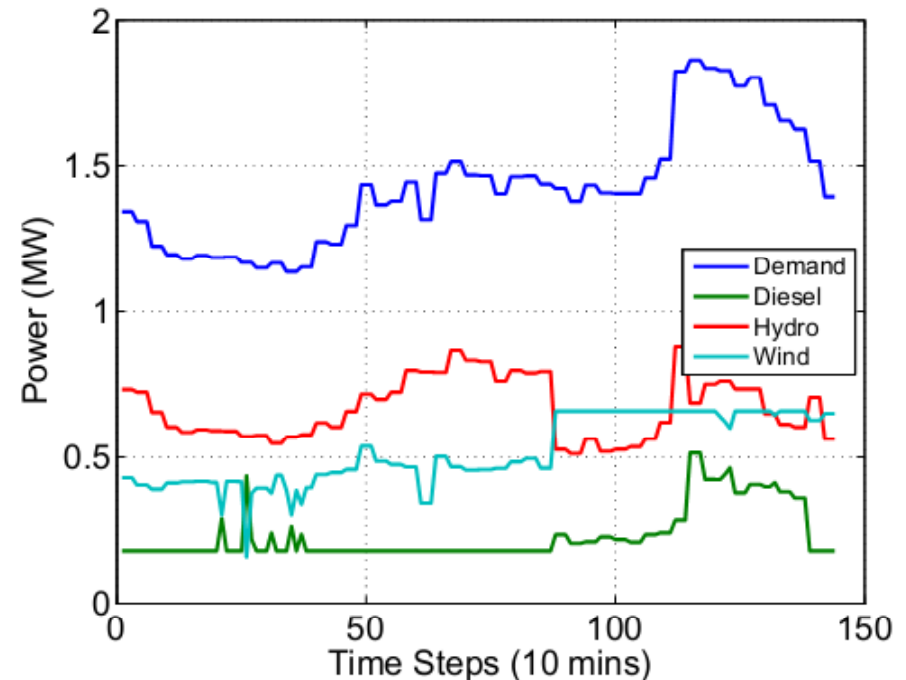


Fig. 2.b Generation outputs of Hydro Units on Apr.16<sup>th</sup>

# Scheduling Results for Distributed Look-ahead Dispatch



Centralized look-ahead dispatch



Distributed look-ahead dispatch

Fig. 3 Generation outputs: Centralized v.s Distributed Look-ahead Dispatch on Jan 16

The distributed approach gives a similar dispatch results to the centralized approach without too much performance degradation.



# St. Miguel Island



# System Circumstances

Gen	Type	Capacity (MW)	Lowest Output (MW)	Marginal Cost (\$/MWh)	Ramping Rate (%/min)
1	Oil	102.66	8.41	185	100.0%
2	Hydro	5.03	0	87	5.1%
3	Wind	30	0	88	67.0%
4	Geothermal	27.8	0	28.1	50%

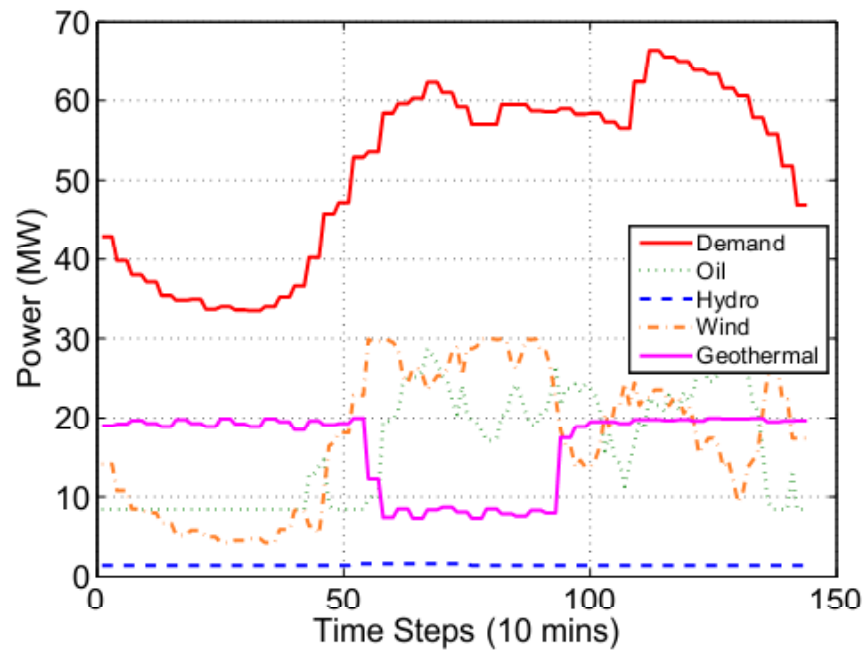
- Oil is the most expensive but is the fastest unit.
- Hydro in this island is run-of-river (slow, nondispatchable)
- Geothermal units are also undispachable

# Total Operating Cost

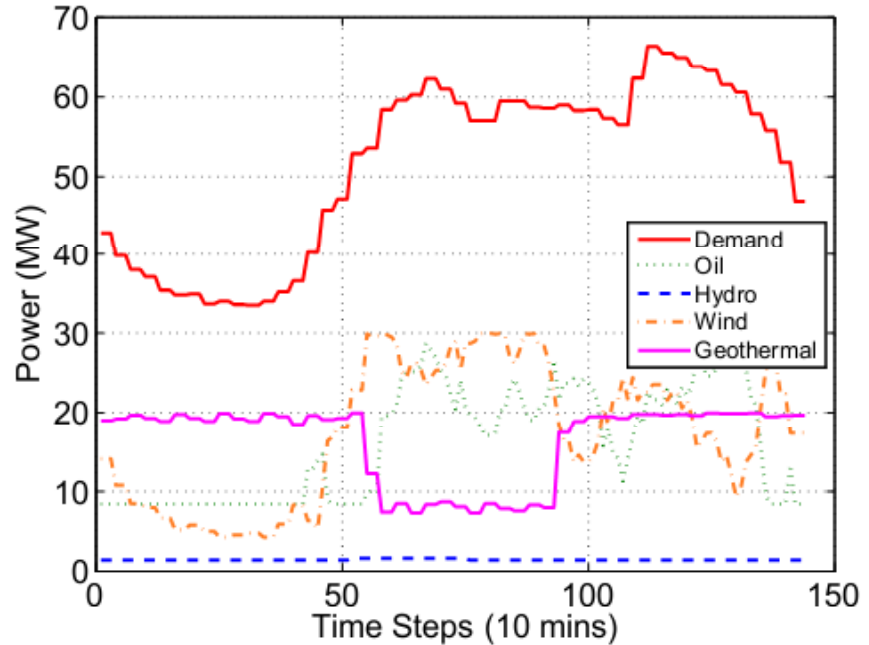
	Version 1	Version 2	Version 3	Savings (%)	Note:
Jan.16th	\$ 122,149.27	\$ 122,149.27	\$ 122,149.27	0.00%	<b>Version 1</b> the static scheduling case
Apr.16th	\$ 99,451.98	\$ 99,451.98	\$ 99,451.98	0.00%	<b>Version 2</b> the centralized look-ahead scheduling case
July.16th	\$ 114,124.32	\$ 114,124.32	\$ 114,124.32	0.00%	<b>Version 3</b> the distributed look-ahead scheduling case
Oct.15th	\$ 168,017.17	\$ 168,017.17	\$ 168,017.17	0.00%	(Version 1 price)

In St. Miguel Island, because the renewable resources (wind, hydro, and geothermal) are all non-dispatchable, they are treated as negative loads. Therefore, the cost-saving is very limited even given some advanced dispatch approach.

# Scheduling Results for Jan. 16



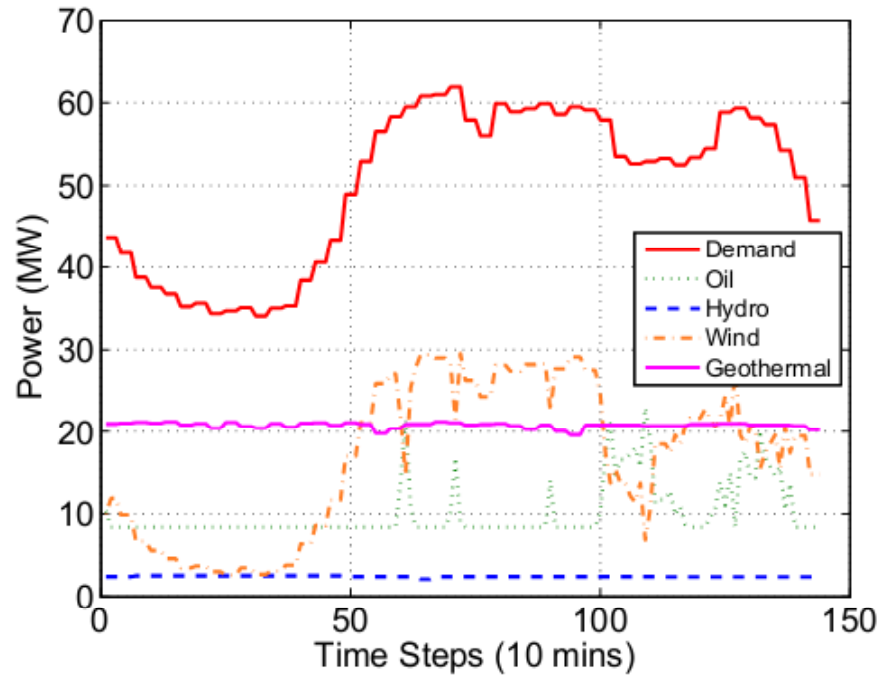
Centralized Static Dispatch



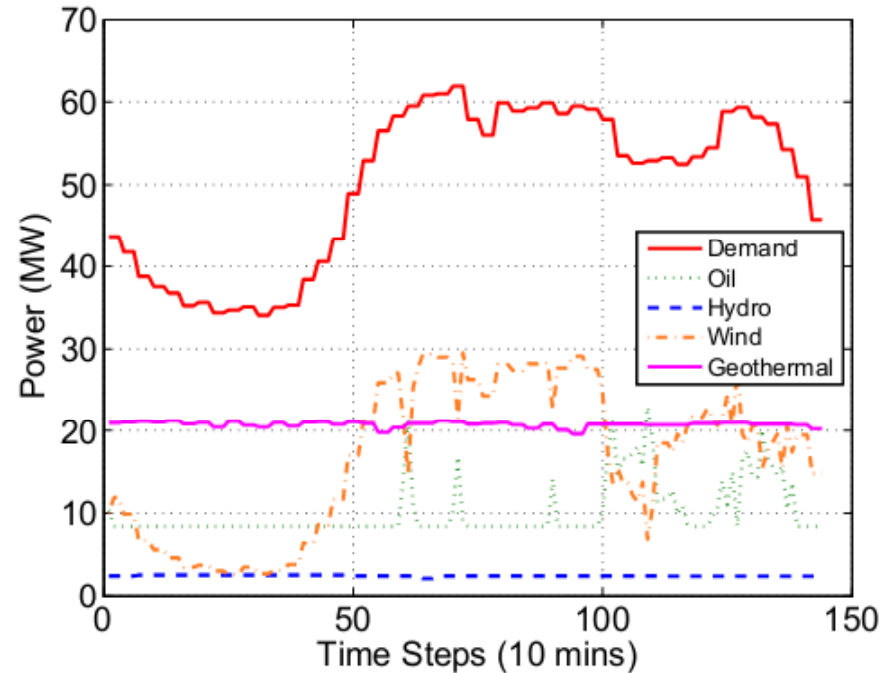
Centralized Look ahead Dispatch

Fig. 4 Generation outputs in St. Miguel on Jan16

# Scheduling Results for Apr. 16



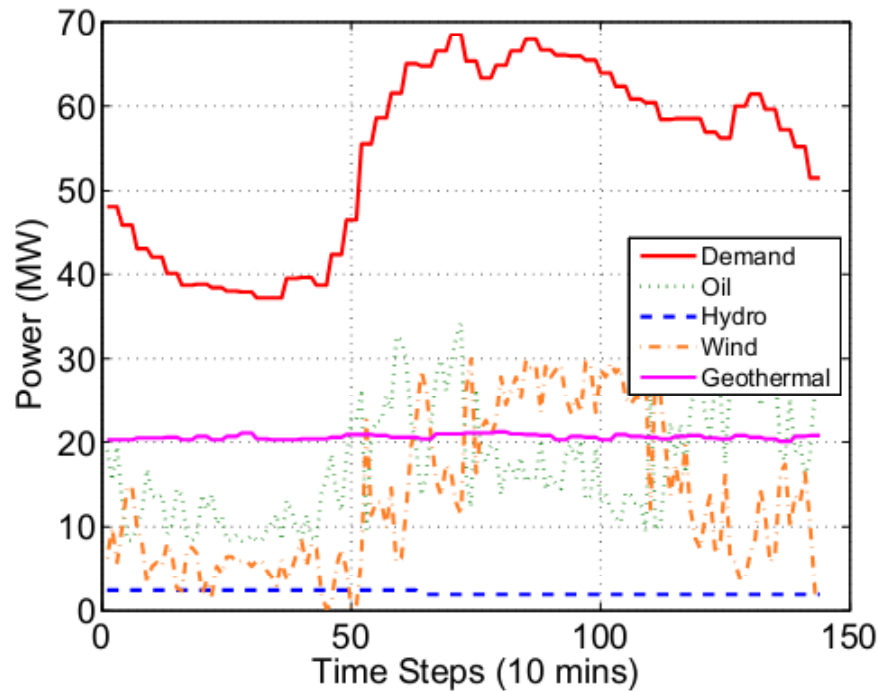
Centralized Static Dispatch



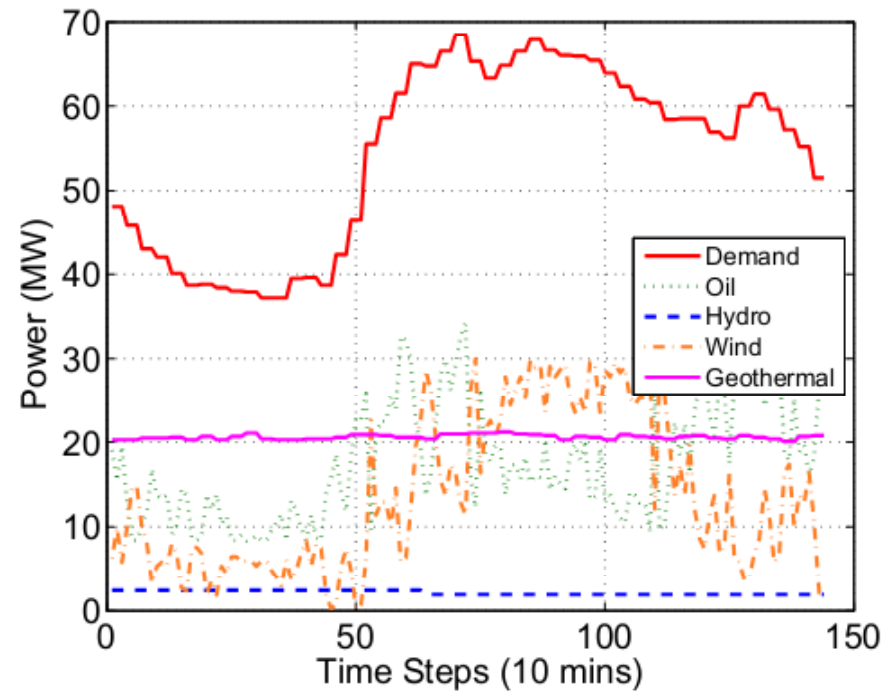
Centralized Look ahead Dispatch

Fig. 5 Generation outputs in St. Miguel on Apr 16

# Scheduling Results for July. 16



Centralized Static Dispatch



Centralized Look ahead Dispatch

Fig. 6 Generation outputs in St. Miguel on July 16

# Scheduling Results for Oct. 15

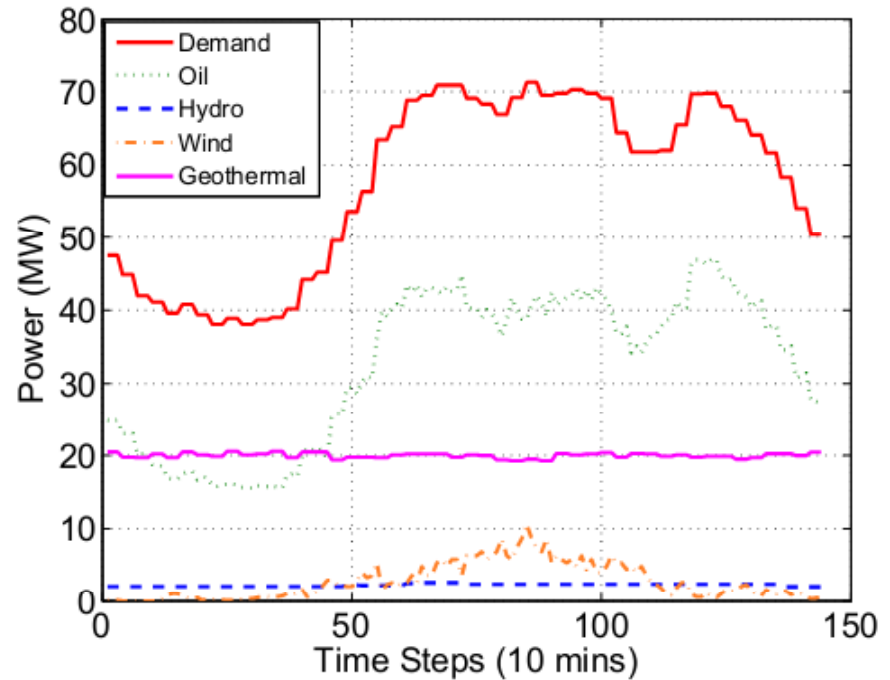
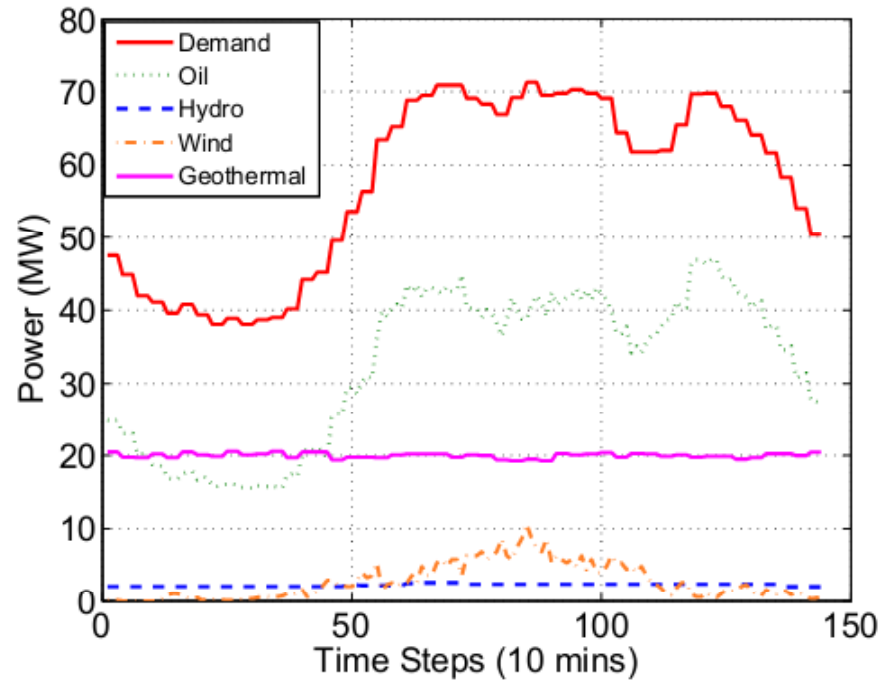


Fig. 7 Generation outputs in St. Miguel on Oct 15



# Conclusions

- Three different dispatch methods are applied in Flores and St. Miguel.
- The cost savings of advanced dispatch methods depend on (1) *relative cost* (2) ramp rate (3) controllability.
- In Flores, look-ahead approach can save about 1.5 % of the total generation cost.
- In St. Miguel, the benefits are limited because of the uncontrollability of hydro, wind and geothermal units.



# Thank You

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