

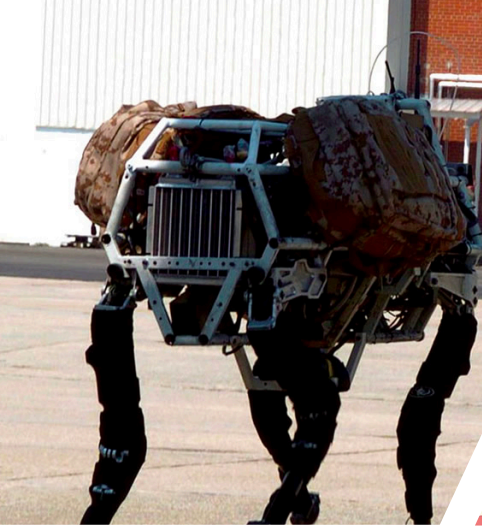
# Influence-Directed Explanations for CNNs

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Klas Leino

# Overview

- Background on Interpretability
- Input Influence
- Internal Influence
  - Slices
  - Distributions of Interest
  - Quantities of Interest
  - Axioms
- Interpretation of Internal Features



Google



Google Search

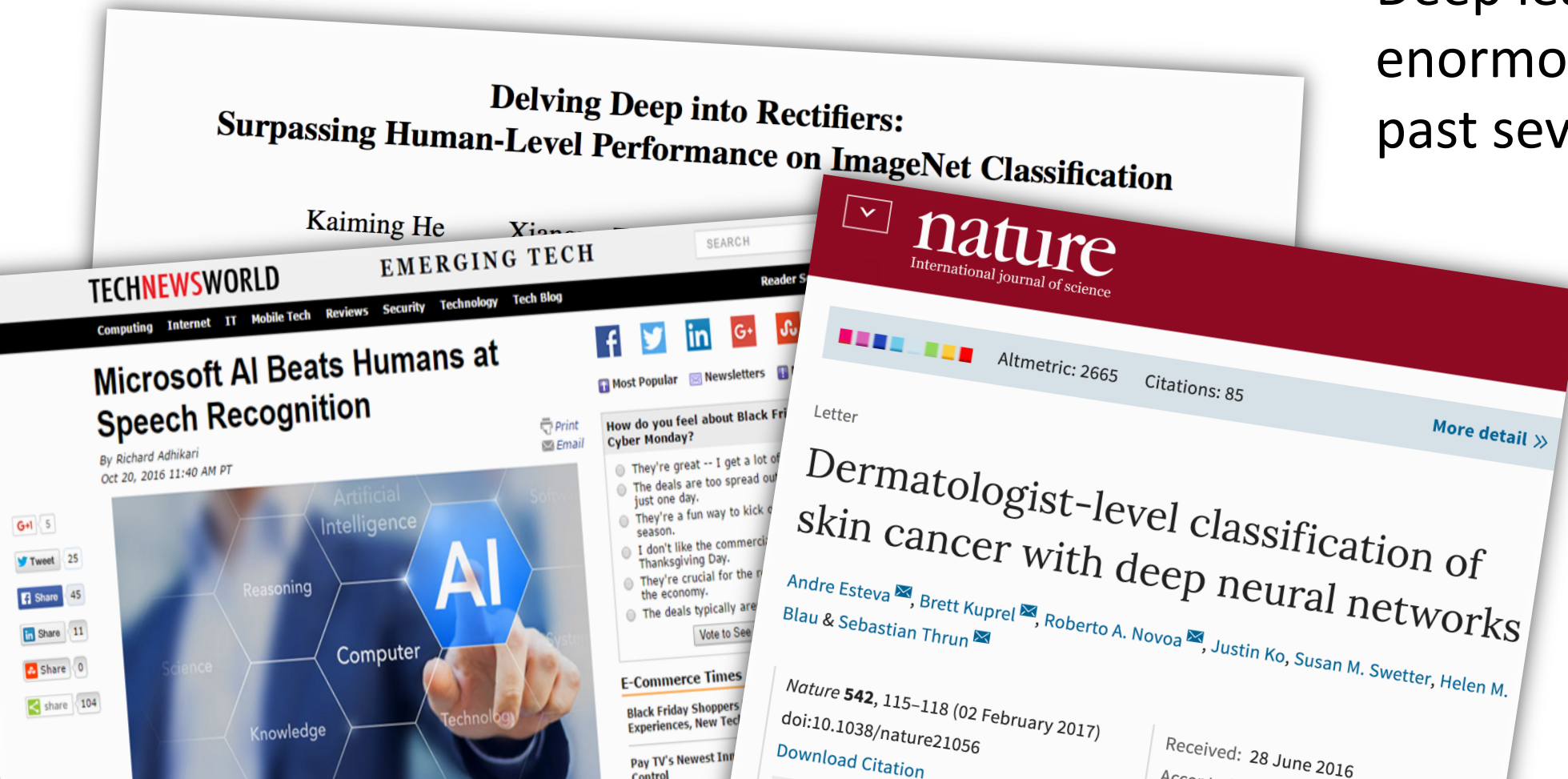
I'm Feeling Lucky



Machine Learning  
is Everywhere

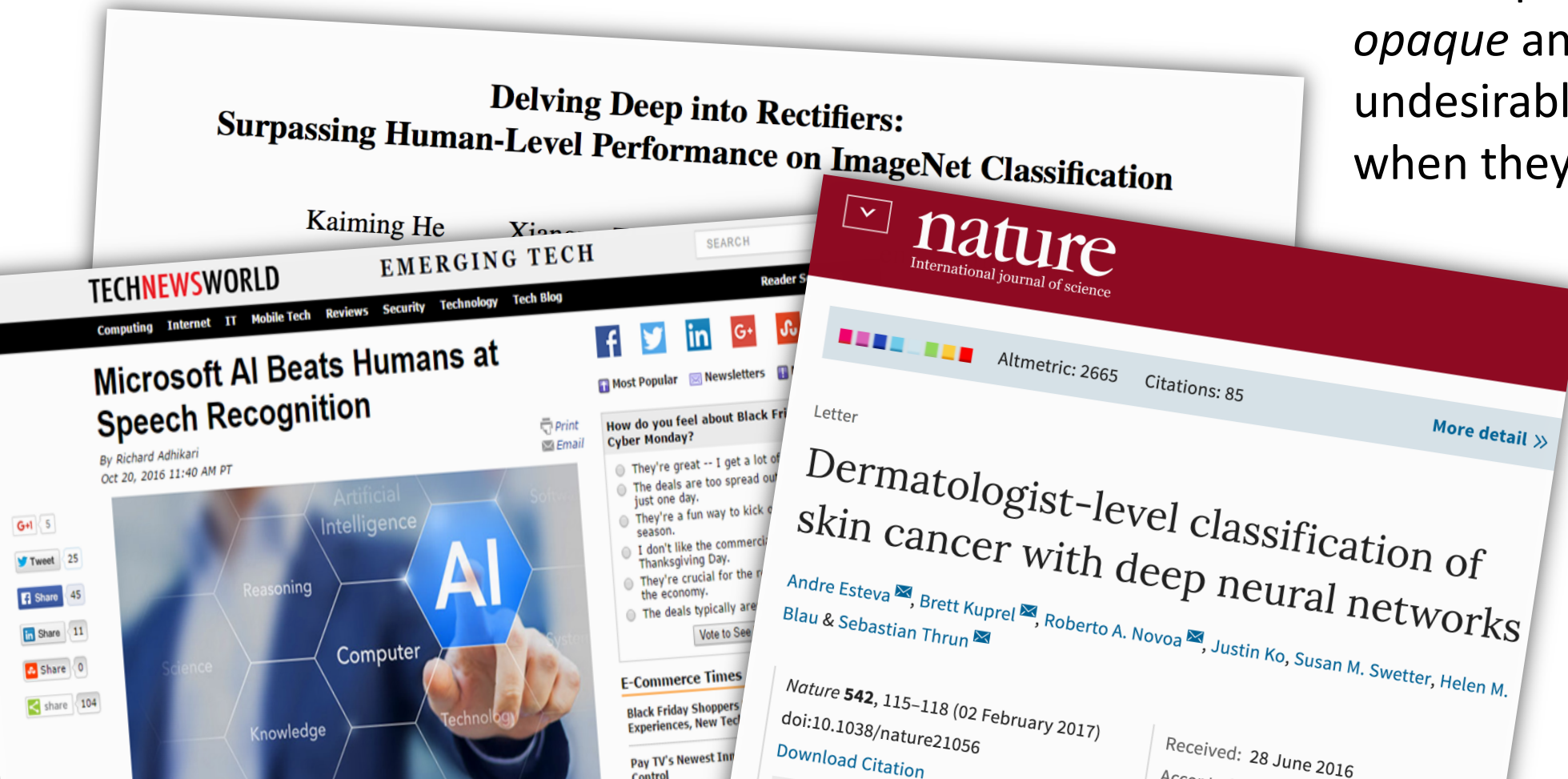
# How Much can We Trust DNN Predictions?

Deep learning has seen enormous success in the past several years



# How Much can We Trust DNN Predictions?

But deep networks remain *opaque* and often exhibit undesirable behavior even when they appear to work well



# Example: Adversarial Attacks

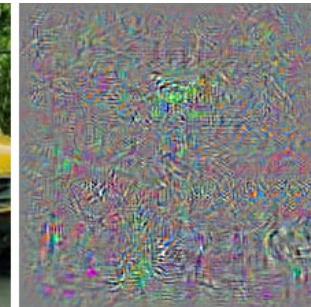


**OSTRICH**

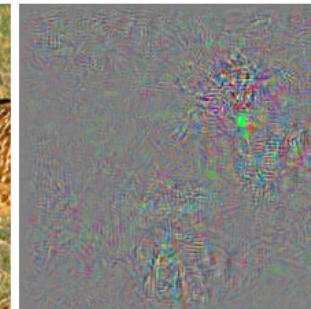
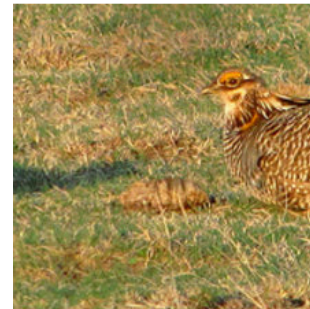


what is this a picture of?

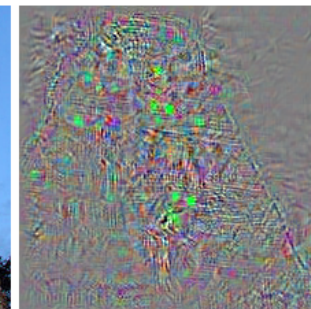
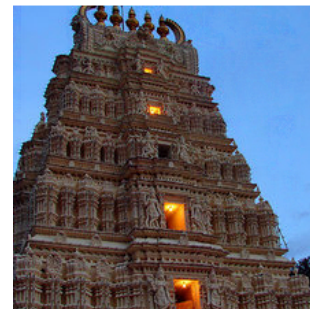
Original Image      Adversarial Perturbation      Perturbed Image



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# Increasing Model Trust

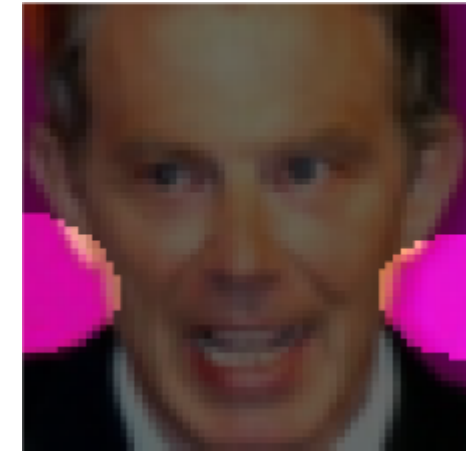
- Generalization error might not be sufficient to instill model trust
- Question: when a model makes a decision, did it make it for the right reason?
- By examining the inner workings of a network, we may be able to address these types of questions

# Example: Overfitting

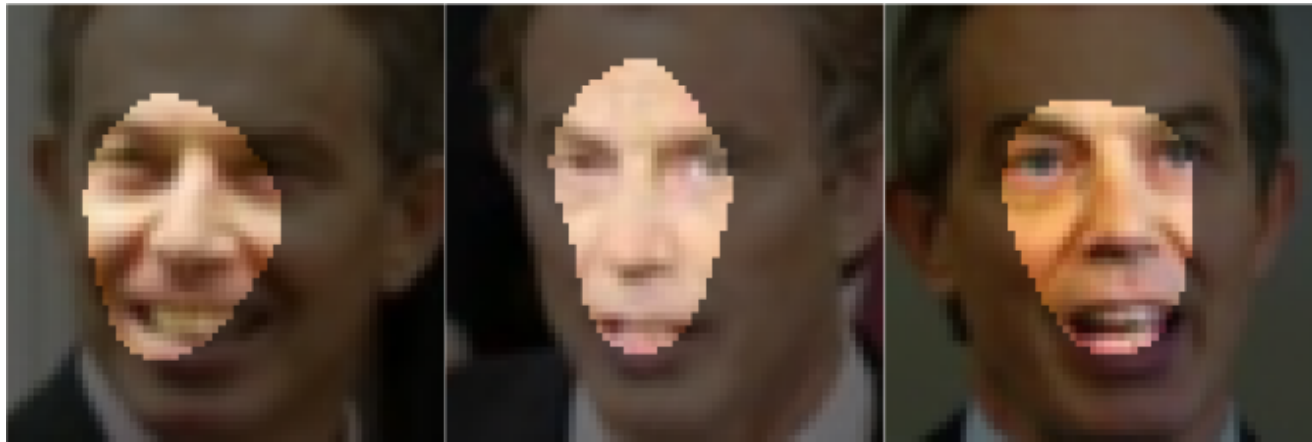
notice the distinctive pink background



Sample of LFW training instances



Explanation [Leino et al. 2018] on training instance of Tony Blair with distinctive pink background. The model uses the background to classify the instance as Tony Blair.



Typical explanations on test instances of Tony Blair



# What Else Might We Want to Understand?

- Explaining mistakes
  - Question: when a model makes a mistake, why?
- Uncovering new knowledge
  - Question: did the model learn a pattern that we overlooked but might find useful?

# Purpose of an Explanation Framework

- Answer *queries* like the questions posed in previous slides
- Goal: provide a framework for rigorously formulating and answering as broad a set of specific queries as possible

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# Notation

- We will take a functional view of a neural network:

*A model is a function,  $f: \mathbb{R}^n \rightarrow \mathbb{R}^m$ , where  $n$  is the number of input features and  $m$  is the number of classes*

- Let  $x \in \mathbb{R}^n$  be an input to the model
  - We say  $x_j$  for  $j \in [n]$  is a *feature* or *variable*
- Let  $f_c(x)$  be the model's output for class  $c$  on input  $x$

# Influence Measures

- An (input) *influence measure*,  $\chi$ , for a model,  $f$ , assigns a value to each of the input features,  $x_i$ , specifying how important  $x_i$  was in determining the model's output,  $f(x)$

# Saliency Maps

- Informally, for an influence measure to be *causal* (with respect to the model), a feature should be considered important if changing it slightly\* would change the output of the model
- Gradient w.r.t. features captures this intuition precisely
- Simple influence definition [Simonyan et al. 2014]

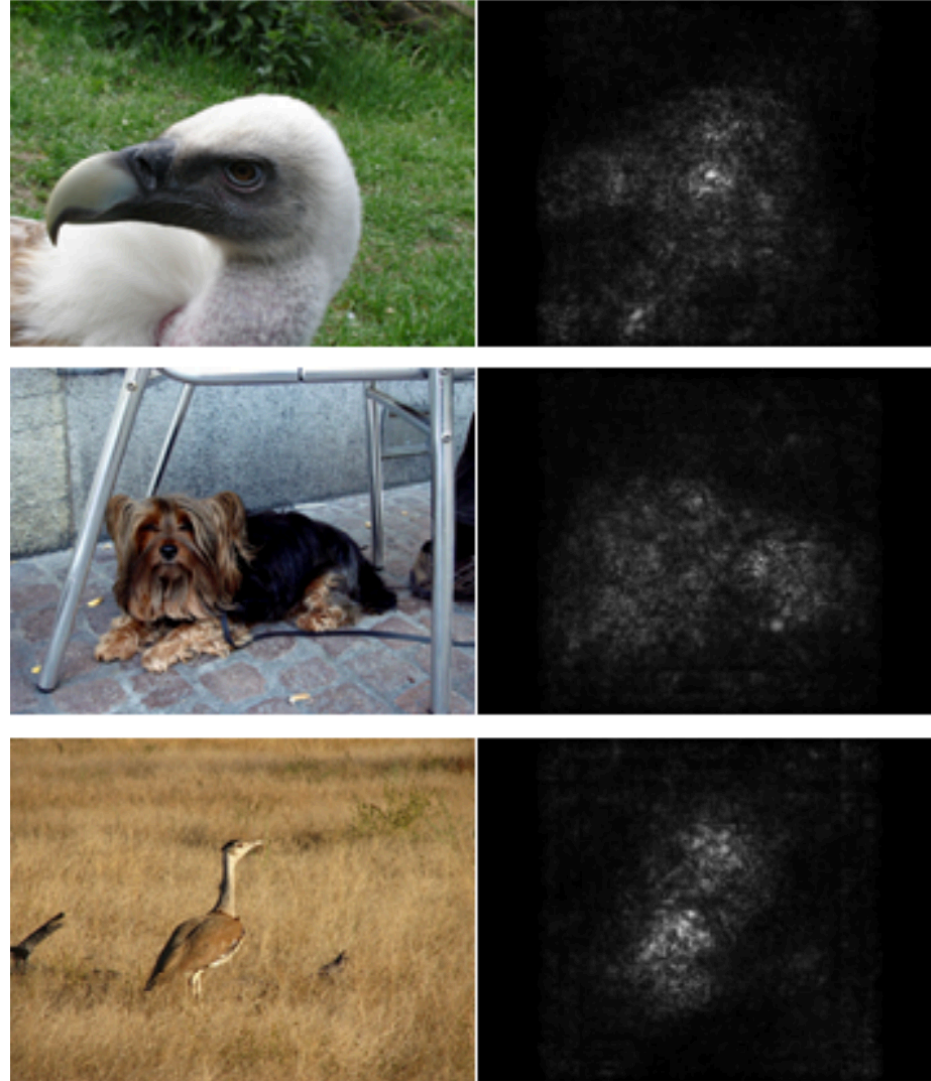
$$\chi_{saliency}(f, \mathbf{x}) = \frac{\partial f_{c'}}{\partial \mathbf{x}}[\mathbf{x}]$$

take the gradient w.r.t. the input

$c'$  is the predicted class

evaluate at the point we are calculating the influence for

# Example: Saliency Maps



[Simonyan et al. 2014]

# Integrated Gradients

- Gradient at a point may describe behavior that is too local
- Example:
  - let  $f(x) = \max\{x, 1\}$  (where  $x \in \mathbb{R}$ , i.e., the input is 1-dimensional)
  - let  $x = 1.5$
  - Then  $f(x) = 1$ , but  $\frac{\partial f}{\partial x}[x] = 0$
  - It seems natural to give some influence to  $x$ , but according to a very local view,  $x$  does not change  $f$
- Integrated gradients [Sundararajan et al. 2017] addresses this by taking the average gradient between the point,  $x$ , and a *baseline* point



# Integrated Gradients

- Integrated gradients [Sundararajan et al. 2017]

$$\chi_{IG}(f, \mathbf{x}, \mathbf{x}_0) = (\mathbf{x} - \mathbf{x}_0) \int_{\alpha=0}^1 \frac{\partial f_{c'}}{\partial \mathbf{x}} [\mathbf{x}_0 + \alpha(\mathbf{x} - \mathbf{x}_0)] d\alpha$$

baseline point

note: this is different from saliency maps conceptually because we multiply the gradient term by the input value (minus the baseline)

this is essentially an integral along the straight-line path from the baseline,  $\mathbf{x}_0$ , to the point,  $\mathbf{x}$

$\alpha$  interpolates between  $\mathbf{x}_0$  and  $\mathbf{x}$

# Example: Integrated Gradients

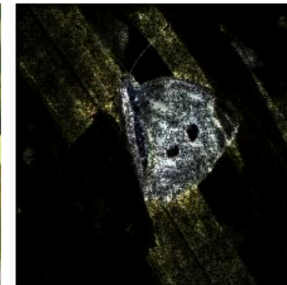
Original image



Integrated gradients



Gradients at image



# Selecting a Baseline

- Baseline is arbitrary, but affects how influence should be interpreted
- Commonly set to zero, i.e., a black image
  - Could be a specific point we want to compare to

# Why Take a Line?

- Line between point and baseline gives rise to some natural axioms
  - **Sensitivity** | states that if the baseline differs from  $\mathbf{x}$  in exactly one variable, and  $f(\mathbf{x}) \neq f(\mathbf{x}_0)$  then that variable must have non-zero influence
  - **Dummy Antisensitivity** | states that if  $f$  does not mathematically depend on a variable, that variable's influence should be zero
  - **Linear Agreement** | states that for a linear model, the influence of each feature is just the weight of that feature
  - **Efficiency** | states that the sum of the influences must be equal to the difference in output on  $\mathbf{x}$  and on  $\mathbf{x}_0$
  - **Symmetry Preserving** | states that symmetrical inputs to  $f$  receive equal influence

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# Generalizing Input Influence

- Become *internal*
  - Assign a meaningful influence score to internal features learned by a deep network
- Become *distributional*
  - Flexibility in defining which points the influence should be supported by
- Support general quantities of interest
  - Flexibility to specify what network behavior we are trying to explain

# Internal Influence

- Internal influence [Leino et al. 2018]

$$\chi_{int}(f = g \circ h, D, q) = \int_{x \in \mathbb{R}^n} \frac{\partial q \circ g}{\partial h(x)} [h(x)] D(x) dx$$

slice

distribution of  
interest ( $\mathcal{D}_I$ )

quantity of  
interest ( $Q_I$ )

take gradient w.r.t.  
internal features

take gradient of  $Q_I$  rather  
than output of  $f$

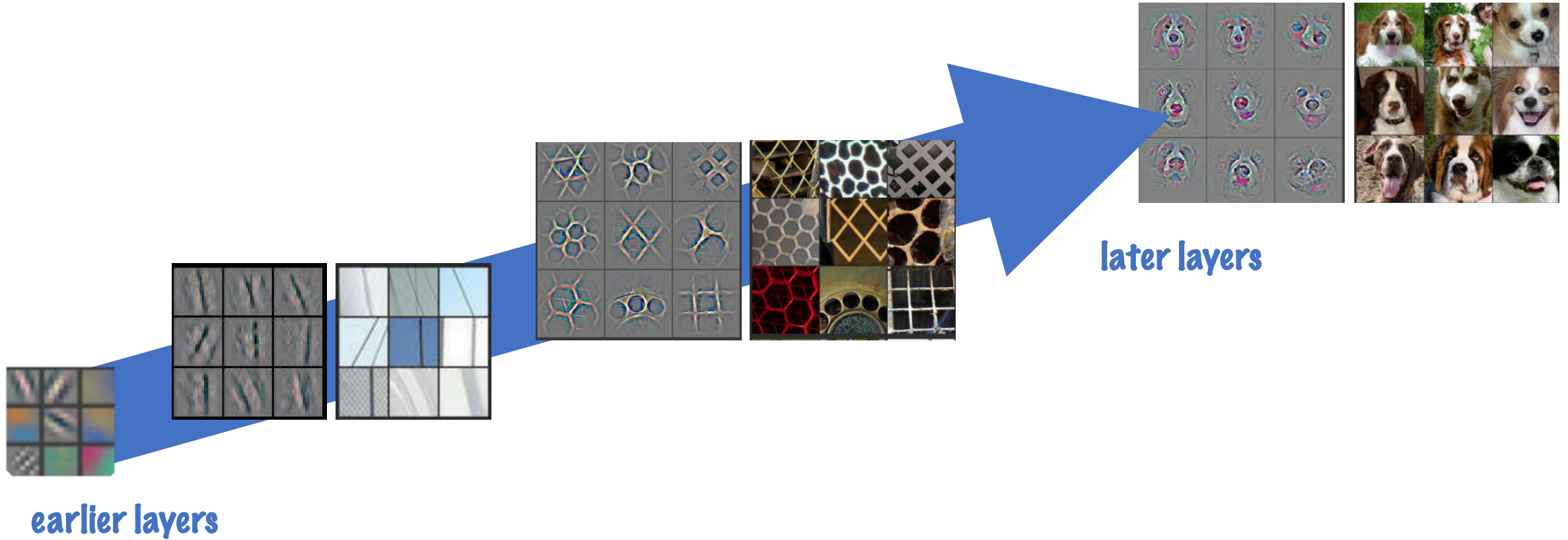
weight each point  
according to the  $\mathcal{D}_I$

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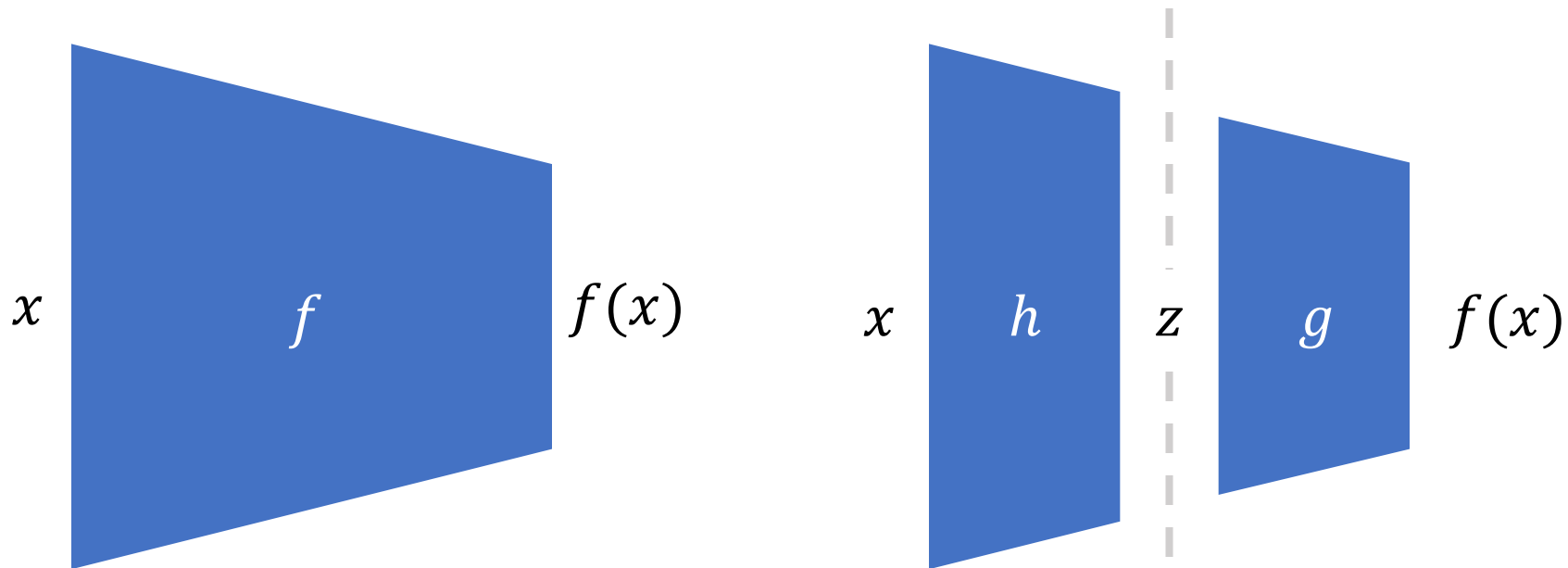


# Different Layers Learn Different Abstractions

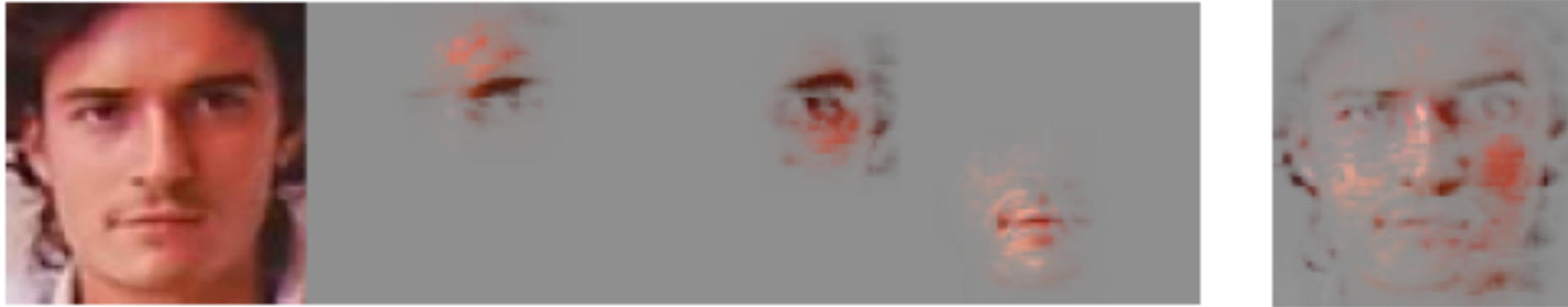


# Slices

- A *slice* of a network,  $f$ , is a pair of functions (or sub-networks),  $\langle g, h \rangle$ , such that  $f = g \circ h$
- Intuitively, this exposes the internals of the network at a chosen layer



# Slices Help Decompose Explanations into Natural Components



Internal Influence

Input Influence

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# Defining the Set of Instances to be Faithful on

- Point may describe behavior that is too local
- Alternatives:
  - Neighborhood around point (smooth gradients)
  - Line to baseline (realizes IG)
  - Entire class
  - All training points
  - Entire space

# Distributions of Interest

- A *distribution of interest* (DoI) is a probability distribution over input points in  $\mathbb{R}^n$ , represented by its PDF,  $D$
- E.g., to get a linear path from  $\mathbf{x}$  to  $\mathbf{x}_0$  (as in IG), we can define the DoI to be a uniform distribution over the points on the line segment between  $\mathbf{x}$  and  $\mathbf{x}_0$ , i.e.,

$$D(\mathbf{x}') = \begin{cases} \frac{1}{|\mathbf{x} - \mathbf{x}_0|} & \text{if } \mathbf{x}' \text{ is on the line segment } \overrightarrow{\mathbf{x}\mathbf{x}_0} \\ 0 & \text{otherwise} \end{cases}$$

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# Defining the Quantity to Explain

- We may be interested in explaining a model behavior besides its prediction, for example
  - Which features contributed to some other class that wasn't chosen by the model?
  - Why was class A chosen rather than class B?
  - Which features contributed to the activation of a particular internal neuron?



# Quantities of Interest

- A *quantity of interest* (QoI) is a function,  $q$ , of the output\* of  $f$  that specifies what network behavior we would like to calculate influence towards.
- E.g.,
  - to use the network's prediction as before,  $q(f(x)) = \max\{f(x)\}$
  - to compare class A with class B,  $q(f(x)) = f_A(x) - f_B(x)$

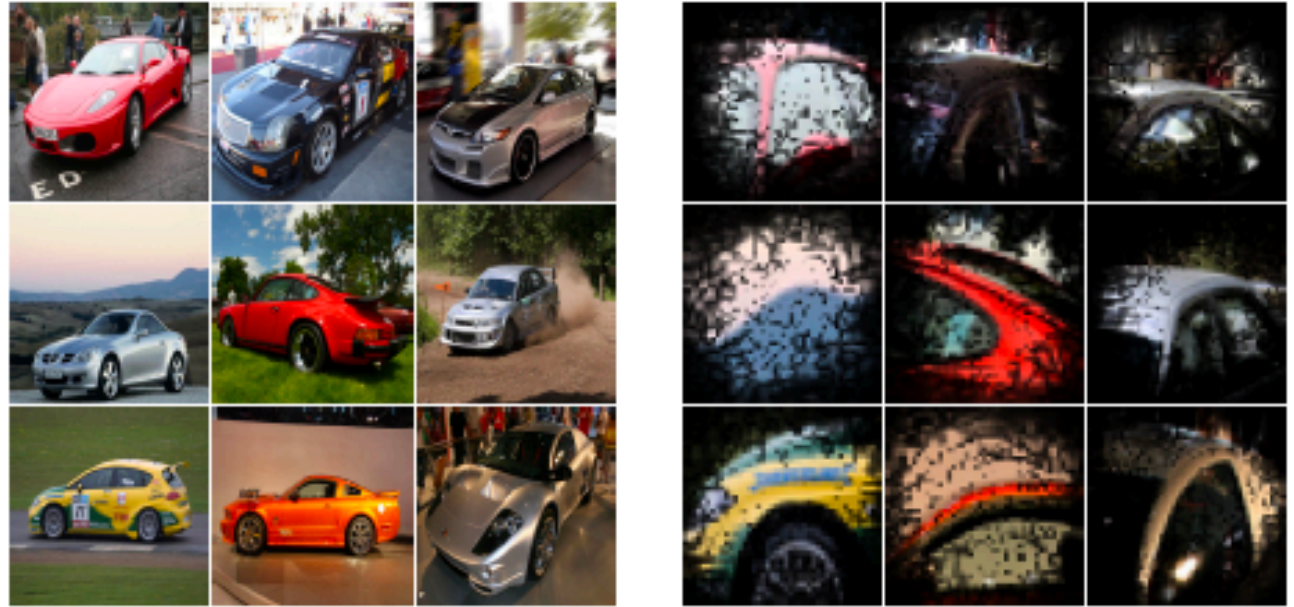
# Example: Comparative Quantities of Interest



Top neuron for quantity  $f_{sportscar}(x)$



Top neuron for (comparative) quantity  $f_{sportscar}(x) - f_{convertible}(x)$



same neuron generalizes to other instances

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# Justification for Internal Influence

- Internal influence follows from a few natural axioms
  - **Linear Agreement** | states that for a linear model, the influence of each feature is just the weight of that feature
  - **(distributional) Marginality** | essentially captures that the influence must be causal with respect to the model – a feature can only get influence according to its marginal contribution to the quantity of interest
  - **Distributional Linearity** | states that each point must be weighted according to its probability density given by the distribution of interest
  - **Slice Invariance** | states that the influence doesn't depend on the implementation of  $h$  and  $g$ , only on the parts of the network that are exposed
  - **Preprocessing** | states that computing internal influence for a slice should be the same as computing input influence for  $g$ , where  $g$ 's inputs are preprocessed by  $h$

# Summary of Internal Influence

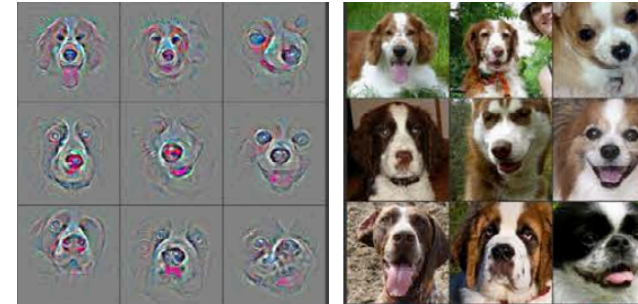
- Goal is to enable a broad set of queries that can be tailored to the specific application/context
  - *Slice* allows us to specify level of abstraction
    - e.g., raw inputs or high-level features
  - *Distribution* allows us to specify relevant points
    - e.g., line from baseline or entire class
  - *Quantity* allows us to specify what we are explaining
    - e.g., specific class or comparison of two classes

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# How do We Interpret Influential Internal Neurons?

- Backpropagation techniques, e.g., Zeiler et al. 2013



- Use input influence with a quantity of interest that selects a particular internal neuron

