1 LC-3b Microcode [40 points]

We wrote the microcode for at least one state of the LC-3b microarchitecture in class. In this homework, you will complete the microcode for states numbered 0, 3, 4, 6, 9, 17, 18, 19, 20, 21, 24, 25, 27, 32, 33, 35 of the LC-3b. Refer to Appendix C of Patt and Patel for the LC-3b state machine and datapath and Appendix A of Patt and Patel for the LC-3b ISA description.

Fill out the microcode in the microcode.csv file handed out with this homework. Enter a 1 or a 0 or an X as appropriate for the microinstructions corresponding to states. You do not need to fill out states 8, 10 and 11. We fill out state 18 as an example. Please turn in this CSV file electronically along with your homework.

2 Addressing Modes [15 points]

We covered the following addressing modes in class:

- Absolute
- Register indirect
- Based (base + displacement)
- Scale indexed (base + index × constant)
- Memory indirect
- Auto increment/decrement (by 1 byte)

Consider the following high-level programs:

- `uint8_t a[150]; // a is allocated in memory
  for (i = 0; i < 150; i++) {
    a[i] = 5;
  }
`

- `int a[150]; // a is allocated in memory
  for (i = 0; i < 150; i++) {
    a[i] = 5;
  }
`

- `int *p; // *p is allocated in memory
  *p = 150;
`

- `int **p; // *p and **p are allocated in memory
  **p = 150;
`

Assume that in the first two programs, a register contains the address of the start of the array, and in the last two programs, a register contains the value of `p`.

For each of the above three programs, which of the addressing modes, do you think, would lead to the minimum number of instructions? (Note that no addressing mode fits perfectly. You might require other instructions for address computation.)
3 Microarchitecture vs. ISA [15 points]

(a) Briefly explain the difference between the microarchitecture level and the ISA level in the transformation hierarchy. What information does the compiler need to know about the microarchitecture of the machine in order to compile the program correctly?

(b) Classify the following attributes of a machine as either a property of its microarchitecture or ISA:

(i) The machine does not have a subtract instruction.
(ii) The ALU of the machine does not have a subtract unit.
(iii) The machine does not have condition codes.
(iv) A 5-bit immediate can be specified in an ADD instruction.
(v) It takes \( n \) cycles to execute an ADD instruction.
(vi) There are 8 general purpose registers.
(vii) A 2-to-1 mux feeds one of the inputs to ALU.
(viii) The register file has one input port and two output ports.

4 Single-Cycle Processor Datapath [30 points]

In this problem, you will modify the single-cycle datapath we built up in lecture to support the JAL instruction. The datapath that we will start with (from Lecture 5, Slide 53) has been reproduced on the next page. Your job is to implement the necessary data and control signals to support the JAL instruction, which we define to have the following semantics:

\[
\text{JAL} : \quad R31 \leftarrow PC + 4 \\
PC \leftarrow PC_{31...28} \| \text{Immediate} \| 0^2
\]

Add to the datapath on the next page the necessary data and control signals to implement the JAL instruction. Draw and label all components and wires very clearly (give control signals meaningful names; if selecting a subset of bits from many, specify exactly which bits are selected; and so on).
5 Pipelining [30 points]

Given the following code:

```
MUL R3, R1, R2
ADD R5, R4, R3
ADD R6, R4, R1
MUL R7, R8, R9
ADD R4, R3, R7
MUL R10, R5, R6
```

Note: Each instruction is specified with the destination register rst.

Calculate the number of cycles it takes to execute the given code on the following models:

(i) A non-pipelined machine
(ii) A pipelined machine with scoreboarding and five adders and five multipliers without data forwarding
(iii) A pipelined machine with scoreboarding and five adders and five multipliers with data forwarding.
(iv) A pipelined machine with scoreboarding and one adder and one multiplier without data forwarding
(v) A pipelined machine with scoreboarding and one adder and one multiplier with data forwarding

Note: For all machine models, use the basic instruction cycle as follows:

- Fetch (one clock cycle)
- Decode (one clock cycle)
- Execute (MUL takes 6, ADD takes 4 clock cycles). The multiplier and the adder are not pipelined.
- Write-back (one clock cycle)

Do not forget to list any assumptions you make about the pipeline structure (e.g., how is data forwarding done between pipeline stages)

6 Fine Grain Multithreading [40 points]

Consider a design “Machine I” with five pipeline stages: fetch, decode, execute, memory and writeback. Each stage takes 1 cycle. The instruction and data caches have 100% hit rates (i.e., there is never a stall for a cache miss). Branch directions and targets are resolved in the execute stage. The pipeline stalls when a branch is fetched, until the branch is resolved. Dependency check logic is implemented in the decode stage to detect flow dependences. The pipeline does not have any forwarding paths, so it must stall on detection of a flow dependence.

In order to avoid these stalls, we will consider modifying Machine I to use fine-grained multithreading.

(a) In the five stage pipeline of Machine I shown below, clearly show what blocks you would need to add in each stage of the pipeline, to implement fine-grained multithreading. You can replicate any of the blocks and add muxes. You don’t need to implement the mux control logic (although provide an intuitive name for the mux control signal, when applicable).
(b) The machine’s designer first focuses on the branch stalls, and decides to use fine-grained multithreading to keep the pipeline busy no matter how many branch stalls occur. What is the minimum number of threads required to achieve this? Why?

(c) The machine’s designer now decides to eliminate dependency-check logic and remove the need for flow-dependence stalls (while still avoiding branch stalls). How many threads are needed to ensure that no flow dependence ever occurs in the pipeline? Why?

A rival designer is impressed by the throughput improvements and the reduction in complexity that FGMT brought to Machine I. This designer decides to implement FGMT on another machine, Machine II. Machine II is a pipelined machine with the following stages.

<table>
<thead>
<tr>
<th>Stage</th>
<th>Stages</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fetch</td>
<td>1 stage</td>
</tr>
<tr>
<td>Decode</td>
<td>1 stage</td>
</tr>
<tr>
<td>Execute</td>
<td>8 stages (branch direction/target are resolved in the first execute stage)</td>
</tr>
<tr>
<td>Memory</td>
<td>2 stages</td>
</tr>
<tr>
<td>Writeback</td>
<td>1 stage</td>
</tr>
</tbody>
</table>

Assume everything else in Machine II is the same as in Machine I.

(d) Is the number of threads required to eliminate branch-related stalls in Machine II the same as in Machine I?

**YES NO** (Circle one)

If yes, why? If no, how many threads are required?

(e) What is the minimum CPI (i.e., maximum performance) of each thread in Machine II when this minimum number of threads is used?

(f) Now consider flow-dependence stalls. Does Machine II require the same minimum number of threads as Machine I to avoid the need for flow-dependence stalls?

**YES NO** (Circle one)

If yes, why? If no, how many threads are required?

(g) What is the minimum CPI of each thread when this number of threads (to cover flow-dependence stalls) is used?

(h) After implementing fine grained multithreading, the designer of Machine II optimizes the design and compares the pipeline throughput of the original Machine II (without FGMT) and the modified Machine II (with FGMT) both machines operating at their maximum possible frequency, for several code sequences. On a particular sequence that has no flow dependences, the designer is surprised to see that the new Machine II (with FGMT) has lower overall throughput (number of instructions retired by the pipeline per second) than the old Machine II (with no FGMT). Why could this be? Explain concretely.
Assume a machine with a 7-stage pipeline. Assume that branches are resolved in the sixth stage. Assume that 20% of instructions are branches.

(a) How many instructions of wasted work are there per branch misprediction on this machine?

(b) Assume $N$ instructions are on the correct path of a program and assume a branch predictor accuracy of $A$. Write the equation for the number of instructions that are fetched on this machine in terms of $N$ and $A$. (Please show your work for full credit.)

(c) Let’s say we modified the machine so that it used dual path execution like we discussed in class (where an equal number of instructions are fetched from each of the two branch paths). Assume branches are resolved before new branches are fetched. Write how many instructions would be fetched in this case, as a function of $N$. (Please show your work for full credit.)

(d) Now let’s say that the machine combines branch prediction and dual path execution in the following way:

A branch confidence estimator, like we discussed in class, is used to gauge how confident the machine is of the prediction made for a branch. When confidence in a prediction is high, the branch predictor’s prediction is used to fetch the next instruction; When confidence in a prediction is low, dual path execution is used instead.

Assume that the confidence estimator estimates a fraction $C$ of the branch predictions have high confidence, and that the probability that the confidence estimator is wrong in its high confidence estimation is $M$.

Write how many instructions would be fetched in this case, as a function of $N$, $A$, $C$, and $M$. (Please show your work for full credit.)
8 Mystery Instruction [40 points]

A pesky engineer implemented a mystery instruction on the LC-3b. It is your job to determine what the instruction does. The mystery instruction is encoded as:

```
15 14 13 12 11 10  9  8  7  6  5  4  3  2  1  0
1010  BaseR  SR1  0  0  0  0  1  0
```

The instruction is only defined if the value of SR1 is greater than zero.

The modifications we make to the LC-3b datapath and the microsequencer are highlighted in the attached figures (see the last four pages). We also provide the original LC-3b state diagram, in case you need it. (As a reminder, the selection logic for SR2MUX is determined internally based on the instruction.)

The additional control signals are

- **GateTEMP1/1**: NO, YES
- **GateTEMP2/1**: NO, YES
- **LD.TEMP1/1**: NO, LOAD
- **LD.TEMP2/1**: NO, LOAD

**COND/3:**

- **COND<sub>000</sub>**: Unconditional
- **COND<sub>001</sub>**: Memory Ready
- **COND<sub>010</sub>**: Branch
- **COND<sub>011</sub>**: Addressing mode
- **COND<sub>100</sub>**: Mystery 1

The microcode for the instruction is given in the table below.

<table>
<thead>
<tr>
<th>State</th>
<th>Cond</th>
<th>J</th>
<th>Asserted Signals</th>
</tr>
</thead>
<tbody>
<tr>
<td>001010</td>
<td>COND&lt;sub&gt;000&lt;/sub&gt;</td>
<td>001011</td>
<td>ALUK = PASSA, GateALU, LD.TEMP2, SR1MUX = SR1 (IR[8:6])</td>
</tr>
<tr>
<td>001011</td>
<td>COND&lt;sub&gt;000&lt;/sub&gt;</td>
<td>110001</td>
<td>LD.MAR, SR1MUX = BaseR (IR[11:9]), ADDR1MUX = BaseR, ADDR2MUX = 0, MARMUX = ADDER, GateMARMUX</td>
</tr>
<tr>
<td>110001</td>
<td>COND&lt;sub&gt;001&lt;/sub&gt;</td>
<td>110001</td>
<td>LD.MDR, MIO.EN, DATA.SIZE=WORD</td>
</tr>
<tr>
<td>110011</td>
<td>COND&lt;sub&gt;000&lt;/sub&gt;</td>
<td>100100</td>
<td>GateMDR, LD.TEMP1, DATA.SIZE=WORD</td>
</tr>
<tr>
<td>100100</td>
<td>COND&lt;sub&gt;000&lt;/sub&gt;</td>
<td>100101</td>
<td>GateTEMP1, LD.MDR, DATA.SIZE=WORD</td>
</tr>
<tr>
<td>100101</td>
<td>COND&lt;sub&gt;001&lt;/sub&gt;</td>
<td>100101</td>
<td>R.W=WRITE, DATA.SIZE=WORD</td>
</tr>
<tr>
<td>100111</td>
<td>COND&lt;sub&gt;000&lt;/sub&gt;</td>
<td>101000</td>
<td>GateMARMUX, MARMUX = ADDER, ADDR1MUX = BaseR (IR[11:9]), ADDR2MUX = SEXT[IR[5:0]], DRMUX = BaseR (IR[11:9]), LD.REG</td>
</tr>
<tr>
<td>101000</td>
<td>COND&lt;sub&gt;100&lt;/sub&gt;</td>
<td>001011</td>
<td>GateTEMP2, LD.TEMP2</td>
</tr>
</tbody>
</table>

Describe what this instruction does.
9  REP MOVS Déjà Vu [40 points]

Recall from Homework 1 that we can translate code under Complex Instruction Set Computing (CISC) ISA to Reduced Instruction Set Computing (RISC) ISAs. Similarly, we can implement a CISC instruction using microprogrammed microarchitectures as well. Here you will implement the LC-3b equivalent for a single Intel x86 instruction, REP MOVS, which is almost similar to REP MOVSB instruction but move words instead of bytes.

The REP MOVS instruction uses three fixed x86 registers: ECX (count), ESI (source), and EDI (destination). The repeat (REP) prefix on the instruction indicates that it will repeat ECX times. Each iteration, it moves one word from memory at address ESI to memory at address EDI, and then increments both pointers by one. Thus, the instruction copies ECX bytes from address ESI to address EDI. For those who are interested, the Intel architecture manual (found on the wiki at [http://www.ece.cmu.edu/~ece447/s15/doku.php?id=techdocs](http://www.ece.cmu.edu/~ece447/s15/doku.php?id=techdocs)).

1. How would you implement REP MOVS if your goal is to minimize the amount of additional hardware you add to the basic microprogrammed LC-3b design discussed in class? Show all your work and design decisions. Write your assumptions.

2. How would you implement REP MOVS if your goal is to minimize the latency of the instruction? Show all your work and design decisions. Write your assumptions.
Address of Next State
Suppose it takes memory five cycles to read a value. That is, once MAR contains the address to be read and the microinstruction asserts READ, it will take five cycles before the contents of the specified location in memory are available to be loaded into MDR. (Note that the microinstruction asserts READ by means of three control signals: MIO.EN/YES, R.W/RD, and DATA.SIZE/WORD; see Figure C.3.)

Recall our discussion in Section C.2 of the function of state 33, which accesses an instruction from memory during the fetch phase of each instruction cycle. For the LC-3b to operate correctly, state 33 must execute five times before moving on to state 35. That is, until MDR contains valid data from the memory locations specified by the content of MAR, we want state 33 to continue to re-execute. After five clock cycles, the value in MDR will be available for use.
C.2. THE STATE MACHINE

Figure C.2: A state machine for the LC-3b

NOTES
- Base + SEXT[off6]
- PC+off9: PC + SEXT[off9]
- *OP2 may be SR2 or SEXT[imm5]
- ** [15:8] or [7:0] depending on MAR[0]