CMU 18-447 Introduction to Computer Architecture, Spring 2012

Handout 10/ HW 5: Out-of-order processing, Caches, Memory

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Due: **Monday, Apr 2, 2012**

1 Out-of-order Execution

A five instruction sequence executes according to Tomasulo's algorithm. Each instruction is of the form ADD DR,SR1,SR2 or MUL DR,SR1,SR2. ADDs are pipelined and take 9 cycles (F-D-E1-E2-E3-E4-E5-E6-WB). MULs are also pipelined and take 11 cycles (two extra execute stages). An instruction must wait until a result is in a register before it sources it (reads it as a source operand). For instance, if instruction 2 has a read-after-write dependence on instruction 1, instruction 2 can start executing in the next cycle after instruction 1 writes back (shown below).

```
instruction 1     |F|D|E1|E2|E3|..... |WB|
instruction 2       |F|D |- |- |..... |- |E1|
```

The machine can fetch one instruction per cycle, and can decode one instruction per cycle.

The register file before and after the sequence are shown below.

	Valid	Tag	Value
R0	1		4
R1	1		5
R2	1		6
R3	1		7
R4	1		8
R5	1		9
R6	1		10
R7	1		11

(a) Before

	Valid	Tag	Value
R0	1		310
R1	1		5
R2	1		410
R3	1		31
R4	1		8
R5	1		9
R6	1		10
R7	1		21

(b) After

(a) Complete the five instruction sequence in program order in the space below. Note that we have helped you by giving you the opcode and two source operand addresses for the fourth instruction. (The program sequence is unique.)

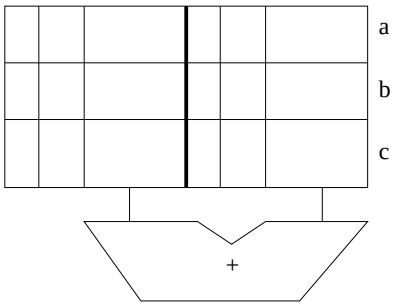
Give instructions in the following format: "opcode destination ⇐ source1, source2."

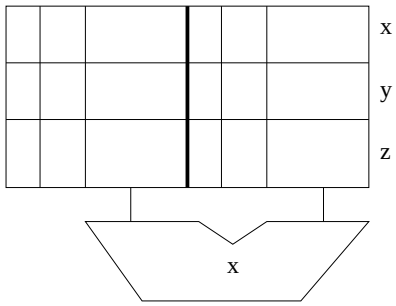
		⇐		,	
		⇐		,	
		⇐		,	
MUL		⇐	R6	,	R6
		⇐		,	

(b) In each cycle, a single instruction is fetched and a single instruction is decoded.

Assume the reservation stations are all initially empty. Put each instruction into the next available reservation station. For example, the first ADD goes into "a". The first MUL goes into "x". Instructions remain in the reservation stations until they are completed. Show the state of the reservation stations at the end of cycle 8.

Note: to make it easier for the grader, when allocating source registers to reservation stations, please always have the higher numbered register be assigned to source2



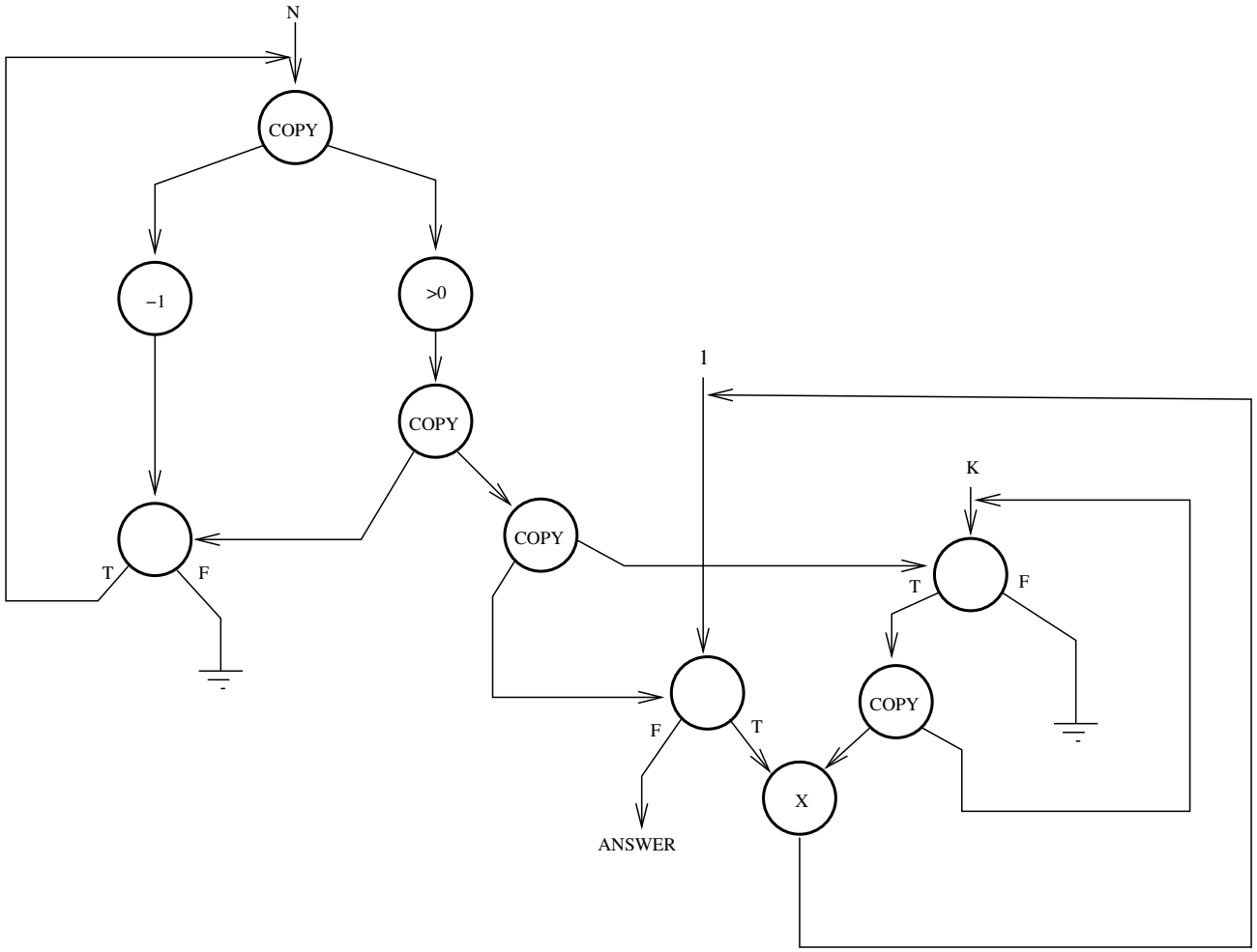


(c) Show the state of the Register Alias Table (Valid, Tag, Value) at the end of cycle 8.

	Valid	Tag	Value
R0			
R1			
R2			
R3			
R4			
R5			
R6			
R7			

2 Data flow

The following data flow graph requires three non-negative integer input values 1 (one), N, k as shown. It produces a value Answer, also shown.



What function does this data flow graph perform (in less than ten words, please)?

3 Vector Processing

Consider the following piece of code:

```
for (i = 0; i < 100; i ++)
  A[i] = ((B[i] * C[i]) + D[i])/2;
```

(a) Translate this code into assembly language using the following instructions in the ISA (note the number of cycles each instruction takes is shown with each instruction):

Opcode	Operands	Number of Cycles	Description
LEA	Ri, X	1	Ri ← address of X
LD	Ri, Rj, Rk	11	Ri ← MEM[Rj + Rk]
ST	Ri, Rj, Rk	11	MEM[Rj + Rk] ← Ri
MOVI	Ri, Imm	1	Ri ← Imm
MUL	Ri, Rj, Rk	6	Ri ← Rj x Rk
ADD	Ri, Rj, Rk	4	Ri ← Rj + Rk
ADD	Ri, Rj, Imm	4	Ri ← Rj + Imm
RSHFA	Ri, Rj, amount	1	Ri ← RSHFA (Rj, amount)
BRcc	X	1	Branch to X based on condition codes

Assume it takes one memory location to store each element of the array. Also assume that there are 8 registers (R0-R7).

Condition codes are set after the execution of an arithmetic instruction. You can assume typically available condition codes such as zero, positive, negative.

How many cycles does it take to execute the program?

(b) Now write Cray-like vector/assembly code to perform this operation in the shortest time possible. Assume that there are 8 vector registers and the length of each vector register is 64. Use the following instructions in the vector ISA:

Opcode	Operands	Number of Cycles	Description
LD	Vst, #n	1	Vst ← n. Vst - Vector Stride Register
LD	Vln, #n	1	Vln ← n. Vln - Vector Length Register
VLD	Vi, X	11, pipelined	
VST	Vi, X	11, pipelined	
Vmul	Vi, Vj, Vk	6, pipelined	
Vadd	Vi, Vj, Vk	4, pipelined	
Vrshfa	Vi, Vj, amount	1	

How many cycles does it take to execute the program on the following processors? Assume that memory is 16-way interleaved.

(i) Vector processor without chaining, 1 port to memory (1 load or store per cycle)

(ii) Vector processor with chaining, 1 port to memory

(iii) Vector processor with chaining, 2 read ports and 1 write port to memory

4 Caching

Below, we have given you four different sequences of addresses generated by a program running on a processor with a data cache. Cache hit ratio for each sequence is also shown below. Assuming that the cache is initially empty at the beginning of each sequence, find out the following parameters of the processor's data cache:

- Associativity (1, 2 or 4 ways)
- Block size (1, 2, 4, 8, 16, or 32 bytes)
- Total cache size (256B, or 512B)
- Replacement policy (LRU or FIFO)

Assumptions: all memory accesses are one byte accesses. All addresses are byte addresses.

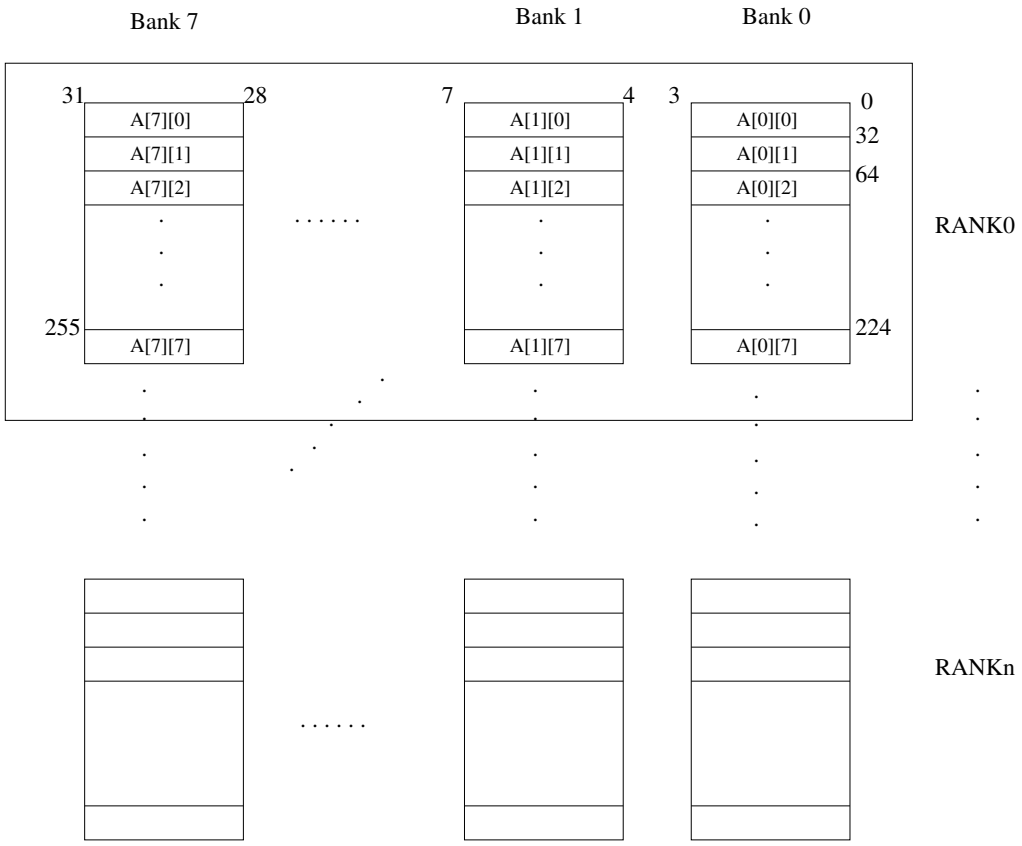
Sequence No.	Address Sequence	Hit Ratio
1	0, 2, 4, 8, 16, 32	0.33
2	0, 512, 1024, 1536, 2048, 1536, 1024, 512, 0	0.33
3	0, 64, 128, 256, 512, 256, 128, 64, 0	0.33
4	0, 512, 1024, 0, 1536, 0, 2048, 512	0.25

5 Main Memory Organization and Interleaving

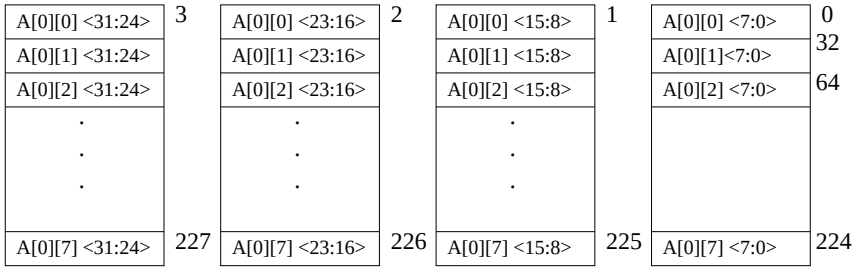
Consider the following piece of code:

```
for(i = 0; i < 8; ++i){
  for(j = 0; j < 8; ++j){
    sum = sum + A[i][j];
  }
}
```

The figure below shows an 8-way interleaved, byte-addressable memory. The total size of the memory is 4KB. The elements of the 2-dimensional array, A, are 4-bytes in length and are stored in the memory in column-major order (i.e., columns of A are stored in consecutive memory locations) as shown. The width of the bus is 32 bits, and each memory access takes 10 cycles.



A more detailed picture of the memory chips in Bank 0 of Rank 0 is shown below.



(a) Since the address space of the memory is 4KB, 12 bits are needed to uniquely identify each memory location, i.e., Addr[11:0]. Specify which bits of the address will be used for:

- Byte on bus
  Addr [_____ : _____]
- Interleave/Bank bits
  Addr [_____ : _____]
- Chip address
  Addr [_____ : _____]
- Rank bits
  Addr [_____ : _____]

(b) How many cycles are spent accessing memory during the execution of the above code? Compare this with the number of memory access cycles it would take if the memory were not interleaved (i.e., a single 4-byte wide array).

(c) Can any change be made to the current interleaving scheme to optimize the number of cycles spent accessing memory? If yes, which bits of the address will be used to specify the byte on bus, interleaving, etc. (use the same format as in part a)? With the new interleaving scheme, how many cycles are spent accessing memory? Remember that the elements of A will still be stored in column-major order.

(d) Using the original interleaving scheme, what small changes can be made to the piece of code to optimize the number of cycles spent accessing memory? How many cycles are spent accessing memory using the modified code?

6 Virtual Memory

An ISA supports an 8-bit, byte-addressable virtual address space. The corresponding physical memory has only 128 bytes. Each page contains 16 bytes. A simple, one-level translation scheme is used and the page table resides in physical memory. The initial contents of the frames of physical memory are shown below.

Frame Number	Frame Contents
0	Empty
1	Page 13
2	Page 5
3	Page 2
4	Empty
5	Page 0
6	Empty
7	Page Table

A three-entry Translation Lookaside Buffer that uses LRU replacement is added to this system. Initially, this TLB contains the entries for pages 0, 2, and 13. For the following sequence of references, put a circle around those that generate a TLB hit and put a rectangle around those that generate a page fault. What is the hit rate of the TLB for this sequence of references? (Note: LRU policy is used to select pages for replacement in physical memory.)

References (to pages): 0, 13, 5, 2, 14, 14, 13, 6, 6, 13, 15, 14, 15, 13, 4, 3.

(a) At the end of this sequence, what three entries are contained in the TLB?

(b) What are the contents of the 8 physical frames?